Preloaded structures for space exploration vehicles

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Abstract. This paper is devoted to the design and simulation of a rover equipped with 4 preloaded structure legs. Space exploration vehicles (rovers) are employed for moving sensors, transporting planet samples and manipulating small modules. In order to perform such tasks with high accuracy, high mechanical stiffness frames are required. At the same time, a certain degree of compliance is required to mitigate mechanical stress caused by motion over a rough surface or in case of unexpected collisions. For this reasons, preloaded structures could represent a suitable solution. They present sharp stiff-to-compliant transitions at design-determined load thresholds. The paper describes the dynamic model of a single rover leg, the simulation of an impact event and the overall design of system.

Keywords: Rover, space exploration, preloaded structures, S-structures, dynamic model.

1 Introduction

Space exploration vehicles (rovers) are employed for moving sensors, transporting planet samples and manipulating small modules [1]. In order to perform such tasks with high accuracy, high mechanical stiffness frames are required. At the same time, a certain degree of compliance is required to mitigate mechanical stress caused by motion over a rough surface or in case of unexpected collisions [2]. Preloaded structures can be the effective solution to the problem. These structures are fitted with preloaded springs, in such a way that they exhibit a compliant behavior only when a threshold load is reached [3].

In mechanics, for a single DoF, elasticity is modelled as a linear relation $F = kx$ between force F and deformation x , where k is the elastic coefficient. However, for the preloaded structures high stiffness is exhibited up to a certain load, and past that, compliance: this non-linear behaviour (bilinear) is shown in Fig. 1. Indeed, the simplest “soft” linearly elastic compliant link or actuator would have very poor performances, causing oscillations and poor dynamic stability during normal operation. One solution to this problem is applying a preload to

the relevant elastic components. This arrangement effectively splits the elastic field in two areas, based on loading conditions: one where the system is as rigid as the material which is used for the structure (elastic coefficient k_1) and the other where rigidity is given by the elastic components (coefficient k_2); typically $k_1 \gg k_2$. In the plot, F_p is the preload force: indeed, if the applied force $F < F_p$, then, in this case, the resulting deformation x can be less substantial.

Fig. 1 Force F versus displacement x in a preloaded structure.

Preloaded structures are employed especially in the field of the collaborative robots (cobots) to keep positional accuracy high, while at the same time allowing for collision mitigation through compliance after a certain force threshold is reached [3]. The use of preload to increase the rigidity of structures can be found also in several areas of structural engineering, e.g. in the design of large telescopes [4], in space docking systems [5] in variable-stiffness mechanisms [6] and even in pipe joints [7]. Usually, these applications were concerned mainly on single-doF systems, such as active or passive joints, link structures etc. In a previous research, we have produced a comprehensive n-DoF dynamic model [8].

In this paper we show the design of a 4 legs rover equipped with 4 independently steering wheels, as shown in Fig. 2. Each leg is made up of a chain of links connected by a series of preloaded mechanisms similar to those described by Medina et al. [9]. In order to verify the dynamic behaviour of the rover during an impact event, a “quarter model” of the rover has been implemented.

In Section 2, the overall design of the rover is presented. Section 3 is devoted to the n-DoF model of the preloaded structures. Simulation results are presented in Section 4.

2 Planar n-D.o.F. Model

Let us consider a sequence of n serial links, as visible in Fig. 3 a), each of length $l_1, \dots, l_n$, mass $m_1, \dots, m_n$, and rotational inertia $J_1, \dots, J_n$. A preloaded elastic connection is placed between each contiguous link. The elastic connection can be modeled as a device producing a torque $M(\alpha_i)$, where α_i is the relative angle between the i^{th} link and the next. The torque $M_i(\alpha_i)$ follows a trend similar to that

shown in Fig. 1 for $F(x)$; however, since this would require discontinuities (split-field) in the elastic relation, a parametric curve was instead arbitrarily selected to approximate the nominal behaviour, as follows,

Fig. 2 Design of the rover equipped with 4 preloaded structure legs. In a) an overview is illustrated, whereas in b) the main dimensions are shown in mm.

$$M_i(\alpha_i) \cong \left(\frac{M_{0,i}^2}{\pi} \right) \text{atan}(f_i \alpha_i) + k_i \alpha_i, \quad (1)$$

where the parameter $M_{0,i}$ represents the preload torque, k_i the stiffness of joint and f_i is an approximation factor. This type of formulation, being continuous in $\mathbb{C}^1$ (as opposed to a split-field one), helps avoiding numerical noise during simulations.

The independent coordinates, in vector form, are $\mathbf{q} = \{y_l, \vartheta_1, \alpha_1, \dots, \alpha_n\}$, where y_l and ϑ_1 are respectively the vertical position and orientation of the robot chassis. A small-angles approximation is applied to the entire model. The left end-point is constrained horizontally, while it is free to move vertically. This way it is possible to simulate the dynamic behaviour of a single leg (the quarter model of the vehicle). As Fig. 3b shows, the wheel is connected to the 4th link and the mass of the rover quarter is concentrated in $\mathbf{Q}_1$.

Fig. 3 Diagram of n-DoF preloaded structures. In a) a n-DoF free body diagram is shown as implemented in the general model. In b) a 3-DoF model is shown as implemented in the simulation for the rover limb; indeed the location of the body and of the wheel can be seen as well as the modelization for the contact interface.

From the principle of virtual works, it follows that:

$$\delta\Omega + \delta W_{ext} = 0, \quad (2)$$

where the first term represents the inertial forces virtual work, and the second the external forces virtual work. These can be expanded as follows,

$$\delta\Omega = \sum_{i=1}^{n+1} m_i \ddot{y}_i \delta y_i + \sum_{i=1}^{n+1} I_i \ddot{\theta}_i \delta \theta_i, \quad (3)$$

$$\delta W_{ext} = -T_l \delta y_l - M_l \delta \vartheta_1 + T_r \delta y_r + M_r \delta \vartheta_{n+1} + \sum_{i=1}^{n+1} M(\alpha_i) \delta \alpha_i + \sum_{i=1}^{n+1} c_0 \dot{\alpha}_i \delta \alpha_i + \sum_{i=1}^{n+1} m g \delta y_i, \quad (4)$$

In matrix form, Eq. (3) can be written as,

$$\delta\Omega = \delta \mathbf{y}^T \mathbf{M} \ddot{\mathbf{y}} + \delta \boldsymbol{\vartheta}^T \mathbf{J} \ddot{\boldsymbol{\vartheta}}, \quad (5)$$

where $\delta \mathbf{y} = \{\delta y_1, \dots, \delta y_n\}^T$ and $\delta \boldsymbol{\vartheta} = \{\delta \vartheta_1, \dots, \delta \vartheta_n\}^T$ are the vector of virtual displacements, $\mathbf{M}$ is the mass matrix, $\mathbf{J}$ is the matrix of moments of inertia, $\ddot{\mathbf{y}} = \{\ddot{y}_1, \dots, \ddot{y}_{n+1}\}^T$ and $\ddot{\boldsymbol{\vartheta}} = \{\ddot{\vartheta}_1, \dots, \ddot{\vartheta}_{n+1}\}^T$ are the vectors of the vertical accelerations of points $y_1, \dots, y_{n+1}$, and of angles $\vartheta_1, \dots, \vartheta_{n+1}$ respectively. Accelerations along the longitudinal axis x are neglected since small vertical displacements are assumed. In order to reach a formalism based on $\mathbf{q}$, some changes in variables are necessary. Indeed, based on simple geometric considerations, we can write,

$$\begin{pmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \\ y_{n+1} \end{pmatrix} \cong \begin{bmatrix} 1 & l/2 & 0 & \cdots & \cdots & 0 \\ \vdots & l & l/2 & \ddots & & \vdots \\ \vdots & \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \vdots & & \ddots & l/2 & 0 \\ 1 & l & \cdots & \cdots & l & l/2 \end{bmatrix} \begin{pmatrix} y_l \\ \vartheta_1 \\ \vdots \\ \vartheta_n \\ \vartheta_{n+1} \end{pmatrix} = \mathbf{A} \begin{pmatrix} y_l \\ \vartheta_1 \\ \vdots \\ \vartheta_n \\ \vartheta_{n+1} \end{pmatrix}. \quad (6)$$

It is clear that an approximation ($\sin \vartheta_i \cong \vartheta_i$ if ϑ_i is small) is applied to get, from the exact formalism, to the linearized one that appears in matrix $\mathbf{A}$. Similarly, it can be said that,

$$\begin{pmatrix} y_l \\ \vartheta_1 \\ \vdots \\ \vartheta_n \\ \vartheta_{n+1} \end{pmatrix} = \begin{bmatrix} 1 & 0 & \cdots & \cdots & 0 \\ 0 & 1 & \ddots & & \vdots \\ \vdots & \vdots & \ddots & \ddots & \vdots \\ \vdots & \vdots & & 1 & 0 \\ 0 & 1 & \cdots & \cdots & 1 \end{bmatrix} \begin{pmatrix} y_l \\ \vartheta_1 \\ \alpha_1 \\ \vdots \\ \alpha_n \end{pmatrix} = \mathbf{B} \mathbf{q}, \quad (7)$$

It follows immediately that,

$$\mathbf{y}^T = \mathbf{A} \mathbf{B} \mathbf{q}, \quad (8)$$

On a similar note, to write $\mathbf{q}$ in terms of the absolute angles $\boldsymbol{\vartheta}$, the following can be written,

$$\begin{pmatrix} \vartheta_1 \\ \vdots \\ \vdots \\ \vartheta_{n+1} \end{pmatrix} = \begin{bmatrix} 0 & 1 & 0 & \cdots & 0 \\ \vdots & \vdots & \ddots & \ddots & \vdots \\ \vdots & \vdots & & \ddots & 0 \\ 0 & 1 & \cdots & \cdots & 1 \end{bmatrix} \mathbf{q} = \mathbf{C} \mathbf{q}, \quad (9)$$

At this point, Eq. (5) can be written into the following matrix form,

$$\begin{aligned} \delta \Omega &= (\mathbf{A} \mathbf{B} \delta \mathbf{q})^T \mathbf{M} \mathbf{A} \mathbf{B} \ddot{\mathbf{q}} + (\mathbf{C} \delta \mathbf{q})^T \mathbf{J} \mathbf{C} \ddot{\mathbf{q}} = \\ &= \delta \mathbf{q}^T (\mathbf{B}^T \mathbf{A}^T \mathbf{M} \mathbf{A} \mathbf{B} + \mathbf{C}^T \mathbf{J} \mathbf{C}) \ddot{\mathbf{q}} \end{aligned} \quad (10)$$

Regarding the external forces and considering the situation illustrated in Fig. 3, we can write the expression in Eq. (4) as follows,

$$\begin{aligned} \delta W_{ext} = & \{\delta y_l, \delta \vartheta_1, \delta y_{P,r}, \delta \vartheta_{n+1}\} \begin{Bmatrix} -T_l \\ -M_l \\ T_r \\ M_r \end{Bmatrix} + \{\delta \alpha_1, \dots, \delta \alpha_n\} \begin{Bmatrix} M(\alpha_1) \\ \vdots \\ M(\alpha_n) \end{Bmatrix} + \\ & c_o \begin{Bmatrix} \dot{\alpha}_1 \\ \vdots \\ \dot{\alpha}_n \end{Bmatrix} + g\{\delta y_1, \dots, \delta y_n\} \begin{Bmatrix} m_1 \\ \vdots \\ m_n \end{Bmatrix}, \end{aligned} \quad (11)$$

In the above equation, we call $\{m_1, \dots, m_n\}^T = \boldsymbol{\mu}$; in order to find the first vector in the first term on the right, we can write,

$$\begin{Bmatrix} \delta y_l \\ \delta \vartheta_1 \\ \delta y_{P,r} \\ \delta \vartheta_{n+1} \end{Bmatrix} = \begin{bmatrix} 1 & 0 & 0 & \dots & 0 & 0 \\ 0 & 1 & 0 & \dots & 0 & 0 \\ 1 & l & l & \dots & l & l \\ 0 & 1 & 1 & \dots & 1 & 1 \end{bmatrix} \mathbf{B} \delta \mathbf{q} = \mathbf{D} \delta \mathbf{q}, \quad (12)$$

Finally, if $\{\alpha_1, \dots, \alpha_n\}^T = \mathbf{E} \mathbf{q}$, where $\mathbf{E}$ is obvious, $\mathbf{T}_{ext} = \{-T_l, -M_l, T_r, M_r\}^T$, and considering Eq. (8) we can write the following matrix form for Eq. (4),

$$\delta W_{ext} = \delta \mathbf{q}^T (\mathbf{D}^T \mathbf{T}_{ext} + \mathbf{E}^T \bar{\mathbf{M}}(\mathbf{E} \mathbf{q}) + c_o \mathbf{E}^T \mathbf{E} \dot{\mathbf{q}}) + (\mathbf{AB})^T \boldsymbol{\mu} g,$$

where the $\bar{\mathbf{M}}$ operator is defined as $\bar{\mathbf{M}}(\mathbf{r}) = \{M_1(r_1), \dots, M_n(r_n)\}$, with $\mathbf{r} = \{r_1, \dots, r_n\}$ a general vector.

Reassembling Eq. (2) with the expressions in Eq. (10) and (11), it follows that $(\mathbf{B}^T \mathbf{A}^T \mathbf{MAB} + \mathbf{C}^T \mathbf{JC}) \ddot{\mathbf{q}} + c_o \mathbf{E}^T \mathbf{E} \dot{\mathbf{q}} + \mathbf{E}^T \bar{\mathbf{M}}(\mathbf{E} \mathbf{q}) + \mathbf{D}^T \mathbf{T}_{ext} + (\mathbf{AB})^T \boldsymbol{\mu} g = 0$, thus,

$$\mathbf{H} \ddot{\mathbf{q}} + \mathbf{S} \dot{\mathbf{q}} + \mathbf{G}(\mathbf{q}) + \mathbf{D}^T \mathbf{T}_{ext} + (\mathbf{AB})^T \boldsymbol{\mu} g = 0, \quad (13)$$

Where $\mathbf{H}$ and $\mathbf{S}$ are the inertial coefficients matrix and the viscous damping coefficient matrix respectively; the term $\mathbf{G}(\mathbf{q})$ is the internal forces matrix and models the joints elasticity. It is non-linear with respect to $\mathbf{q}$.

Upon impact, considering the wheel stiffness k_w , the vertical force produced on the structure is

$$T_r = \begin{cases} -y_{n+1} k_w & \text{if } y_{n+1} < 0 \\ 0 & \text{if } y_{n+1} \geq 0 \end{cases} \quad (14)$$

The torque exerted by the wheel is null: $M_r = 0$. M_l is the internal force exerted by the rest of the rover on the quarter; since the first link has to remain always

horizontal, such requirement has been fulfilled by introducing a high stiffness k_l and the following boundary condition: $M_l = k_l \theta_1$. Notice that also $T_l = 0$. The interaction between the ground and the wheel is modeled as a spring system of k_{ground} stiffness (see Fig. 3b), where the contact force is $F_c = k_{ground} y_{cmp}$, with y_{cmp} is the ground compenetration measure. In order to produce viable and stable results, the model expressed in Eq. 13 was time-integrated using the classic “RK4” Runge-Kutta method.

3 Simulation of an impact event

During deployment, a rover experiences high loads due to impacts with the ground. For this reason, as can be seen on the left in Fig. 4, we defined a use case with a 0.200 m vertical drop at a gravity level equal to that of earth, which is a conservative approach. Considering that the clearance of the rover is 0.250 m , we elected to limit the deceleration phase to 90% of that value in order to avoid collision between the ground and the belly of the rover. As the plots in Fig. 4 show, the results of the simulation show the first impact at approximately $t = 0.2\text{ s}$, with a rebound take-off starting at $t = 0.56\text{ s}$, a subsequent free-flight phase that ends with a secondary impact at $t = 0.87\text{ s}$.

Fig. 4. Impact simulation. On the left, a summary of the main values is reported. On the right, in the top-most plot the acceleration of the wheel joint P_4 is shown; in the middle, the acceleration can be seen of the body of the rover, corresponding to joint P_0 ; the bottom-most chart shows the evolution in time of the contact force between the ground and the wheel.

The lowest point reached by the rover belly is $y = -0.220\text{ m}$ compared with the standstill value. It is important to note the peak values of the acceleration at point P_0 and P_4 ; indeed, if we recall that the body of the rover is integral to the former, whereas the wheel is connected to the latter, we can appreciate how the rover body experiences lower magnitude accelerations. More specifically, not considering

low-energy peaks (very small duration), the wheel experiences accelerations in excess of 500 m/s^2 , whereas the body sees this value limited to less than 20 m/s^2 , sustained, and approximately 60 m/s^2 peak value. As a comparison, these values are close to only 4 times the static force exerted by gravity on the ground. In the top and middle plots of Fig. 4, during the free-flight phase, a strong oscillation can be seen that is highly irregular in nature; this is due to the bi-elastic behavior of the joints. Results show that this type of mechanism can be used effectively to limit accelerations on the body of the rover, while at the same time acting as a stiff structural component when loads are below a certain threshold.

6 Conclusions

This paper described the design and the dynamic simulation of a rover for space exploration, equipped with 4 preloaded structure legs. The proposed solution guarantees a high stiffness behavior during conventional operations, as well as a compliance behavior when an expected load (collision or motion over an irregular surface) occurs. At the same time, a certain degree of compliance is required to mitigate mechanical stress caused by motion over a rough surface or in case of unexpected collisions. Simulation results show the benefit introduced by the preloaded structures.

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