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# A new stereoscopic "Sum-Trigger-II" for the MAGIC Telescopes 

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To myself and my family because
what you can is what you want!
And to everybody
who believes
in justice...


## Abstract

This thesis describes the work done in collaboration with the $M P I^{1}$ group during three years of Ph.D. at the University of Udine - Department of Physics and INFN Section of Padova, in 2009-11. The candidate is a member of the MAGIC (Major Atmospheric Gamma-ray Imaging Čerenkov) collaboration, which manages two IACT (Imaging Air Čerenkov Telescopes) telescopes for VHE $\gamma$-ray astrophysics.
MAGIC, located at the Observatory of Roque de Los Muchachos in the Canary Island of La Palma, is devoted to the detection of $\gamma$-rays of astrophysical origin in the energy domain above 25 GeV (Very High Energy).

Gamma-ray photons, the most energetic hence smallest wavelength form of electromagnetic radiation, travel incredible distances across the Universe. At such high energies the photon fluxes are extremely low and direct detection would require detector effective areas that are impractically large for current space-based instruments. Fortunately, such high energy photons produce extensive air showers of secondary particles in the atmosphere that can be observed on the ground, both directly by radiation counters and optically via the Čerenkov light emitted by the ultra-relativistic shower particles.
Gamma-ray astrophysics observations are still limited at lower energies by non-gammaray backgrounds, and, at higher energies, by the number of photons that can be detected. Larger area detectors and better background suppression are essential for progress in the field. Low energy threshold and excellent sensitivity are key parameters for a better understanding of $\gamma$-ray messengers in the GeV domain, and allow these telescopes to cover energies in good overlap with satellite experiments, thereby providing essential complementary information. The importance of this range of the electromagnetic spectrum is extremely relevant, because it probably hides the explanation of open and enigmatic questions. The main targets are very distant AGNs (Active Galactic Nuclei), Pulsars and GRBs (Gamma-Ray Burst).

This research is mainly focused on the design, the development, and the realization of a new stereoscopic Sum-Trigger-II for the MAGIC Telescopes, in order to increase the detection efficiency at very low energies $(<50 \mathrm{GeV})$. The Sum-trigger-II is an alternative to the current standard digital trigger, which has an energy threshold of about 50 GeV . This novel trigger concept is based on the analogue sum of signals coming from patches of the camera detector. A small prototype system, the so-called "Sum-Trigger", was already used in a single telescope operation mode, which led to the detection of pulsed $\gamma$-rays from the Crab Pulsar at 25 GeV . Soon, the old prototype analogue Sum-Trigger will be upgraded to a new system filling the whole trigger area in the camera, which will be mounted on both telescopes for stereo observations. The new system will contain new elements: a continuously adjustable analogue delay line, which allows a computer controlled timing flat-fielding of all trigger channels, a passive backplane for the signals distribution to the right patch and a differential high frequency cabling. The system will also have an automatic gain flat-fielding and an absolute trigger threshold calibration.

[^0]
## Outline

This thesis presents the project of a novel stereoscopic Sum-Trigger-II for the MAGIC telescopes. It can be divided in the following two parts:

## Part I: The physics case

In Chapter 1, an introduction to $\gamma$-ray astronomy and astrophysics is presented, starting from the historical point of view and finishing with modern research.
The beginning dates back some centuries before the common era. Chinese, Indians, Mayan, Egyptians, and Babylonians started to record the positions of celestial bodies and the cycles of Nature indispensable for agricultural activities. The first attempt to give a logical explanation to the stars came from the ancient Roman-Greek philosophers. They changed completely the purpose of science, moving it from farming and religion to pure knowledge.
For two millennia man was tied to geocentrism, until heliocentrism was introduced with the Copernican Revolution in the sixteenth century. This is the beginning of the Scientific Revolution, a period that saw a fundamental transformation in scientific ideas across many disciplines. A new scientific method was introduced and the discovery of new technologies, such as the telescope, eased the progress of knowledge.
Between the nineteenth and twentieth century, the development of spectroscopy and the subsequent rise of the new science of astrophysics created new activities for astronomers in the investigation of the physical and chemical nature of stars. Until then, the astronomers were bound by the relatively narrow frequency band of visible light, to which our eyes are sensitive and the Earth's atmosphere is transparent enough. The second part of the twentieth century saw rapid technological advances in astronomical instrumentation. Specific sensors able to detect radiation at different wavelengths were developed and new telescopes began observing the Universe in the infrared, ultraviolet, $X$-ray, and $\gamma$-ray parts of the electromagnetic spectrum, as well as observing cosmic rays.
The discovery of cosmic rays was a crucial moment for the growth of astrophysics, because it opened the access to new methods to study celestial bodies. The development of this new branch contributed also to the detection of $\gamma$-rays, energetic photons that travel through the Universe without being deflected by magnetic fields.
The main very high energy gamma sources studied by experiments as MAGIC are: Supernova Remnants, Pulsar, Binary System, Active Galactic Nuclei and Gamma-Ray Bursts. In addition, these new telescopes can perform studies related to fundamental physics and cosmology.

In Chapter 2, the theory of the extended atmospheric showers, the detection technique of $\overline{\mathrm{VHE}} \gamma$-rays and the subsequent data analysis are presented.
Elementary processes which occur both in our galaxy or in distant extragalactic sources can accelerate or even generate high energy particles. These particles are messengers
of the astrophysical emission phenomena and cross long distances up to the Earth's atmosphere. Gamma-rays, which are not deflected by the magnetic fields during their travel, follow a straight trajectory and indicate the position of the source.
Impinging the Earth's atmosphere, the cosmic particles initiate a cascade of secondary products that develops towards the ground. The spatial and the temporal evolution of the shower depends on the nature and the energy of the primary particle, which triggers different particle processes.
Relativistic charged particles in the shower may polarize the atmospheric medium that then emits Čerenkov photons. Ground-based telescopes collect the faint Čerenkov light, producing a two-dimensional projection of the three-dimensional shower. This technique, called $I A C T$, allows one first to discriminate the background, imposing topological and temporal constraints, and then to reconstruct the event. In fact, the data recorded by the detector are treated by complex algorithms which parametrize the shower morphology in order to extrapolate information about the astrophysical source.

In Chapter 3, a study of the morphology of low energy showers is presented.
The MAGIC telescopes has been designed mainly for physics research at low energies in the GeV domain, with several motivations which range from fundamental physics to cosmology and astrophysics. Unfortunately, this portion of the spectrum lies between the lower limit of the IACT technique and the upper limit of satellite experiments. A good overlap between ground-based and space detectors is crucial to give continuity to research fields that are connected.
The intrinsic limitation of the detection technique and the available technology force one to use innovative methods, novel algorithms and upgraded systems. In this ambitious context, the attention to every detail, both physical and technological, is essential. In order to find the best solutions, the proprieties of the low energy electromagnetic shower, due to a $\gamma$-ray, are explained and the projection's morphology is analysed. Qualitative results and conclusions based on empiric and Monte Carlo studies are reported. Finally, the main features are linked to possible solutions that can improve the efficiency of a Čerenkov telescope.

## Part II: The technological case

In Chapter 4, the MAGIC telescopes, operating at the Canary Island of La Palma, are introduced and the hardware components described, before and after the upgrade of MAGIC-I.
The telescopes are light tubular structures, which sustain a parabolic reflective surface, utilized to collect the Čerenkov photons emitted by the extended air showers. They can be orientated in azimuth and elevation to track a source in the sky with high angular resolution.
The Čerenkov light is focused on photosensors, which convert the optical signals into electrical ones. The pulses are then amplified and processed by a multi-level trigger system which performs a selection on which events should be recorded. In parallel, there is the data acquisition branch which registers the interesting signals every time it is activated by the trigger. All the subsystems are controlled by an central control. Currently, the telescopes are being upgraded. A new readout and an improved trigger system are being commissioned. In the summer of next year, the camera of the older telescope will be renewed and a novel stereoscopic analogue trigger will be added in the electronic chain.

Chapter 5 is dedicated to the presentation of the novel stereoscopic analogue trigger. In 2007, an innovative prototype trigger system, called Sum-Trigger was installed in the MAGIC electronic chain. The new concept is based on the analogue sum of adjacent pixels, which exceeds a fixed threshold when they are lit-up by an extended air shower. The success of this idea reached the apex with the publication on Science of the Crab Pulsar discovery at 25 GeV . Unfortunately, the trigger area was limited to a thin central ring of the camera and the stability, the maintenance and the equalization of the system were extremely difficult.
A new professional version, dubbed Sum-Trigger-II, is under construction. The basic concept is the same, but the system layout, the electronics controls, compactness and robustness are significantly improved. Monte Carlo simulations of the complete system predict very interesting achievements in the domain under 50 GeV .
Every subsystem that composes the Sum-Trigger-II is illustrated in detail and the current performance is presented.

In Chapter 6, the concept and the hardware of the stereoscopic trigger is described. Since 2009, MAGIC is endowed with a second telescope which allows data-taking in the stereo mode. The stereoscopy gives the possibility to register the same event from two different points of view, improving the detection quality and the image reconstruction in the analysis framework. In a $I A C T$ array, the telescope layout determines the features and the performance of the experiment. MAGIC has built the second telescope 85 m far from the first one, ensuring a large common effective area, which consequently keeps a low energy threshold.
The telescopes operate synchronously when tracking the same source. A common trigger system (stereo trigger) alerts the data acquisition, when the same atmospheric shower hits both detectors generating local triggers. Obviously, the different light paths and the relative delays introduced by the electronics chains are taken into account and corrected in the selection logic.
The stereo trigger, which will also manage the outputs of the new analogue Sum-Trigger$I I$, will be upgraded with a new multi-purpose board, dubbed MiniPulsar. The main design and the performance of the first prototype are described in detail at the end of the chapter.

The last Chapter outlines the conclusions and the future perspectives of this work.

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## I

## Introduction: $\gamma$-ray astrophysics


#### Abstract

STROPHYSICS ${ }^{a}$ deals with the physical properties of celestial objects that A populate the Universe. This field of study is in strong progress and it is catching the attention of many physicists, because it is a very broad subject, full of unsolved questions. We can consider it a composite of many disciplines, as for instance electromagnetism, thermodynamics, relativity, cosmology and even fundamental physics. Astrophysics represents the encounter between two very ancient branches of science: astronomy and physics. A historical overview and a description of the main aspects of this subject, which will be the starting point of this introduction, should provide a simple and logical explanation of the current research activity in astrophysical environments. This chapter is focused mainly on three topics: 1) history of astrophysics; 2) cosmic-rays; 3) current status of gamma astrophysics.


${ }^{a}$ In Greek means: nature of stars.

### 1.1 History of astrophysics

The Universe observation is one of the most ancient man's curiosity, originating in the elementary needs of mankind. The astronomers were instrumental in establishing the measurement of time, because people needed to know exactly when to plant and harvest. They followed the cycles of the seasons and lived close to the natural rhythms of the planet. The possibilities of antique science stopped at fixing the apparent positions of the objects on the sphere and collecting the visible properties. Any attempt to rationalize the observed facts was a failure, until Greeks laboriously built up a speculative system.
In the beginning the astrometry, which deals with the position and the motion of the heavenly bodies, was the only astronomy ${ }^{1}$ branch developed. We have to wait many centuries to see the coming of a new discipline, called astrophysics, which treats the investigation of their chemical and physical nature. At the current time, astrophysics may be said to have absorbed the old descriptive astronomy, while the astrometry is based on the theory of gravitation, where mathematics keeps a central role.

[^1]
### 1.1.1 Prehistoric astronomy

The first astronomical knowledge was early established by the Chinese, Indians, Mayan, Egyptians, and Babylonians.
The Chinese were meticulous in keeping astronomical records, particularly the appearance of comets, novae and other transients. An impressive Chinese record in July 1054 is a guest star, that was bright enough to be seen during the daytime for nearly a month in the constellation, that we call Taurus. We believe this to be the supernova explosion that gave rise to the Crab Nebula, and our knowledge of the date of the explosion itself is a very important key in understanding the death of massive stars.
They used the circumpolar stars ${ }^{2}$ as their reference point for the heavens, unlike the Indo-Europeans, who used observations based upon the rising and setting of celestial bodies on the ecliptic and the horizon. In order to mark the passage of time and the seasons, the Chinese primarily used the orientation of the Big Dipper ${ }^{3}$ constellation relative to the pole star in early evening. The Chinese astronomers generated fantastically accurate measurements of time and charted unusual cosmological phenomena, and their ideas filtered down the Silk Road into the Middle East and Europe.

Indian astronomy was heavily tied to their religious and spiritual outlook of the world, but it contained many accurate observations of phenomena and some original elements, which were a catalyst for the growth of mathematics. It was mainly based upon the stars and the sidereal period, namely the time that takes an object to make one full orbit around the Sun. They used the stars and the planets to create astrological charts and read omens, devising sophisticated mathematical models and developing many interesting theories, many of which passed into the Islamic world and Europe.
In addition, Indian astronomers also proposed that the stars were exactly like the Sun, but much further away. They also understood that the Earth was spherical and attempted to calculate the circumference of the planet.


Figure 1.1: One of the most important Mayan calendar: the Haab'.

The observations of the Mayan priestastronomers were entirely dedicated to astrology. Their incredibly accurate astronomical calculations and sophisticated mathematics were steeped in religion and omens.
It is not surprising that the Mayans observed the stars to chart the seasons and developed a calendar. The two main calendars were the Tzolk' in, a 260 -day calendar of 13 numbers and 20 day names, and the Haab' (Fig. 1.1), of 365 days. This calendar had 18 months of 20 days, with a 5 -day month added at the end of the year. The reason why they used 20 days for a month is largely based upon their numeric system, which is a base twenty. The Mayans did not have complex instruments to estimate the positions of celestial objects, but they built some great temples,

[^2]which were aligned to the Sun, especially midsummer, midwinter and the equinoxes. They further refined their astronomical techniques, recording the positions of the planets, devising tables for long-term predictions of the movements of these planets, and creating tables to predict eclipses. Their predictions were so sophisticated that they included corrections, showing that they fully understood that the movement of the planets and precession were complex.

In Egypt, considerable technical skill was attained and a constellation system came in use [24]. For instance, the precise orientation of the pyramids, aligned towards the pole star, is a piece of evidence. Moreover, the evaluation of the site of the temple of Amun-Re at Karnak, taking into account the change over time of the obliquity of the ecliptic ${ }^{4}$, has shown that the Great Temple was aligned on the rising of the midwinter Sun.


Figure 1.2: Circular megalith at Nabta. (Courtesy of Raymbetz)

Also the Egyptian calendar was always in close connection with the stars' evolution and it was the base of agriculture and predicting the seasons. The main example are the stone circles at Nabta Playa (Fig. 1.2), which show that they were accomplished at marking time and calculating the coming of the Nile's floods. The Egyptians were fully aware that the year was about 365 days plus the extra quarter day and they prepared a calendar based around the star Sirius, which arises highly on the sky in conjunction with the Nile's floods. The days were divided into 24 hours, using sundials to tell the time. For the night, 36 groups of stars, called Decans were considered. The most amazing example is the star map, also called star clock, on the ceiling of the King Ramesses VI's tomb. This map may be used to map the journey of the stars for each hour of the night, through the whole year.
Whilst Egyptian civilization declined, it became absorbed by the Greek and Roman cultures and many aspects are still modern and in use.

The Babylonian astronomy was deeply influenced by Sumerians, which introduced the astrolatry ${ }^{5}$ and the sexagesimal (base 60) place-value number system. This is a simplified method of recording very great and very small numbers and it is still the base of the modern practice of dividing a circle into 360 degrees, of 60 minutes each. By merging this new mathematical instrument and the skill to observe and study the sky, they have identified the ecliptic way of the Sun, which was divided in 360 parts, each one for one single day of the year. They have also identified, for the first time, the inner planet Mercury and the outer planets Mars, Jupiter and Saturn.
During the 8th and 7th centuries BCE, Babylonian astronomers developed a new empirical approach to astronomy. They began studying philosophy dealing with the ideal nature of the Universe and began employing an internal logic within their predictive planetary systems. In the 3rd century BCE, searching in the past reports for repeating occurrences of ominous phenomena for each planet, they created mathematical mod-

[^3]els that allowed them to predict these phenomena directly. This was an important contribution to the astronomy and the philosophy of science, and some scholars have thus referred to this new approach as the first scientific revolution. This new approach to astronomy was adopted and further developed in Greek and Hellenistic astronomy, where the dependency upon Cosmology starts.
More importantly, this period saw the transmission of ideas between the Indians, Babylonians, Greeks, and Persians. This exchange of theories and philosophy was extremely important to the development of astronomy.

### 1.1.2 Greek and Roman astronomy

The main fortune of Greeks was the strategic geographical position. They lay at the crossroads of many trade routes and were influenced by many other great cultures. The ancient Greek philosophers took in the knowledge of other populations and refined astronomy with an innovative approach. They moved from an observational science into a full-blown theoretical science. The Greeks kept the idea of Gods, but they were not satisfied with purely theological explanations for phenomena and began to model the structure of the Universe. This was the first real attempt to find a grand universal theory and to explain the origin of Universe, which is a machine that runs upon mechanical and mathematical principles, that could be deduced through logic and reasoning.

There are several important Greek astronomers, such as Thales ( $624-546$ BCE), who recognized the importance of the star constellation Ursa Minor for the navigation, and Anaximander ( $610-546 \mathrm{BCE}$ ), who was the first to create a cosmological model. His major contribution was to imagine the Earth as hanging in space, with the other heavenly bodies describing circles around it. Anaximander believed that the Earth was cylindrical in shape and surrounded by air and then fire (Fig. 1.3). The inhabited portion lay on top of the cylinder, surrounded by an ocean. Another great contribution was the idea of infinity and the tantalizing possibility that the Universe could be unbounded.
Another one was Pythagoras (570-495 BCE), who postulated that the Earth was spher-


Figure 1.3: Left: the Anaximander's Universe model, in which the celestial bodies move around the Earth in circle. (Image credit: © Centre for Astrophysics and Supercomputing, Swinburne University of Technology)
Right: the Anaximander's Earth model, which consists in a cylinder surrounded by air and fire.
ical, a huge departure from Anaximander's model. Famously, he proposed this idea because he noticed that ships disappear below the horizon when they sail away, implying that the surface of the Earth is curved.
The milestone was put by Plato (427-347 BCE) and his pupil Aristotle (384-322

BCE). They believed that the entire cosmos was constructed with precision and that circles and spheres, as the most perfect objects, were the key to understand the Universe. In their models, the stars, Sun, and Moon were fixed to concentric crystalline spheres, rotating inside one another. The stars formed the outermost crystal sphere, followed by the planets, the Sun, the Moon, and the spherical Earth at the centre. Unfortunately, this image of the sky does not explain completely the motion of the Universe objects, both size and brightness variability and the different seasons' length. The problem was ostensibly solved by $A p$ pollonius of Perga (250-220 BCE) and his solution was applied by Hipparchus (190$120 \mathrm{BCE})$ to describe the movements of the Sun and Moon. He believed that the Earth did not lie at the very centre of the Universe, but lay slightly off-centre. Ptolemy ( $90-168$ CE) took further this idea and expanded it to all the planets, proposing the famous theory of epicycles ${ }^{6}$ (Fig. 1.4). Using trigonometry, Hipparchus and Ptolemy devised a model, where the Sun, Moon, and planets moved around the Earth in circles, but rotated in smaller circles within this cycle. This perfectly explained the sometimes retrograde motion of the Moon and planets, and elucidated why the Sun and Moon were sometimes closer to the Earth and, subsequently, larger [126].


Figure 1.4: The Ptolemy's geocentric model. (Image credit: Lola Judith Chaisson - Astronomy today, by E. Chaisson \& S. McMillan) Ptolemy was the apex of an important cycle in the history of astronomy. In this period the Romans conquered Egypt, which again became the centre of scientific activity. Obviously this is the end of an amazing cultural interchange, where the native Egyptian tradition of astronomy had merged with Greek astronomy as well as Babylonian astronomy.

The ancient Roman-Greek philosophers were both a blessing and a curse of science. On the one hand, they moved the idea of the structure of the Universe away from Gods and superstition, using geometry to create harmonic models which described the underlying motions of the Universe. On the other hand, the geocentric model and the epicycles of the ancient Greek astronomers persisted for long time, influencing later theoretical cosmologists to take the wrong path. In fact, the Ptolemaic astronomy became standard in medieval Western European and Islamic astronomy, until it was displaced by the heliocentric and Tychonic systems in the 16th century.

### 1.1.3 Sixteenth century

After the significant contributions of Greek sages, the astronomy entered into a relatively static period. For many centuries, the main astronomy's core was strongly tied to the old Roman-Greek philosophy. Many concepts remained immutable and they settled into the common social and religious life. There was no space for new original thoughts, because they were not considered innovative, but often something completely wrong, nasty and dangerous. In addition, the advanced astronomical treatises of classi-

[^4]cal antiquity were written in Greek, and with the decline of knowledge of that language, only simplified summaries and practical texts were available for the study. This very long trend was disrupted by two daring astronomers, who met much resistance, not only from the Catholic Church and its reluctance to accept a theory not placing God's creation at the centre of the Universe, but also from those who saw geocentrism as a fact that could not be subverted by a new, weakly justified theory. These two are Nicolaus Copernicus and Tycho Brahe.

In $1543^{7}$, Copernicus upset the historic geocentric model introducing the heliocentrism, where the Earth and planets revolved around a stationary Sun at the centre of the Solar System [45]. Now it is easier to explain the planets motion and there is no need to recourse to the sophisticated epicycles. Copernicus moved heliocentrism from philosophical speculation to predictive geometrical astronomy, elaborating the system in full geometrical detail and using selected astronomical observations to derive important numbers. His work was a consequence of a yearning for a greater mathematical harmony, without violating the principle of uniform circular motion ${ }^{8}$ proposed by the Greek predecessors.
His theory stimulated further scientific investigations, becoming a landmark in the history of science that is often referred to as the Copernican Revolution.

The Tycho Brahe's thinking was more conservative than Copernicus's one. He combined the geometrical benefits of the Copernican system with some philosophical concepts of the Ptolemaic system. He proposed a geo-heliocentric model, in which the Sun, the Moon and the stars revolve around the Earth, and the other five planets orbited the Sun. The central topics of Thyconic theory were an unmoving Earth for reasons of physics, astronomical observations and religion.
Brahe was one of the greatest observer of the sky. He succeeded to measure, with a precision never reached, the ecliptic inclination, the eccentricity of Earth's orbit, the inclination of the lunar orbit and the retrograde lunar nodes ${ }^{9}$. Finally he drew up the first modern stars catalogue with more than 1000 star positions.

### 1.1.4 Recent astronomy

During the last four centuries and especially the twentieth one, the understanding of the cosmos is extraordinarily progressed thanks to the development of new instruments and methods. From then on, the dichotomy between science and technology became very strong, progressing more often in parallel. The beginning is 1609, when Galileo Galilei started to observe the stars using a small optical telescope ${ }^{10}$ (Fig. 1.5). In the sea of these striking discoveries, there are the Jupiter's satellites, the phases of Venus, the mountains of the Moon, the spots on the Sun, Saturn's unique "appendages" and the perception of the stellar composition of the Milky Way [62].
However this was the century of theory, where many aspects of Nature were thus laid down with marvellous intuition; one above all, the geometrical plan of movement in the

[^5]

Figure 1.5: The first telescope built by Galileo Galilei (1609). The main tube is composed of wood lathes, covered by red-brown skin and gold friezes. The convex lens diameter is 37 mm and its focal length is 980 mm , while the eyepiece diameter is 22 mm with a focal length of $-47,5 \mathrm{~mm}$ (a negative focal length means it is divergent). The telescope can magnify the objects by a factor of 21 times with a field of view of $15^{\prime}$. (Courtesy of Museo Galileo Firenze - photo Franca Principe)

Solar System. Johannes Kepler was the first to attempt to derive mathematical predictions of celestial motions from assumed physical causes. In 1609, he elaborated the first two of the "Three Laws" of planetary motion [81] and the third in 1619 [82]. The first rule eliminates the circular motion, which had been fashionable for two millennia. The second replaces the idea that planets move at uniform speed around their orbits, with the empirical observation that the planets move more rapidly when they are close to the Sun and more slowly when they are farther away. The third rule is a harbinger of the law of gravitation, which would be developed by Newton.
Subsequently Isaac Newton discovered the Universal Gravitational Law (1687), showing that the same uniformly acting force regulates celestial revolutions and compels heavy bodies to fall towards the Earth's surface. Every particle of matter attracts every other with a force directly proportional to their masses, and inversely proportional to the squares of their distances apart. This was a further bond between physics and astronomy. He also found out the three laws of motion [103], which dominated the scientific view of the physical Universe for the next three centuries. Finally, Newton demonstrated the consistency between Kepler's laws and his gravitation theory verifying the discordance between the Sun and the centre of gravity of the Solar System, thus removing the last doubts about heliocentrism and advancing the Scientific Revolution. This period rose a deep transformation in scientific ideas across physics, astronomy, and many other disciplines, which heavily influenced modern sciences. The core of this new kind of thinking is the concept of a systematic, mathematical interpretation of experiments and empirical facts: the scientific method. The way in which scientists worked was radically changed.

By comparing modern with antique observations, in 1718 Edmund Halley (16561742) understood the stars' movement, which is far from being fixed, each star having its own path across the sky. The stellar motions became a wide and expansive field of research and a preliminary attempt to regularize them was made by Herschel's determination.
In fact, the extraordinary improvement of reflecting telescopes (Fig. 1.6) by means of Sir William Herschel (1738-1822) opened a fresh epoch of discoveries, mainly in the Solar System environment. He got a high notoriety for the discovery of Uranus and two of its major moons, Titania and Oberon, but probably his most important contribution came
from the search for visually very close pairs of stars. In that period, the astronomers tried to explain the proper motion of stars looking at the changes over time in their apparent separation due to parallax shift. He announced the hypothesis that the two stars might be a binary system, orbiting under mutual gravitational attraction [70].
The following step was pursued by Friederich Bessel, Wilhelm Struve and Thomas Henderson in 1838. Continuing to use the parallax method ${ }^{11}$, they measured the star distances. The first stars accurately measured by them were 61 Cygni, Vega and Alpha Centauri.


Figure 1.6: Model of telescope, exhibited in the William Herschel museum in Bath, which he discovered Uranus with. The power and magnification of his telescope was the secret of his success. It is 7 foot long and 6 inch diameter. Both mirrors, the main at the bottom of the tube and the secondary mirror near the top, were made of speculum metal.

The missing element to form the recent astrophysics is given by William Huggins in 1864. After reading the Kirchhoff and Bunsen's report about the identification of chemical elements (spectrum analysis) by means of spectrograph ${ }^{12}$, he decided to take advantage of this new technology and started to extract the composition of celestial objects [75]. In fact, he was the first to take the spectrum of a planetary nebula analysing $N G C 6543$ and he identified the gaseous nature (mainly hydrogen) of many other diffuse and planetary nebulae [76]. In such a way, he began the study of novae physical mechanisms.
The investigation about the elementary constituents of the Universe became fundamental. This was the original stepping stone towards the traditional aspect of astrophysics, where the main interest was focused on the physical properties, such as density, temperature, chemical and nuclear composition of matter, luminosity and emitted spectrum of stars, galaxies, interstellar and intergalactic medium and everything that populates the Universe.

Another pioneer of stellar spectroscopy was Pietro Angelo Secchi, who was the first to adopt spectroscopy for the stellar classification. Using a visual spectroscope on the Roman College Observatory's telescope, he completed a study of the spectra of about 4000 stars $[117,118,119]$. His scheme, subdivided in four spectral types, paved the way to future classifications, such as the Harvard classification system compiled at the Harvard College Observatory in the 1880s. This system was based on the Henry Draper Catalogue, which was a listing of the positions, magnitudes, and spectral types of stars in all parts of the sky. The first version ${ }^{13}$ of the catalogue contained 10351 stars, designated by letter in alphabetic sequence according to the strength of their hydrogen spectral lines. At the beginning of the twentieth century and in the same observatory, Henrietta Swan Leavitt began to measure the brightness of many stars, noting that in the Magellanic Clouds several of them were variable and showed a pattern. In 1912, she confirmed

[^6]that the brighter variable stars (Cepheid variables) had longer periods [89]. This relation between the luminosity and the stars' period is known as the period-luminosity relationship and it opened the possibility of measuring distances in the Universe.
The Leavitt's method was well calibrated by Harlow Shapley some years later. By determining the distances of many globular clusters, for the first time he estimated the size of the Milky Way, which was much larger than previously believed [120]. He also concluded that the position of the Sun lay in the periphery of our own galaxy, far away from its centre. The belief of a small Universe was abandoned and its geometry was transformed from heliocentric to off-centre, dwindling the anthropocentric world view.

In the same period, around 1910, Ejnar Hertzsprung and Henry Norris Russell independently developed a procedure to classify the stars with the same spectrum, according to some features as the luminosity, temperature and mass. The final result for the stellar luminosity was the $H$ - $R$ diagram (Fig. 1.7). Nevertheless, the diagram clarified the stars' topology and some peculiar behaviour, but nothing related to their evolutionary mechanism and their internal engine. To know about that, we have to wait the marvellous insights of Arthur Eddington.


Figure 1.7: The $H-R$ diagram is a graph of stars showing the relationship between the stars' absolute magnitudes or luminosities versus their spectral types or classifications and effective temperatures. (Courtesy of $E S O$ )

Arthur Eddington studied the internal star equilibrium, he tried to discern all the forces at stake and developed the first true understanding of stellar processes [51]. His model was correctly based on the balance between the gravitational and radiant force, where any variation could change the main mechanism. The model treated a star as a sphere of gas held up against gravity by internal thermal pressure, and one of his chief additions was to show that radiation pressure was necessary to prevent collapse of the sphere. Moreover, he grasped the sub-nuclear origin of the immense generated stellar energy, overturning current thinking. He said that the energy was produced by some nuclear reactions which broke the nuclei of elements, located in the star's core. In 1920, Eddington considered the hydrogen as the most important fuel of these reactions, triggered by very high pressure and temperature. This is a typical exothermic ${ }^{14}$ process, called nuclear fusion, which can self-feed.
This marvellous intuition was completed twenty years later by Hans Bethe, who proposed the proton-proton chain and carbon-nitrogen-oxygen cycle as the two main fusion

[^7]reactions, by which stars convert hydrogen to helium [11].
At the same time, Eddington was one of the first to receive several papers regarding Einstein's theory of general relativity. Thanks to his mathematical skills, he understood the general relativity and in 1919 he organized two expeditions to observe a solar eclipse to make the first empirical test of Einstein's theory: the measurement of the deflection of light by the Sun's gravitational field.

The relativity theory was concluded by Albert Einstein in 1916, but this was a very long and complex work, started more than ten years before. It was in the year 1905, when Einstein published the special theory of relativity [52], changing radically the basis of classic physics, finding a brilliant solution on how to reconcile the laws of classical mechanics with the laws of the electromagnetic field.
The peak of that study was just the general relativity theory [53], according to which the gravity of a body can modify the properties of the space, introducing the curvature of the space-time. Hence, he applied this theory to model the structure of the Universe as a whole. This new physics provides the foundation for several current understandings, as the black holes, regions of space where gravitational attraction is so strong that not even light can escape.

One of the most attracted contemporary by Einstein's theory, was the German Karl Schwarzschild. He was the first to provide the exact solution to the Einstein field equations of general relativity, for the limited case of a single spherical non-rotating mass. The choice of the right approximations and the use of an elegant polar-like spherical coordinate system, secured that admirable result, appreciated directly by Einstein himself. That solution contains a coordinate singularity, which lies on the sphere of points at a particular radius, called the Schwarzschild radius ${ }^{15}$. If the radius of the central body is less than the Schwarzschild radius, all the massive bodies and even photons, located inside this region, must inevitably fall into the central body. When the mass density of this central body exceeds a particular limit, it triggers a gravitational collapse and produces a black hole.

In the first quarter of the twentieth century the knowledge of the Universe's structure notably increased, but its size was still unclear. This topic originated an important debate between the astronomers H. Shapley and H. Curtis, called the Great Debate [121]. Shapley argued that the Milky Way was the entirety of the Universe, containing all the spiral nebulae, such as Andromeda. On the other side, Curtis asserted that such nebulae were separate galaxies, thereby extragalactic objects. The debate was resolved only using larger telescopes. Fundamental was the Edwin Hubble's work, in which he measured the great distance (greater than the Milky Way size calculated by Shapley) of some Cepheid variable stars located in spiral nebulae, confirming that spiral nebulae are independent galaxies.
Stimulated by the innovative De Sitter's theory, in 1929 Hubble added another amazing feature of the Universe: the expansion. Observing the light spectra from galaxies beyond the Milky Way, he discovered a shift of light to red. This effect was a clear demonstration that the galaxies were drifted away. Hubble quoted in a plot the galaxies' speed and the distance, carried out the linear trend, namely increasing the galaxies distance their speed also increased (Hubble's law ${ }^{16}$ ) [74].
Assuming a homogeneous, isotropic and expanding Universe, the law was theoretically derived from general relativity equations and afterwards Hubble confirmed it empiri-

[^8]cally. Already back in 1922, Alexander Friedmann had published a set of a possible mathematical solutions to the field equations that argued for an expanding Universe. In 1927, also the astrophysicist Georges Lemaitre had published a model of an expanding Universe, but their works were accepted only few years later [90].
An expanding Universe means that long ago it must have been far denser. In 1931 Lemaitre proposed that the Universe might have been originated by a primeval cosmic explosion, later on dubbed Big Bang ${ }^{17}$ [91]. This hypothesis was challenged by a new theory, in which the Universe might be in a steady state. In this cosmological model, proposed by F. Hoyle, H. Bondi and T. Gold, new matter is continuously created as the Universe expands without changing its appearance over time. New stars and galaxies are formed at the same rate that old ones become unobservable as a consequence of the expansion [19].
The Steady-State theory started to be in decline in the late 1960s, when observations demonstrated that the Universe was evolving. From then on, the Big Bang is implicitly accepted in most astrophysical publications.

Another important scientist was Walter Baade. Between the two World Wars, he extensively studied the Crab Nebula and advanced the idea that Supernovae could produce cosmic rays and neutron stars. Moreover, he discovered two kinds of Cepheid variable stars, observing the central region of the Andromeda galaxy [6]. Considering this new population of stars, the period-luminosity relationship was corrected and the scale of the Universe became double [7].

As consequence of these new well-grounded theories and the advent of accelerators, scientists realized that the important cosmological features could be explained as natural and inevitable effect of elementary particle physics. Moreover, all of this pushed to another great change in the backgrounds of astronomers and their activities followed from observations beyond visual light.
In 1931, the American radio engineer Karl Jansky detected a radio emission from the centre of Milky Way [77] and opened the way for radio astronomy. Also X-ray astronomy took off after the war, thanks to physicists with expertise in designing and building instruments to detect high-energy particles. Finally $\gamma$-rays, infrared and ultraviolet light provided further means of non-optical discoveries in the space age. Currently, some particle physicists are turning to cosmology extrapolating information regarding the behaviour of matter under extreme conditions, beyond the limits of particle accelerators.

### 1.1.5 Modern astrophysics

The junction between astronomy and physics was provided by Newton, which derived the gravitation from the laws of Kepler. From then on, this bond became always more strong and after the novel concepts promoted by illustrious scientists in the nineteenth and twentieth centuries, as Einstein, Maxwell, Stokes, Boltzmann and many others, it matured into something indissoluble and inseparable. This is the birth of modern astrophysics, a branch of astronomy that studies the physical properties of celestial objects. Because it is a very broad field, astrophysicists typically apply many scientific disciplines, including relativistic, quantum and statistical mechanics, electromagnetism, thermodynamics, relativity, nuclear and sub nuclear physics. In practice, modern astronomical research involves a substantial amount of physics. Astrophysics can be divided in three different sections: 1) the theoretical astrophysics that prepares models and simulations to describe the phenomena in the Universe; 2) the observational

[^9]astrophysics that records the radiation coming from space; 3) the fundamental space physics that uses cosmos like a laboratory to investigate particular particle properties and exotic physics, inaccessible in the common accelerators.

Theorists endeavour to create mathematical models and figure out the observational consequences of those models. They combine computational expertise with complex mathematics and detailed physics to solve surprising astrophysical problems and predict natural processes. It's then a matter of experimental observers to look for data that can refute a model or help in choosing between several alternate or conflicting proposals. In fact the advancement of science depends on the interplay between experimental research and theory. Some current classical subjects of theoretical astrophysics are stellar evolution and stellar endpoints, galaxy formation, magnetohydrodynamics ${ }^{18}$, origin of cosmic rays ${ }^{19}$ and physical cosmology ${ }^{20}$.

The astrophysical observations are established on the reception from space of electromagnetic radiation, charged cosmic rays and neutrinos. The electromagnetic radiation sweeps over a large range of wavelengths (Fig. 1.8), which need specific techniques and detectors, as explained in the following list:

- The radio astronomy treats the radiation with a wavelength greater than some millimetres. There are two kinds of source emitting in this range of the spectrum: a) very cold ( $<1000 \mathrm{~K}$ ) objects as interstellar gas and molecular clouds; b) relativistic electrons in a weak magnetic field. Furthermore, there are some non thermal sources, which emit at these frequencies. The most important are pulsars and AGNs (Active Galactic Nuclei). At the wavelength of about one millimetre there is another relevant and appealing emission, the cosmic microwave background radiation ${ }^{21}(C M B R)$. The study of these waves requires very large radio telescopes, to increase the signal-to-noise ratio and the angular resolution. The technological solutions lead to interferometric arrays like Very Large Array ( $V L A$ ) or huge single structure like the RATAN-600, which consists of a 576 m diameter circle of rectangular radio reflectors.
- The infrared astronomy studies the radiation with a wavelength between millimetre fraction and 780 nm , close to the visible limit. Here, cold stars and non thermal $A G N s$ are detectable. In addition, the interstellar dust emits in this range. Infrared observations are usually made with telescopes similar to the familiar optical telescopes, but new discoveries have been obtained by infrared satellite missions, where the most representative was IRAS (Infrared Astronomical Satellite). It has detected about 350000 infrared sources, increasing the number of catalogued astronomical sources by about $70 \%$.
- The optical astronomy is the oldest and the only one in use until last century, because originally the astronomers could exclusively use the nuked eyes. In any case, this is not the real justification of the current success of this branch. The reasons are first the high atmosphere transparency in the visible domain, second the emission wavelength of most of the objects that populate the Universe and third the application of that radiation range to verify some physical and chemical properties as temperature, luminosity and matter composition. The main observed

[^10]sources are stars, galaxies and nebulae. Currently, both optical telescopes and satellites are available for this research field. Gran Telescopio Canarias (GTC) is the world's largest single-aperture optical telescope.

- The ultraviolet astronomy deals with the radiation between 300 and 10 nm . Many emissions occur in this interval and they are a signature of hotter objects, typically in the early and late stages of their evolution. Unfortunately ultraviolet emissions are strongly absorbed in the interstellar space or by ozone in the atmosphere. This means that the observations at these wavelengths must be performed from the upper atmosphere or from space. For example, the Hubble Space Telescope and FUSE have been the most recent major space telescopes to view the near and far UV spectrum of the sky.
- The X-astronomy works from a wavelength of 0.01 to 10 nm , corresponding to the energies in the range 120 eV to 120 keV . Typically, $X$-rays from about 0.12 to 12 keV are classified as "soft" $X$-rays, while from about 12 to 120 keV "hard" $X$-rays, due to their penetrating abilities. The $X$-ray emission is coming from sources that contain an extremely hot gas at temperatures of many million degrees kelvin. Often the material is heated by the fall in the strong gravitational field, produced for instance by a nearby black hole. The first $X$-ray source dates back to 1962 , when Sco $X$ - 1 was discovered by a rocket designed by Riccardo Giacconi. Unfortunately $X$-rays are absorbed by the Earth's atmosphere, so the detectors must be taken to high altitude by balloons, sounding rockets ${ }^{22}$ or satellites as BeppoSAX.
- The gamma astronomy handles the most energetic radiation, above 120 keV . At this high frequencies, the main sources are extreme and non thermal and can generate almost inconceivable amounts of energy. Pulsars, AGNs, Supernovae remnants, Gamma-Ray Bursts and Micro-quasars are the most detectable. In the first part of the gamma spectrum, space observatories as FERMI (Gammaray Space Telescope) are preferred, because the particles energy is too low to flow through the atmosphere. In the second part, the flux of high energy photons falls dramatically and the poor statistic imposes very large sensitive surface, which can be only built on ground. As shown in figure 1.8, the opacity of the atmosphere should prevent usual direct detection on the Earth's surface, however the interaction of $\gamma$-rays with atomic nuclei provides an alternative method. MAGIC (Major Atmospheric Gamma-ray Imaging Čerenkov Telescope) is an example of ground-based gamma telescope that uses this innovative approach.

Besides the photons, the Earth is hit by different showers of charged particles, called cosmic rays. These are basically protons, electrons and heavy nuclei that are deflected by magnetic fields, so they don't arrive directly from the origin along straight lines. It is impossible to determine the provenance of cosmic rays and the relation between detected particles and sources' properties. Nevertheless, these particles play often a central role in the generation of electromagnetic radiation very close to the source. The photons travel straightforward and can be recorded to study that process and the matter emitting not thermally.

The last kind of particles that are revealed on ground are neutrinos. They are not deflected by magnetic field being neutral and can be linked to the place of creation.

[^11]

Figure 1.8: A sketch of the electromagnetic radiation absorption passing across the Earth's atmosphere. (From NASA website: http://missionscience.nasa.gov/ems/01_intro.html)

The problem here is the weak interactive power of neutrino. It is able to pass through ordinary matter almost unaffected, increasing extremely the difficulty to detect it. On the other side, this is a nice peculiarity of neutrino, because it is not significantly attenuated by its travel through the interstellar medium and it can probe very far astrophysical sources. Right now only two neutrino sources have been detected for certain: the Sun and the supernova 1987 A by the water-based detectors Kamiokande II.

Fundamental physics in space can provide the knowledge needed to address outstanding questions at the intersection of physics and astronomy. With laboratory energies necessarily limited, the Universe provides a fantastic range of extraterrestrial particle accelerators. The aim is to study signals from remote and energetic astrophysical objects to find out plausible answers to some unsolved important questions related to fundamental laws of Nature. The main items are driven by the necessity to find an evidence of a unified theory and investigate matter under exceptional conditions. Exploring the extreme Universe, scientists hope to probe the deepest laws of gravity and nuclear physics. These are exciting and potentially important topics that challenge astrophysicists for an explanation.
Important fields of research are the relativistic gravity and physics beyond the Standard Model ${ }^{23}$. An example is the LISA (Laser Interferometer Space Antenna) project, a system of three identical spacecrafts arranged in an equilateral triangle formation and separated by about 5 million km . Its objective is to measure gravitational waves expected from massive black holes, and galactic binaries.

### 1.2 Cosmic rays

As explained in sub section 1.1.5, cosmic rays are energetic charged particles, originating from outer space. The name is misleading, because for some time it was believed that

[^12]the radiation was electromagnetic in nature. Contrarily, most cosmic rays are nuclei of atoms, ranging from the lightest to the heaviest elements in the periodic table. In addition, they also include high energy subatomic particles. They strongly interact with matter, but they are able to travel from their distant emitters to the Earth, because of the low matter density in space. Then, they collide with atoms in the air atmosphere and produce other secondary particles that shower down to the Earth.
There are still many open questions mainly regarding the origin of cosmic rays, but it is evident that the knowledge of quantity and type of these particles, helps us to understand the acceleration processes involved and to measure the composition of the Sun and many other distant sources.
In the history of particle physics, cosmic rays are a milestone, because after their recent discovery, just last century, positron, muon and pion had been studied. In fact, before the particle accelerators reached very high energies, cosmic rays served as a source of particles for high energy physics investigations.

### 1.2.1 History of cosmic rays

In 1785 Coulomb found that electroscopes ${ }^{24}$ can spontaneously loose electricity in a certain time period, either by contact with less humid air or in the insulating supports [48]. One century after, Henri Becquerel made known the spontaneous radioactivity from elements in the ground. It was generally believed that the radioactivity caused air ionization and could be the most plausible explanation of the electroscopes' discharge. Moreover, further measurements, at the beginning of the twentieth century, demonstrated that such discharge was due to ionizing agents coming from outside the electroscope's vessel. Radiation from radioactive elements penetrated the container, producing ions in the air close the leaves and caused them to drop. Considering that the radioactivity originated from material in the crust, scientists started to calculate how much the consequent radiation should decrease with height. Bringing an electroscope at the top of Eiffel Tower in Paris ( 300 m above ground), the ionization rate due to the foreseen radiation was measured. Actually the measurement showed a diminution, but too small to confirm the previous estimation. Nevertheless the terrestrial origin of the unknown radiation continued to be the most common assumption, but the situation was so uncertain to keep alive both the idea of an extra-terrestrial and atmospheric origin.

The turning point was marked by Domenico Pacini (Fig. 1.9). In 1911 he observed a reduction ( $\sim 20 \%$ ) of the ionization rate at a depth of three meters underwater from the surface. Pacini concluded that not all the radiation could come from the radioactivity of Earth's mantle, but a part must be emanated from outside [106]. The radiation's decrease in underwater environment seemed to be in contrast with the weakening at the top of Eiffel Tower. The mystery was sorted out measuring the effect at some kilometres of altitude, thanks to balloons.
In fact the natural radioactivity was generated


Figure 1.9: Domenico Pacini during a measurement in May 1910. (Courtesy of Pacini family)

[^13]by cosmic rays ( $\sim 18 \%$ ), by sources from nature ( $\sim 23 \%$ ) and by sources in the atmosphere ( $\sim 59 \%$ ), such as the radon gas (now we have to add the contribution from human-caused background radiation). Close to the Earth's surface, the terrestrial and cosmic contributions slightly balanced each other and it was difficult to see an evident difference, moving for some dozens of metres. Therefore appealing results were obtained flying up with special balloons.

In 1912 Victor Hess found that the ionization increased more rapidly as he ascended in a balloon (Fig. 1.10(a)). The outcome of the experiment showed that the ionization diminished just above the ground, it had a minimum around 1 km and then it grew slightly until $\sim 4 \mathrm{~km}$. In the last part of the flight (from 4 km to 5.2 km ), the penetrating radiation became very strong and higher than on the ground (Fig. 1.10(b)). The solidity of this appraisal was guaranteed by the scientific apparatus consisting of three ionization chambers ${ }^{25}$. This was the confirmation that part of radiation entered the atmosphere from above [71]. Besides, he executed many balloon ascensions with different conditions: during the night, the day and even a Sun's eclipse. It was obvious that the radiation origin was related to something extraterrestrial, but not presumably the Sun. The name given to this radiation was cosmic ray, because it was thought it might


Figure 1.10: On the left photo, Victor Hess was preparing the balloon flight, in which he discovered the cosmic rays. On the right, the recorded points by Hess' ionization chambers, installed on the balloon. The presence of cosmic rays is evident only above 4 km . (From [85])
be a very penetrating electromagnetic wave. Only subsequently it was shown to be composed of material particles. In fact, the Pacini and Hess' investigations were only the beginning of the cosmic rays comprehension. Neither the composition nor the origin were unravelled at that period and some aspects are still now unsolved.

Another important step was obtained in 1928 by a lucky chance, when Jacob Clay recorded an ionization's dependence with the latitude during two trips [25]. The event spurred to measure the cosmic ray intensity changing the geomagnetic latitude. In 1932 Compton confirmed that there was a latitude correlation, corroborating that cosmic rays were charged particles, because such variation should not happen in case of gamma photons. Compton did not stop here, but furthermore he proved that most of the cosmic rays are positive. He counted the number of particles coming from west than from east close to the equator. Because of interaction with the Earth's magnetic field,

[^14]the west flux, constituted by positive particles, was higher.
The cosmic rays discovery opened a new way to understand the constituents of matter. In 1932, analysing the cloud chamber's tracks released by cosmic rays, Carl Anderson detected particles that acted like electrons, but with opposite charge [3]. The positron, so coined by Anderson, was the first evidence of antimatter and the experimental proof of the Dirac equation ${ }^{26}$, which was the first theory fully to account for relativity in the context of quantum mechanics. Some years after it is the turn of the subatomic particle muon, always by hand of Anderson in collaboration with Neddermeyer [4]. The method is repeatedly the same: to distinguish the track curve's dimension and direction produced by cosmic radiation, when it passed through a chamber dipped in a magnetic field.
It was already clear that the particles observed presumably were not the primary cosmic rays, but secondary products from the interaction with the atmospheric nuclei. Only in 1941 the first primary proton was proved, when Schein and co-workers carried out complex Geiger-Müller ${ }^{27}$ counter arrangements in balloon experiments [116].
Unfortunately the World War II slowed down the activity in this sector and the last detection is dated 1947, when the quartet Powell, Muirhead, Lattes and Occhialini placed for long time some photographic emulsions ${ }^{28}$ at high altitude mountains, under the bombardment of cosmic particles. Subsequently, the photographic plates were developed and the microscopic inspection of the emulsions revealed the tracks of another charged element: the pion [88].

From then on, the accelerators started to take off and the cosmic rays, which have the drawback to be out of human control, were ousted. Anyhow this is not the end of cosmic rays history, rather they strongly came back in the last decade in order to compensate to the limited energy the man can produce in the scientific facilities. Nowadays, cosmic rays are one of the most meaningful argument of astro-particle physics and they are studied to better understand very energetic astronomical processes.

### 1.2.2 Cosmic ray features

The composition, the flux and the energy range are important topics of cosmic rays, because they are a direct sample of matter from Cosmos. This discernment allows us also to provide an exhaustive illustration of the Universe structural evolution, because they concur to the formation of some metals.
Cosmic rays include practically all the elements in the periodic table and many subatomic particles. They are constituted by $99 \%$ of atomic nuclei and by $1 \%$ of electrons and positron. Considering the nuclei's fraction, about $89 \%$ are nuclei of hydrogen (protons), $10 \%$ of helium (alpha particle), and the remaining $1 \%$ of heavier elements, which are the end products of stars' nuclear synthesis. We are talking about the primary cosmic rays, namely the original charged particle before the interaction with the interstellar matter or the Earth's atmosphere. When the primary ray bangs into other matter, secondary particles are created. This process is called cosmic ray spallation and it is the beginning of nuclear fission and nucleosynthesis. The result of the collision is the expulsion of large numbers of nucleons from the object hit and consequently lighter and rare metals, as lithium, are produced. Differently, when the cosmic rays approach

[^15]Earth, they collide with the nuclei of atmospheric gases. In these collisions pions, kaons and muons are generated.

The upper layer of the atmosphere is not hit by a constant flux of cosmic rays. The Sun's solar wind and the Earth's magnetic field are the causes of this variability. The solar wind, which is modulated by the solar activity, diffuses magnetized plasma. The cosmic rays, which interact with the plasma, are decelerated and sometime stopped, if their energy is low. On the other side, charged particles are deflected by Earth's magnetic field, which is dependent on latitude and longitude ${ }^{29}$. First, the cosmic flux, charged both positively and negatively, differs from East to West due to the geomagnetic field polarity. Moreover the charged particles tend to move along the magnetic lines, hence the radiation intensity is lower at the Equator than at the poles, where the lines are concentrated and perpendicular to the surface.

The energy spectrum of the primary cosmic rays (Fig. 1.11) covers many decades and it is now known to extend beyond $10^{20} \mathrm{eV}$. This upper limit is fixed by the very poor statistics due to the extremely low flux intensity, around one particle every century in an area of $1 \mathrm{~km}^{2}$. Ultra-energetic particles interact with photons of $C M B R$ and cause a drastic lowering of the flux, called $G Z K^{30}$ cut-off. The lower energy limit is bound to the motion of the solar magnetic wind, which blocks the low energy galactic cosmic rays.
The curve's profile is not constant and in some selected regions it is compatible with


Figure 1.11: The experimental data of the cosmic rays energy spectrum in the wide range from $\sim 300 \mathrm{MeV}$ to more than $10^{20} \mathrm{eV}$. As explained in the end of previous section (1.1.5), the current most powerful particle accelerators stop at energies of $\sim 10^{13} \mathrm{eV}$, very far from the most energetic cosmic ray, ever recorded by man. (From [66])

[^16]different power law functions:
\[

$$
\begin{equation*}
\frac{\mathrm{d} \Phi}{\mathrm{~d} E} \propto E^{-\alpha} \tag{1.1}
\end{equation*}
$$

\]

where $\alpha$ is the differential spectral index, which suggests a non-thermal origin of cosmic rays. Two particular portions can be easy distinguished: the so called "knee" around $10^{15} \mathrm{eV}$ and the "ankle" around $10^{18} \mathrm{eV}$. Below the knee and beyond the ankle the dependence of cosmic ray intensity on particle energy is close to $\mathrm{E}^{-2.7}$, while between them is almost $\mathrm{E}^{-3.1}$. The vast energy spectrum indicates that there is a considerable amount of sources, which require different techniques to be detected.

There are many different and complementary techniques employed in this physics area. Some of them have the intent to examine primary cosmic ray, other the secondary products. These detectors can be sorted into:

* Ground experiments: AGASA, HiRes Fly's Eye and Pierre AUGER Observatory. They are designed to detect the ultra high energy cosmic rays. AGASA and $A U G E R$ are very large surface arrays, respectively of $100 \mathrm{~km}^{2}$ and $3000 \mathrm{~km}^{2}$. Differently HiRes utilizes the atmospheric fluorescence technique.
* Satellite experiments: $A M S-02$ and $P A M E L A$. They want to catch the antimatter content of the Universe, measuring the composition of cosmic particles.
* Balloon experiments: ATIC, BESS-Polar, CREAM and TRACER. They are been utilized for the study of medium energy cosmic rays, flying in Antarctica sky. The ATIC detector used the principle of ionization calorimetry, while the central device of BESS-Polar was a magnetic spectrometer. CREAM housed different systems capable of precise measurements of elemental spectra (for $\mathrm{Z}=1 \div 26$ ) nuclei over the energy range $\sim 10^{11}$ to $\sim 10^{15} \mathrm{eV}$. TRACER has worked in the domain from $\sim 10^{13}$ to $\sim 10^{15} \mathrm{eV}$, for nuclei with Z between 5 and 26 .


### 1.2.3 Cosmic ray origin

The cosmic rays, being electrically charged, are deflected by several magnetic fields throughout the galaxy and in the intergalactic space. This means that they don't travel straight from their sources, but their directions have been randomized, excluding the possibility to easily analyse them.
Actually the origin of cosmic rays is doubtful, but it is presumed to be in great measure associated to violent events, such as stellar explosions in our own galaxy. This is the most probable explanation, but not the only one, since the extension of the energy spectrum points to a variety of sources. In fact the first part of the spectrum, below $\sim 10^{15} \mathrm{eV}$, should be dominated by the galactic component of cosmic rays, while the last part, above the "ankle", by the extragalactic one.
In case of galactic cosmic rays, their energy derives from supernova explosions, which are very rare events (one every 50 years in our own galaxy). To justify the long term constancy of cosmic rays intensity, a not negligible part of the energy, released by such exceptionally high burst ( $\sim 10^{51} \mathrm{ergs}$ ), must be converted to produce them. It is commonly accepted that cosmic rays are accelerated in the resulting explosion shock waves, which pass through the surrounding interstellar gas. The mechanism is called Fermi acceleration mechanism ${ }^{31}$ and it provides an illustration on how to accelerate particles

[^17]up to $10^{15} \mathrm{eV}$. For higher energies an incontrovertible demonstration is still missing. Finally, most of the cosmic rays remain confined to the disk of the galaxy, trapped by its magnetic field.
A direct information of their place of production is lost, but the electromagnetic radiation they provoke can be studied. An important example is the Crab Nebula, a supernova remnant that emits radio synchrotron radiation due to primary electrons spiralling in the magnetic field. Also $\gamma$-rays, generated from the collision with interstellar gas, are observable.

The high-end spectrum in figure 1.11 indicates that the cosmic rays direction might be correlated to an extragalactic origin. According to the GZK limit, at these very high energies ( $\gtrsim 5 \cdot 10^{19} \mathrm{eV}$ ) the particles interact with the photons of the CMBR. The favourite branch is:

$$
\begin{equation*}
\gamma_{C M B R}+p \rightarrow \Delta^{+} \rightarrow p+\pi^{0} \tag{1.2}
\end{equation*}
$$

or

$$
\begin{equation*}
\gamma_{C M B R}+p \rightarrow \Delta^{+} \rightarrow n+\pi^{+} \tag{1.3}
\end{equation*}
$$

where pions are produced through the $\Delta$ baryon resonance. This process continues until the cosmic ray energy falls below the pion production threshold and the mean attenuation length is of the order of several Mpc , incomparable with the small dimension of our own galaxy ( 15 kpc ). Assuming a galactic origin for these ultra energetic protons, the absorption would be insignificant and the cut-off should not be present. On the contrary the flux drop seems to be an evidence as reported by the $A U G E R^{32}$ collaboration in the plot 1.12, supporting the extragalactic scenario with a suppression at $10^{20} \mathrm{eV}$. Moreover the cross section of this process and the $C M B R$ photons density fix


Figure 1.12: The $G Z K$ cut-off measured by the Pierre AUGER Observatory (filled points) and by HiRes instrument (open points). (From [42])
the maximum travel distance, that can be covered by particles with an energy higher than pion production threshold. These extragalactic cosmic rays, travelling over 50 Mpc, should never be observed on Earth. This remoteness is known as $G Z K$ horizon. A further validation is given by the acceleration models, which predict that particles of energy larger than $10^{18} \mathrm{eV}$ have to be addressed to the extragalactic space. Preliminary experimental data come from the $A U G E R$ project. It seems that the highest energy events, which are not deflected much by the weak magnetic fields in our own galaxy,

[^18]present a direction effectively correlated with $A G N s^{33}$ [41]. Here the protons could be accelerated by the strong magnetic field associated by the central black hole. Unfortunately there is nothing certain, because these data are affected by poor statistics and large errors. An example, which marks the unresolved situation, comes from the controversial data of $A G A S A$ experiment.

## $1.3 \gamma$-rays

The cosmic rays are not the only messengers from the unreachable celestial bodies: a substantial contribution is furnished by the electromagnetic radiation. Only a small part of this light is visible, the rest spreads in all the electromagnetic spectrum. The main feature of these photons is to be neutral, so they are not deflected by the magnetic fields in the outer space. They point back directly to the production source, providing stunning elements for the comprehension of the astrophysical and fundamental processes under extreme conditions.
A brief overview of the electromagnetic radiation spectrum and the associated detectors has been already presented in subsection 1.1.5. Here the attention is focussed on the very energetic light: $\gamma$-rays. Typically they manifest the presence of a high energy phenomena in the Universe, often related to AGNs, Pulsars, Microquasar or Supernova remnants. These processes include cosmic ray impacts with interstellar gas, stars explosions, and interactions of energetic electrons with magnetic fields.

### 1.3.1 History of $\gamma$-rays

The presence of gamma emission in the Universe was foreseen by theoreticians many years before the advent of the suitable instruments [58, 68, 100]. Initially, experiments were carried out with the help of spacecraft or special balloons in the 1960s, because $\gamma$-rays are mostly absorbed by the Earth's atmosphere. Some detectors were foreseen to catch $X$ and $\gamma$-rays flashes from nuclear bomb blasts: the most famous case was the Vela program ${ }^{34}$. The first gamma telescope, sensitive to energies greater than 50 MeV , was put into orbit with the satellite Explorer-11 away back in 1961, recording only 22 gamma photons. A problem to the power system compromised soon the data-taking, but not the publication of the article, which marked the beginning of the experimental gamma discipline [86]. Six years later, OSO-3 improved that result with 621 events attributable to cosmic $\gamma$-rays.
In 1972, it is the turn of $S A S-2$, a satellite completely dedicated to the gamma astronomy. Unhappily, it stopped to work only after seven months owing to a serious technical problem. The European Space Agency was more lucky: between 1975 and 1982 a similar detector called COS-B operated very well reporting a complete map of the Milky Way up to 5 GeV . However the main limit was the poor spatial and temporal resolution. Only in 1991 the CGRO (Compton Gamma-Ray Observatory) started its mission, transmitting very explicative data on the most energetic electromagnetic radiation. Its energy domain swept from 20 keV , in the hard $X$-rays upper limit, to 30 GeV , thanks to four main telescopes on board. One of these four telescopes was EGRET (Energetic Gamma-Ray Experiment Telescope), which measured high energy ( 20 MeV to 30 GeV ) $\gamma$-ray source positions to a fraction of a degree and photon energy within $15 \%$. Initially it was validated that a considerable amount of $\gamma$-rays came from the

[^19]galactic plane, but subsequently the $N A S A$ 's jewel revealed some special extragalactic gamma sources, that now we call Blazars ${ }^{35}$. CGRO was a success and opened the way to the development of new instruments.
The following satellite, HETE-2 (High Energy Transient Explorer 2), was lunched on October 2000. In that period, most of the attention was dedicated to the understanding of GRBs (Gamma-Ray Burst), the most luminous and sudden $\gamma$-ray flashes, likely associated with extremely energetic explosions of massive stars (hypernovae) in distant galaxies. The coordinates of $G R B s$ detected were distributed to several ground-based telescopes within few seconds, thereby allowing multiwavelength observations of the initial phases of the afterglow. In fact, this satellite did not house simply the gamma detector, but even $X$-ray and $U V$ instruments.
The last two gamma space missions started in 2002 with INTEGRAL (INTErnational Gamma-Ray Astrophysics Laboratory) and in 2004 with Swift. INTEGRAL is dedicated to the fine spectroscopy $(\mathrm{E} / \Delta \mathrm{E}=500)$ and imaging (angular resolution of 12 arcmin) of objects in the energy interval 15 keV to 10 MeV . Swift is composed by three main instruments, which work in tandem to assure rapid identification of GRBs. One runs in the optical domain 170 to 600 nm , another in the $X$-rays energies 0.3 to 10 keV , while the third in the hard $X$ and soft gamma range 15 to 150 keV . Both satellites are still operating, after many years of activity. INTEGRAL has detected more than 700 gamma sources, as reported in the fourth $I B I S / I S G R I$ soft $\gamma$-ray survey catalogue, while Swift has already recorded more than 500 GRBs. They are constantly providing new insights, helping us to understand processes such as the formation of new chemical elements and the mysterious $G R B s$.

The balloons should not be forgotten, because they were and are a fruitful alternative for $\gamma$-rays study. Often they have been also used for the development of new technologies and payloads for space flight missions. The history of gamma balloonborne experiments is quite recent, but it was immediately stimulating. The extraordinary flights of the gamma imaging telescope GRIS in 1988 allowed to record the first cobalt-decay $\left({ }^{56} \mathrm{Co}\right) \gamma$-ray image from the spectacular supernova $S N 1987 \mathrm{~A}$ and the positron annihilation line at 511 keV from the galactic centre [123, 92]. The obtained result, observing the newborn supernova, was an important brick for the investigation of stars' nucleosynthesis of elements beyond helium. GRIS continued his marvellous activity with other three flights in 1995, mainly analysing the galactic $\gamma$-ray spectrum and reporting new interesting conclusions about the formation of ${ }^{26} \mathrm{Al}$, an isotope that is formed in massive stars near the end of their lives [102].
Further balloon experiments pursued the research in the hard $X$-rays and soft $\gamma$-rays regions. In 1992 and a second time in 1995, HIREGS flew over the Antarctica sky in order to observe solar flares and examine the flare acceleration processes, unresolved by scintillators that have been used in spacecrafts. The High Resolution Gamma-Ray and Hard X-Ray Spectrometer was conceived to operate from 20 keV to 18 MeV with an energy resolution of 1.5 keV , and up to 160 MeV with 0.5 MeV resolution. It confirmed and in addition improved the spectroscopic measurements of GRIS related to the electron-positron annihilation line and the ${ }^{26} \mathrm{Al}$ nucleosynthesis line.
The balloon-borne telescope $T I G R E$ is very recent (2007 \& 2010). A completely different technology, based on multi-layers of thin silicon detectors, was used to measure the energy losses of Compton recoil electrons in the MeV range. This new technique facilitated the background rejection, the sensitivity improvement and a clear image reconstruction. Moreover, the Tracking and Imaging Gamma-Ray Experiment acted as

[^20]both a Compton telescope and a pair detector, guaranteeing a good efficiency over the entire interval 0.3 to 100 MeV and a wide field of view. Some black holes and Pulsars in the galactic neighbourhood were the main targets.

For energies higher than some hundreds GeV , the gamma flux is so weak that the small effective area of satellite experiments is insufficient. The history of ground-based telescopes started away back in 1968 with the Whipple observatory in southern Arizona ${ }^{36}$. It was the pioneer of atmospheric Čerenkov imaging technique in the very high energy (VHE) range 100 GeV to 10 TeV . Whipple was a 10 m telescope designed to collect the faint light of the Čerenkov radiation produced in the interaction between a $\gamma$-ray and the atmosphere. Analysing the properties of the collected blue Čerenkov light, it was possible to trace back to the original $\gamma$-ray. The main discovery occurred after twenty years of continuous progress, in 1989, when Whipple detected the first $\gamma$-rays from the Crab nebula [56]. The measured flux was steady and Crab became the standard candle in the VHE $\gamma$ astronomy.
The astonishing result of the Whipple collaboration pushed the construction of new instruments in the beginning of 1990s. HEGRA (High Energy Gamma-Ray Astronomy) made use of the same principle of its precursor, introducing the stereoscopy, arranging four telescopes on a square of 100 m side length with two additional telescopes centred. This innovative approach to operate simultaneously with several telescopes improved the angular resolution, the spectral reconstruction of the primary particle and the background rejection efficiency. All of this could be translated in a sensitivity to very weak $\gamma$-ray sources, less than $1 \%$ of the Crab nebula flux in 100 h of data-taking. On the other side, this system was able to observe the most energetic photon $(16 \mathrm{TeV})$ for that period from the Blazar Markarian 501.
Another air shower competitor experiment in the very high energy domain was $C L U E$ (Čerenkov Light Ultraviolet Experiment). However, it should be considered complementary, because it was based on a different working method, which allowed to operate with Moon and to point luminous regions. The detector was sensitive in the $U V$ range $(190 \div 230 \mathrm{~nm})$ preventing the use of the classical $I A C T^{37}$ algorithms. CLUE did not achieve important results, but it was an additional sign that this new astrophysical branch provoked high interest.

### 1.3.2 Current $\gamma$-rays detectors

Currently the main and powerful satellite-borne gamma detector is the originally called GLAST (Gamma-Ray Large Area Space Telescope), renamed FERMI in honour of the famous Italian physicist Enrico Fermi. Another important instrument is AGILE (Astrorivelatore Gamma ad Immagini ultra LEggero), realized by the Italian Space Agency (ASI). As written in the subsection 1.3.1, INTEGRAL and Swift are still well operating satellites.

The core of the FERMI space observatory is the LAT (Large Area Telescope), an imaging high energy $\gamma$-ray telescope sensitive in the energy interval from $\sim 20 \mathrm{MeV}$ to $\sim 300 \mathrm{GeV}$ and able to cover the entire sky in only three hours, providing a continuous and efficient scan. The angular resolution is of the order of 1 degree, strongly

[^21]dependent on energy. Point-like emissions are well determined up to few GeV , while going to higher energies, the poor statistics allows only a long integrative study of diffuse sources. These features show a superior performance compared to its predecessor $E G R E T$ (Table 1.1). The improvement in sensitivity is of a factor 30.
$L A T$ is composed of four subsystems, which have specific rules in the detection mech-

| Comparison between FERMI/LAT \& EGRET |  |  |
| :--- | :--- | :--- |
| PARAMETERS | FERMI/LAT | EGRET |
| Energy range | $20 \mathrm{MeV} \div 300 \mathrm{GeV}$ | $20 \mathrm{MeV} \div 30 \mathrm{GeV}$ |
| Peak effective area after background re- <br> jection | $>8000 \mathrm{~cm}^{2}$ | $1500 \mathrm{~cm}^{2}$ |
| Field of view | $>2 \mathrm{sr}$ | 0.5 sr |
| Angular resolution of single photon on- <br> axis | $<3.5^{\circ}(100 \mathrm{MeV})$ <br> $<0.15^{\circ}(>10 \mathrm{GeV})$ | $5.8^{\circ}(100 \mathrm{MeV})$ |
| Energy resolution | $<10 \%$ | $10 \%$ |
| Dead-time per event | $<100 \mu \mathrm{~s}$ | 100 ms |
| Source location determination | $<0.5^{\prime}$ | $15^{\prime}$ |
| Point source sensitivity | $<6 \cdot 10^{-9} \mathrm{~cm}^{-2} \mathrm{~s}^{-1}$ | $\sim 10^{-7} \mathrm{~cm}^{-2} \mathrm{~s}^{-1}$ |

Table 1.1: Main characteristics of the FERMI/LAT detector in comparison with his predecessor EGRET.
anism based on pair production effect ${ }^{38}$. The tracker reconstructs the path of the electron and positron pair, produced by the initial $\gamma$-ray. The calorimeter measures the complete amount of energy released by the particles. The anti-coincidence detector, placed on the outermost layer of the tracker, is a shield to block the unwanted charged cosmic rays. The data acquisition system is an electronic system that processes all the information coming from the previous substructures, selecting only the events of interest. The typical $\gamma$-ray evidence is underlined by no signal in the anti-coincidence shield, two joined tracks in the tracker and an electromagnetic shower in the calorimeter. $F E R M I$ is equipped of a second important instrument, the GBM (Gamma-ray Burst Monitor), which extends down the detectable energy domain to 8 keV . The $G B M$ field of view is several times larger than $L A T$, therefore very soft gammas and hard $X$-rays are caught by his 14 scintillation detectors to localize sudden bursts.

AGILE is a small FERMI observatory competitor, which consists of two instruments: AGILE-GRID and SuperAGILE. This combination sustains simultaneous detection photons in the $30 \mathrm{MeV} \div 50 \mathrm{GeV}$ and in the $18 \div 60 \mathrm{keV}$ energy ranges. The detector is very compact and light, it weights only $\sim 130 \mathrm{~kg}^{39}$, allowing a fast monitoring of the sky. This is an important peculiarity, which helps the rapid repositioning and imaging recording, after an alert of a strong gamma transient from a variable source.
The AGILE instrument, based on the advanced technology of the solid state silicon detectors, is quite powerful and cost-effective. The design concept is very similar to the previously described in the FERMI paragraph. AGILE-GRID contains a silicontungsten tracker followed by a caesium iodide calorimeter, everything covered by an anti-coincidence system. It is characterized by a large field of view of 2.5 sr , a good angular resolution of $15^{\prime}$, a fine spatial resolution and a small dead-time less than $200 \mu \mathrm{~s}$. The SuperAGILE is not thought to be a simple $G R B$ monitor, but it offers in addition the possibility of analysing $\gamma$-ray and hard $X$-ray sources with a good angular

[^22]resolution of 6 arcmin and a sensitivity of $\sim 10 \mathrm{mCrab}$ for one day integration.
Very high energy photons ( $>300 \mathrm{GeV}$ ) can be only revealed with ground-based telescopes. The extremely low particle flux requires detectors with extensive collective area, too huge and heavy for space missions. The detection technique on the ground is completely different, because the calorimeter is provided by the atmosphere. Primary $\gamma$-ray interacts with an air nucleus, producing a wide secondary particle shower. The EAS (Extended Air Shower) can be observed using arrays of counter detectors and through the Čerenkov light caused by his ultra relativistic part. This technique is called IACT.
These IACT telescopes, such as HESS, MAGIC and VERITAS, complement the capabilities of the previously described satellite-borne experiments. They have larger effective areas ( $>10^{4} \mathrm{~m}^{2}$ ), but small fields of view $\left(3 \div 5^{\circ}\right)$ and limited duty cycles relative to space observatories. However, the current Cerenkov telescopes extend a good sensitivity well below 300 GeV , furnishing a useful overlap with FERMI, in a formerly unexplored region of the electromagnetic spectrum. They can reach such a low energy threshold, because they use very large reflective surfaces to collect more photons and they are located at high altitudes, where the Čerenkov light density is higher. The main parameters of these three gamma telescopes are reported in table 1.2.

| Name | Location | Nr. $_{\text {Tel }}$ | Reflective surface $\varnothing$ | $\mathbf{E}_{\text {th }}$ | FoV |
| :--- | :---: | :---: | :---: | :---: | :---: |
| HESS | S | 4 | 12 m | 100 GeV | $5^{\circ}$ |
| MAGIC | N | 2 | 17 m | $55 \mathrm{GeV}(*)$ | $3.5^{\circ}$ |
| VERITAS | N | 4 | 12 m | 100 GeV | $3.5^{\circ}$ |

Table 1.2: Some important characteristics of the three main IACTs in the world. (*) In Sum-Trigger mode, see section 5.1, the threshold is 25 GeV .

HESS (High Energy Stereoscopic System) is a system of 4 IACT telescopes located in Namibia (Africa) at an altitude of 1800 m , that operates from 2003 in the 100 GeV to 100 TeV energy range [61] (Fig. 1.13(a)). The telescopes, which have a single reflective surface of $107 \mathrm{~m}^{2}$, are arranged on a square with 120 m sides. This spacing represents a compromise between the large base length required for good stereoscopic viewing and the requirement that two or more telescopes are hit by the same shower. The collected light is focused by 382 glass mirrors, disposed in the Davies-Cotton design for $f / d \simeq 1.2$. At the focal plane, the photo detector, called camera, is equipped with 960 PMTs (PhotoMultiplier Tubes), covering a $5^{\circ}$ field of view with a pixel size of $0.16^{\circ}$. The telescope' structure uses an alt-azimuth mount, which rotates on a 15 m diameter rail. It is made up of steel tubes, designed for high mechanical rigidity. Both azimuth and elevation are driven by friction drives acting on auxiliary drive rails, providing a positioning speed of $100^{\circ} / \mathrm{min}$. HESS is perfectly indicated to observe the galactic centre region, because it is situated in the southern hemisphere and has a large FoV.

VERITAS is another similar array of four telescopes, located in southern Arizona, each with a 12 m optical Davies-Cotton reflector made of 350 hexagonal glass mirrors for a total area of $110 \mathrm{~m}^{2}$ [132] (Fig. 1.13(b)). The Čerenkov radiation is reflected into a 499 pixels camera mounted on each telescope. Each pixel is a circular PMT XP2970 from Photonis with a quantum efficiency of $\sim 20 \%$ at 320 nm . The single telescope has a field of view of $3.5^{\circ}$ and operates in the energy domain between 100 GeV and 50 TeV . The mechanical structure is similar to that of the Whipple 10 m telescope. The customdesigned tubular steel optical support is propped and orientated by an alt-azimuth commercial positioner (RPM PG-4003) with a maximum speed of 1 degree per second
and a pointing accuracy of $\pm 0.01^{\circ}$.


Figure 1.13: Left: the 4 HESS telescopes. (From Sciencephoto webpage)
Centre: the 4 VERITAS telescopes. (Courtesy of N. Galante)
Right: the 2 MAGIC telescopes. (Courtesy of R. Wagner)
MAGIC (Major Atmospheric Gamma-ray Imaging Čerenkov Telescope) is a system of two telescopes situated at the Roque de Los Muchachos observatory in La Palma, one of the Canary Islands, at about 2200 m above sea level (Fig. 1.13(c)). With a dish diameter of 17 m , it is the largest optical surface in the world. The first telescope started to be operative in 2004, while the second one, at a distance of 85 m from the first, started taking data in fall 2009. Mainly due to the large reflective surface ( $236 \mathrm{~m}^{2}$ ), MAGIC is sensitive to cosmic $\gamma$-rays with energies between $50 \mathrm{GeV}(25 \mathrm{GeV}$ in SumTrigger mode) and 30 TeV . The lightweight carbon fibre frame allows a fast complete rotation of the telescope in less than 20 s . This rapid repositioning is an important feature especially when a $G R B$ alert arrives from satellite monitoring systems. More details will be described in chapter 4.

### 1.3.3 $\gamma$-rays characteristics

In general the radiation propagating in the Universe is generated by hot objects, such as stars, and presents a thermal nature, where the frequency is proportional to their temperature. This radiation can reach the keV domain, but hardly there is something so hot to justify an higher thermal energy. Hence, in the case of high energy cosmic and $\gamma$-rays, the non-thermal processes are the most plausible explanation. Their power-law spectrum (Fig. 1.11) shows no indication of a characteristic temperature dependency, promoting an emission from the most extreme conditions, by particles moving very near the speed of light. Environments as stellar explosions and giant black holes at the centre of active galaxies are the best candidates for $\gamma$-rays generation.
The accelerator mechanisms probably stimulate primarily charged particles, such as electrons and protons, by means of powerful electromagnetic fields. Sometimes the acceleration occurs in a typical one-shot process, but very often the process is fed by a different continuous increasing in particle energy. For instance, in Supernova shock waves the particles gain energy for a long time, even more than 10000 years, bouncing between magnetic fields. Only after this initial stage, $\gamma$-rays appear as secondary products of accelerated charged particles. There are different ways to generate $\gamma$-rays, and hereafter the fundamental processes are described.

The first is due to the decay of $\pi^{0}$, produced when an accelerated proton interacts with nuclei of the ambient medium, into two gammas (Fig. 1.14(a)). This is the main hadronic channel for $\gamma$-ray production. A protons population interacts through inelastic scattering with nuclei and other protons of the ambient material, creating charged and neutral pions (Eq. 1.4). The neutral pions have a short lifetime and they decay in
gammas. The reaction can only take place when the protons energy exceeds a minimum value of two times the pion rest mass ( $\sim 280 \mathrm{MeV}$ ). It is interesting to note that charged pions decay leptonically emitting neutrinos. Therefore the hadronic channel should be correlated to a neutrino emissions.

$$
\begin{align*}
p+p & \rightarrow \pi^{0}+\pi^{+}+\pi^{-} \\
\pi^{0} & \rightarrow \gamma \gamma  \tag{1.4}\\
\pi^{+} & \rightarrow \mu^{+}+\nu_{\mu} \\
\pi^{-} & \rightarrow \mu^{-}+\bar{\nu}_{\mu}
\end{align*}
$$

The second one, which is called leptonic channel, is driven by electrons. When the accelerated particles are electrons, they may undergo bremsstrahlung in the ambient medium (Fig. 1.14(b)), may suffer synchrotron radiation losses in local magnetic fields (Fig. 1.14(c)), or may transfer a significant part of their energy to photons via the Inverse Compton scattering process.
When an high speed electron is deflected by the electrostatic field, generated by a


Figure 1.14: Some sketches of the main $\gamma$-ray production mechanisms. On the left, the neutral pion decay into two gammas, from the scattering between a proton and the interstellar medium. In the centre, the Bremsstrahlung produced by a high energy electron deflected in the electric field of an atomic nucleus. On the right, the Synchrotron radiation generated when a relativistic electron passes through a strong magnetic field.
charged atomic nucleus, it radiates an electromagnetic wave due to bremsstrahlung ${ }^{40}$. The electron loses kinetic energy, which is transferred into a photon. The characteristic bremsstrahlung spectrum is continuous and proportional to $1 / \mathrm{E}$, where E is the energy of the photon. The released amount of energy is contingent on target's density and the crossing distance (Eq. 1.5), while the obtainable frequency range swaps from zero to the electron kinetic energy.

$$
\begin{equation*}
\Delta E=E_{e}\left(1-e^{\frac{d}{x_{0}}}\right) \tag{1.5}
\end{equation*}
$$

The parameter $d$ is the distance and $X_{0}$ is the radiation length, inversely proportional to the target density.
When a relativistic electron passes through a strong magnetic field, it radiates an electromagnetic wave due to the synchrotron radiation. This emission is polarized and the spectrum is characterized by non-thermal power law with a peak proportional to the transverse component of the magnetic field. The maximum possible energy of irradiated photons is shown in equation 1.6: $\gamma_{e}$ is the Lorentz factor of the electron

[^23]$\left(1 / \sqrt{1-\beta^{2}}\right), q_{e}$ the electron charge, $m_{e}$ the electron mass and $B$ the magnetic field.
\[

$$
\begin{equation*}
E_{\max }=\gamma_{e}^{2} \frac{q_{e} B}{2 \pi m_{e}} \tag{1.6}
\end{equation*}
$$

\]

High energy synchrotron radiation can be produced where a strong magnetic field is present, as close to a neutron star surface. This process is responsible for the radio emission from galaxy, from Supernova remnants and extragalactic radio sources, but it cannot exceed TeV limit. The limit's enhancement is provided by Inverse Compton scattering of these photons.
The Inverse Compton process occurs when relativistic electrons scatter off low energy photons, so that the photons gain and the electrons lose energy. It is probably the main gamma production mechanism in the Universe. On the basis of the original electron and photon energy, two regimes should be distinguished because the cross-section differs a lot: the Thomson and the Klein-Nishina limit.

$$
E_{(\gamma, f)} \approx \begin{cases}\frac{4}{3} E_{(\gamma, i)} \cdot \gamma_{e}^{2} & \text { if } \quad E_{e} E_{(\gamma, i)} \ll m_{e}^{2} c^{4}  \tag{1.7}\\ \frac{1}{2} E_{e} & \text { if } \quad E_{e} E_{(\gamma, i)} \gg m_{e}^{2} c^{4}\end{cases}
$$

In the Thomson regime, the emitted photons present a spectrum similar to the original photons, while in the Klein-Nishina regime, the result trend is steeper and is determined by the maximum energy of the participating electrons.

Both channels, hadronic and leptonic, generate a flux which is ruled by the density their charged parent particles and of the target involved. In the $\pi^{0}$ decay the external parameter is the ambient medium, in the synchrotron process is the strength of magnetic fields, while in the Inverse Compton process is the starting energy of target photons. All of this may be translated in a gamma energy spectrum closely related to the spectrum of the parent particles, which can be tracked back and studied.

In the SSC (Synchrotron Self-Compton) model [80] of astrophysical environments, where the gamma production follows a gravitational collapse, the leptonic channel is stimulated by a relation between the synchrotron radiation and the Inverse Compton mechanism. High energy $\gamma$-rays result from Inverse-Compton up-scattering of synchrotron radiation, peaked in the infrared or $X$-ray range, by the same relativistic electrons that produced the synchrotron radiation (Fig. 1.15).


Figure 1.15: Differential energy spectrum of photons in the $S S C$ model. (Courtesy of A. De Angelis)

Once generated, $\gamma$-rays propagate on straight lines through the Universe bringing precise information about the original source. The crossing matter during the travel is not irrelevant as in the case of the weak interactive particle neutrino. The native gamma flux decreases, absorbed before reaching the detectors. The cause resides in two fundamental processes: photon-matter and photon-photon pair production.
In the first case, $\gamma$-rays are absorbed in the interaction with hadronic or leptonic matter, as the interstellar and intergalactic medium. However the cross section is very low and the contribution is really trifling. Conversely, it is influential the main photon-photon pair production (Eq. 1.8).

$$
\begin{equation*}
\gamma+\gamma_{E B L} \rightarrow e^{+}+e^{-} \tag{1.8}
\end{equation*}
$$

For $\gamma$-rays with energy higher than 100 GeV , the target is provided by the optical and infrared part of the Extragalactic Background Light (EBL), produced by stars and reprocessed by cosmic dust (Fig. 1.16). When the $\gamma-$ ray energy is sufficiently high to crate an electron-positron pair, converting energy into matter, the spectrum is heavily modified. For this reason it is important to know the $E B L$, in order to extrapolate the intrinsic spectrum of a source.
The photon absorption along its path is a function of the original photon energy and the


Figure 1.16: A cartoon of the effect of $E B L$ on the $\gamma-$ ray emission from a distant object. If the density of $E B L$ photons is high (upper right graph), absorption is high and the highest energy $\gamma$-rays are lost. So the distribution of measured energies (spectrum) is strongly depleted. If instead the density is low (lower right graph), absorption is less and the spectrum is not changed as much.
redshift of the progenitor source. The light intensity decreases following the expression:

$$
\begin{equation*}
I=I_{0} \cdot e^{-\tau(E, z)} \tag{1.9}
\end{equation*}
$$

where $\tau$ is the optical depth.
Approaching the Earth, cosmic $\gamma$-rays are difficult to detect, because the noise is many orders of magnitude $\left(\sim 10^{8} \div 10^{9}\right)$ stronger. Charged cosmic particles are the primary source of background. Interacting with the Earth's atmosphere, they produce secondary particles and gammas. The experimental identification of primary gamma events is technologically very challenging and essential for the localization and the comprehen-
sion of the collective acceleration mechanisms, currently subject of a broad theoretical work. The energy range from 10 GeV to 50 GeV has not yet been experimentally well investigated. Lowering the energy threshold and the systematics is one of the major challenges of IACTs. For more details on the argument, read chapter 3.

### 1.4 Very high energy gamma sources

In the last ten years, the advent of new satellite and ground-based detectors for high energy $\gamma$-rays has impressively raised the scientific knowledge of the most violent phenomena in the Universe. To get an idea of the achieved detection progress, in figures 1.17 (a) \& $1.17(\mathrm{~b})$ the sky maps of the third $E G R E T$ and the second Fermi source catalogues are shown. The EGRET catalogue contains only 271 sources, the Fermi one 1873, detected in 24 months. An interesting aspect of the last Fermi catalogue is the presence of still a lot of not associated sources, which stimulates a wide range of astrophysical research. In the catalogue, 127 sources are considered to be identified, while plausible associations are proposed for 917 AGNs.

Gamma-ray sources may be distinguished in galactic and extragalactic. Both the satellite and the ground-based data show respectively that the flux and the number of emitters of $\gamma$-rays decrease with the distance from the galactic centre, where they are produced by the collision between cosmic rays and the diffuse galactic gas (Fig. 1.18(a) \& Fig. 1.18(b)). However a large variety of extragalactic sources, such as $A G N s$, have been discovered to emit non-thermal $\gamma$-rays.
In subsections 1.4.1, 1.4.2, 1.4.3 and 1.4.4 the main galactic sources are described, whereas in subsections 1.4.5 and 1.4.6 the extragalactic ones.

### 1.4.1 Supernova remnants

A Supernova remnant $(S N R)$ is the structure resulting from the explosion of a star in a Supernova. It is characterized by an expanding shock wave of ejected material. The shock wave consequent the collapse of a star, at the end of his cycle, can efficiently accelerate particles up to more than $10 \%$ of the kinetic energy of the explosion. Most of the galactic cosmic rays below energy of $10^{15} \mathrm{eV}$ are the progenitors of $\gamma$-rays from Supernova remnants. Consequently the measured VHE radiation is explained both with leptonic and hadronic models.
The first to be detected, assumed as standard candle in gamma astronomy, is the Crab nebula. In the $\mathrm{MeV} \div \mathrm{TeV}$ domain its flux is considered quite stable and used for the experiments calibration. However, in September 2010 and April 2011 the AG$I L E$ and Fermi satellites have reported an increased $\gamma$-ray intensity above 100 MeV $[28,31,27,104]$, not confirmed in the TeV region ${ }^{41}$. The uncommonly rapid flux variation, one order of magnitude higher than the standard value, has reached the peak of $(26 \pm 5) \cdot 10^{-6} \mathrm{ph} \mathrm{cm}^{-2} \mathrm{~s}^{-1}$ on a 12 hour time-scale (Fig. 1.19). It seems that particle acceleration mechanisms in inner nebular shock regions are more efficient than expected from classical theoretical models [129].

Often the Supernova spectra contain a pulsed emission from the central neutron star, which is the argument of subsection 1.4.2. When a $S N R$ contains a Pulsar object in the centre, it is called Pulsar Wind Nebulae. The pulsed radiation emitted from the

[^24]
(b) 2nd Fermi catalogue

Figure 1.17: On the top the 3rd EGRET catalogue, which consists of 271 sources: 5 Pulsars, 1 solar flare, 93 Blazars associations, 1 likely Radio galaxy, 1 normal galaxy and 170 unidentified sources. (From [54])
On bottom the Fermi LAT full sky map showing 1873 flagged sources by source class. Sources potentially confused with diffuse emission are shown in red. Those with any other flag set are shown in blue. Sources with no flag set are shown as small dots. (From [30])
jets, can undergo Inverse Compton scattering with remnant material, engendering high energy $\gamma$-rays.

The essential elements for these phenomena are the star explosions and the interstellar medium. Prolific regions, in this sense, are star-burst galaxies and clusters of galaxies. Star-burst galaxies are characterized by a high frequency of Supernova explosions, becoming efficient acceleration sites and a powerful $\gamma$-ray sources. On the other side, clusters of galaxies are characterized by a dense inter-cluster medium. Cosmic rays, generated during the cluster evolution, are entrapped inside and cannot escape. The history and the progress of the cluster may be deduced by $\gamma$-rays resulting from


Figure 1.18: Left: the sky map of the energy flux derived from the Fermi LAT data of the 2 nd catalogue. The image shows $\gamma$-ray energy flux in the domain between 100 MeV and 10 GeV , in units of $10^{-7} \mathrm{erg} \mathrm{cm}^{2} \mathrm{~s}^{-1} \mathrm{sr}^{-1}$. (From [30])
Right: the map of all $\gamma$-ray sources detected above 100 GeV . (Image credit: R. Wagner)


Figure 1.19: Left: the Crab $\gamma$-ray light curve above 100 MeV detected by AGILE-GRID in April 2011. The gray thin horizontal band shows the typical average flux $\left((2.2 \pm 0.1) \cdot 10^{-6} \mathrm{ph}\right.$ $\mathrm{cm}^{-2} \mathrm{~s}^{-1}$ ), and the gray vertical lines mark the time period without data caused by a communication problem. Right: the $\gamma$-ray pulsar-subtracted spectrum of the Crab nebula flare. The AGILE flaring spectral data (marked in red) were obtained for a 1-day integration during the interval 2011/04/15 09:40 UT-2011/04/16 0.9:40 UT. Data points marked in black colour show the average nebular spectrum. The red curve is the result a possible theoretical model discussed by $A G I L E$ collaboration. The spectral region marked in green shows the $X$-ray spectrum of an inner region of nebula. This is indicative of an $X$-ray upper bound expected from the flare. (From [27])
the interaction between primordial cosmic rays and intra-cluster gas.

### 1.4.2 Pulsars

After a supernova explosion, a dense and fast rotating neutron star is formed in the centre, surrounded by the expanding remnants (Fig. 1.20). Inhomogeneities during the gravitational collapse, cause the neutron star's angular momentum, which increases the rotation speed in relation to its progressive compaction. The particles' acceleration is favoured in this area affected by intense fields, causing beamed electromagnetic radiation, regularly visible only when the beam is pointing towards the Earth. From here the name Pulsar. The radiation's direction is fixed by the magnetic axis of the Pulsar, which does not necessarily coincide with the position of the rotational axis. Without this misalignment, it is impossible for a stationary observer to see the pulsed feature. The pulsed irradiated emission is due to the interaction of the intermittent pulsar wind
outflow with the neighbouring ambient medium.
The experimental spectrum is still under study. Different models predict power law trend with different cut-off in the interval $1 \div 100 \mathrm{GeV}$. The most quoted ones are the Outer gap and the Polar cap models (Fig. 1.21).
In the Polar cap model electrons are accelerated in the open field region near the magnetic poles, radiating $\gamma$-rays via synchrocurvature ${ }^{42}$ radiation. A component of these high energy photons are subjected to pair production, but the rest, with lower energy, can survive and escape to infinity. The relevant feature of the Polar cap is a steep cut-off in the spectrum, which follows a super exponential trend [67].
In the Outer gap model the acceleration


Figure 1.20: Schematic view of a Pulsar. The sphere in the middle represents the neutron star, the curves indicate the magnetic field lines and the protruding cones represent the emission zones. (Creative Commons licenses) mechanism is considered to take place in the outer magnetosphere, far away the neutron stellar surface [23]. The $\gamma$-ray production is determined by photon-photon pair production, which is less energy dependent compared to the previous model. The resultant spectrum is smoother and the cut-off appears at higher energies.
$C r a b$ is one of the few known Pulsar TeV emitters. MAGIC is the only IACT telescope


Figure 1.21: An illustration of Pulsar's magnetosphere (left) and the most popular $\gamma$-ray emission mechanisms from a Pulsar (right). On the right top, the Polar cap and on the right bottom the Outer gap model. (From [96])
able to extend the detection limit to the never reached low energy threshold of 25 GeV . More details are presented in chapter 5.

[^25]
### 1.4.3 Binary systems



Figure 1.22: An artistic view of the accretion disk formation in a binary system.

The common definition of a Binary system indicates two stars that are orbiting around their common centre of mass. Often the distance between the two stars is such that there is no mutual effect and they essentially evolve separately. Sometimes it happens that the stars are close enough to influence each other gravitationally or even exchange mass, modifying their evolution. The more massive object, typically a white dwarf, a neutron star or a black hole of few solar masses, accumulates matter from its companion, forming an accretion disk (Fig. 1.22). In case both the system's components fill their Roche lobes ${ }^{43}$, they give rise to an envelope that surrounds both stars. The accumulated gas in the accretion disk rotates in the external shell, heats up, and in a second stage can falls onto the compact star. Here the in-falling gas meets extreme conditions, which feed the generation of $X$-ray and $\gamma$-rays.

### 1.4.4 Giant molecular clouds

The molecular clouds represent a passive source of $\gamma$-rays. They don't produce any primary cosmic ray useful for an internal active gamma creation. They are simply a relatively dense barrier for the travelling high energy cosmic rays. The collision can be a localized sources of $\gamma$-rays. Generally the flux is not very high, but it may be enhanced if cosmic rays are trapped in cloud magnetic fields. At the present time, they are observed to study the cosmic-ray propagation. The technique is based on the measurement of the gamma flux from molecular clouds located at different distances along the path of an ultra high energy cosmic ray.

### 1.4.5 Active galactic nuclei

$A G N s$ are galaxies with super massive $\left(\gtrsim 10^{6} \mathrm{M}_{\odot}\right)$ black holes in the centre. The observed radiation is characterized by different aspects, which may be unified in a single model that explains the different spectral categories of $A G N s$. At the centre of this system there is the engine, a massive black hole, surrounded by an accretion disk with fast moving clouds. Sometimes the falling matter to the central object stimulates powerful and narrow jets, perpendicular to the galactic plane (Fig. 1.23). The observer's view angle respect to the jet determinates the spectral energy distribution of the emitted radiation.
AGNs may be divided into two main classes, radio-loud and radio-quiet. In the first one, the emission contribution from jets is dominant and so it cannot be correlated to a stellar origin, namely from the stars that compose the galaxy. In the second case, the jets are simply missing or their emission is negligible. Several subclasses are related to the observational conditions.

[^26]

Figure 1.23: The $A G N$ unified model. (Image credit: Aurore Simonnet, Sonoma State University)

* Seyfert I \& II: the unified model proposes that in Seyfert the line of sight points directly to the active nucleus. They show narrow emission lines of hydrogen, helium, nitrogen, and oxygen from the accretion disk surface and a strong nuclear $X$-ray radiation. The optical continuum emission, originated closer to the black hole, is present only in the Seyfert I, because the Seyfert II are observed through an obscuring structure, which prevent the detection. The common host for these $A G N s$ is a spiral galaxy.
* Quasars: it represents an intermediate position of the observer, where the central body, just outside the black hole horizon events, is directly seen. It is an extremely luminous object, more than the host galaxy. Its spectrum covers almost all the bands, mainly in the optical and $X$ one. Some Quasars are also strong sources of radio and $\gamma$-rays. The host galaxies can be spirals, irregulars or ellipticals. The Quasar's luminosity is proportional to the host galaxy mass, so that the most luminous Quasars inhabit in the elliptical galaxies.
* Radio galaxies: with the Radio galaxies the observer is moving towards the jet line. They typically manifest two lobes of radio emission, nearly aligned with the jets. These radio waves are very intense and due to the synchrotron processes. The ordinary radio galaxies host is elliptical, because it contain the most massive black holes.
* Blazars: when the line of sight points to the relativistic jet, the active galaxy is called Blazar. The special alignment with the jet explains some peculiar features, such as very high luminosity, very rapid variation and high polarization. Inside the jet, where a strong magnetic field is present, different particles interact producing a variety of observed non-thermal energy. The radiation spans from low radio frequencies to extremely energetic $\gamma$-rays. The involved processes are synchrotron radiation and Inverse Compton. The jets in Blazars are the favoured site of $\mathrm{GeV} \div \mathrm{TeV}$ photons production.

Depending on the emission properties, Blazars are divided into two classes: Flat Spectrum Radio Quasars (FSRQ) and BL Lac objects (BL Lacs). The FSQR sources show strong and broad emission lines, while BL Lac objects show no optical emission lines. In both cases the host galaxies are giant ellipticals.

The relativistic jets, emerging from the central black hole, are likely the right place where the particles are accelerated. The mainstream interpretation of the acceleration mechanism in the jets is the Synchrotron Self-Compton ejection from ultra relativistic electrons. Only radio-loud AGNs can generate VHE $\gamma$-rays, detectable by the IACT telescopes. Moreover, when a clear correlations between $\mathrm{TeV} \gamma$-rays and non-thermal $X$-rays exists, the leptonic population is considered to be the main channel of production.
The best-known TeV AGNs are Markarian 421 and 501, highly variable and often powerful gamma sources.

### 1.4.6 Gamma-ray bursts

$G R B s$ (Gamma-ray bursts) are mysterious and powerful bursts of $\gamma$-rays, appearing to be distributed uniformly in the sky. They are the most luminous events in the Universe, normally linked to exceptionally energetic explosions of extragalactic origin. Even if the $G R B$ 's light curves are extremely diverse and complex, the distribution of the observed duration shows a clear bimodal trend. In agreement with this peculiarity, they are divided in two groups: short bursts, lasting fractions of second, and long bursts (Fig. 1.24).
Long $G R B s$ are affiliated to super massive stars ( $>40 \mathrm{M}_{\odot}$ ) core collapse and the sub-


Figure 1.24: A sketch that simplifies the $G R B$ formation in two main different scenarios. (From David Darling webpage)
sequent rapid formation of a black hole. Short $G R B s$ have not a clear origin. They are likely associated to a fusion of two neutron stars into a black hole or directly a merging
of a black hole and a neutron star. The knowledge discrepancy between the two classes is fed by the presence of bright afterglows in the long $G R B s$, which have have been studied in greater detail than their short counterparts.
So far, GRBs have only been observed by satellites, while no evidence has been recorded in the VHE band. The main obstacle could be the $E B L$ gamma absorption, not negligible due to their huge distance.

## Atmospheric showers \& IACT technique


#### Abstract

PARTICLES originating in astrophysical processes are meaningful messengers of physics laws in the Universe. They cover long distances, sometimes travelling straight in line if they do not carry electric charge, or otherwise deflected by magnetic fields. Once arrived on the Earth, they may interact with atmospheric atoms, initiating extended air showers. Their evolution mainly depends on the nature of the primary particle and the atmosphere conditions. If the particle gets absorbed, the atmosphere can be considered a sort of natural calorimeter. The secondary products are the main targets of most of the ground-based VHE experiments, which can use different detection methods. The first part of this chapter is focused on the physics of the extended air showers. Then, the IACT technique and the analysis procedure, which takes advantage of that, are described.


### 2.1 The atmospheric showers

The extended atmospheric shower is the result of the interaction, in the high atmosphere, between the air atoms and a high energy cosmic particle, the so-called primary particle. The shower properties depend especially on the kind of the primary particle. It can be a proton, a nucleus, an electron, a photon, or rarely a positron.
The layouts of the experiments are adapted to the energy and the typology of the radiation under study. As mentioned in sub-section 1.2.2, there are vast arrays of detectors (e.g. the Pierre Auger observatory) intended to observe showers initiated by ultra and extreme high energy ( $\mathrm{E} \gtrsim 10^{15} \mathrm{eV}$ ) cosmic rays. Others, like the MAGIC telescope, that take advantage of the secondary products to get information on a very high energy ( $10^{10} \mathrm{eV} \lesssim \mathrm{E} \lesssim 10^{14} \mathrm{eV}$ ) primary $\gamma$-ray.
The ground-based telescopes cannot detect directly the primary cosmic ray, but they can collect its secondary products. Hence, the comprehension of the EASs is essential to develop new strategies for the $\gamma$-rays selection and the background rejection in the new generation IACT telescopes. Thus, scientists can draw new conclusions on the origin and the unknown properties of the primitive cosmic rays.

### 2.1.1 EAS history

The EAS history is tightly related to the discovery of cosmic rays and its further consequent deepening. In 1934, Bruno Rossi noticed the observation of near-simultaneous discharges of two separated and distant Geiger counters, located in a horizontal plane,
during the preparation of a measurement of the so-called East-West effect. He hypothesized that the counters were struck by very extensive showers of particle, but unfortunately he had not time to study this phenomenon more closely [114]. However, this was one of the most meaningful findings in early cosmic-ray investigations.
In 1937, Pierre Auger, unaware of Rossi's report, recorded independently that the cosmic radiation events were coincident in time, so associated to the same event. Further investigations, placing one of the counters in a different building more than 115 m away, revealed the correctness of the Rossi's hypothesis: a new branch of atmospheric physics was opened. Auger pursued this work at high altitudes and succeeded in explaining the origin of the $E A S$ and in quantifying the size distribution. He carried out a systematic identification of its constituent elements, as electrons, protons, and muons, that reached ground level spreading over a large area up to hundreds of squared meters [5]. Moreover, he declared to have observed showers up to $10^{15} \mathrm{eV}$, an energy domain still unknown at that time. This method allowed to register only particles that reached the ground level, but it did not explain the $E A S$ development in the atmosphere.
Not much later, Homi J. Bhabha and Walter Heitler published a mathematical model, based on an expression for the probability of scattering positrons by electrons, which describes how primary cosmic rays interact with the upper atmosphere [12]. In their model, EASs are generated by the cascade production of $\gamma$-rays and $\mathrm{e}^{ \pm}$pairs.

It must be pointed out that such measurements were made possible by the use of coincidence electronic circuits, which are able to warn the simultaneous (within a small time gate) passage of ionizing particles in far-between detectors. The inventor was Rossi in the 1930, who employed several triode vacuum tubes ([113]). The circuit was immediately adopted by many experimenters and the same concept is nowadays used in particle physics and in other areas of technology. It can be considered as the first primordial AND circuit, precursor of the logic ports in the modern computers.

### 2.1.2 Showers description

Primary cosmic rays typically approach the Earth's atmosphere at relativistic speed. They collide mainly with oxygen and nitrogen atoms, and generate fragments that tend to move in the same direction of the primary. In turn, the fragments decay or crash into more air molecules, creating a falling cascade that also spreads slightly sidewise. Therefore, the primary energy is shared out among millions and more secondary particles.

Two kind of showers can be distinguished. The first one, so-called hadronic shower, is initiated by a proton or a nucleus (Fig. 2.1(a)). The products of the first interaction are mainly pions ( $\sim 90 \%$ ), kaons and other nuclei, which constitute the hadronic core. The cascade is divided into three components, associated to the nature of the following secondary particles:

* Electromagnetic: this component derives mainly by the neutral pions decay.

$$
\begin{equation*}
\pi^{0} \rightarrow \gamma+\gamma \tag{2.1}
\end{equation*}
$$

The produced photons are so energetic that can be converted in $\mathrm{e}^{ \pm}$via pairproduction. Further photons are then created by bremsstrahlung in a repetitive cycle, which generates new secondary particles with lower energy. Typically, one third of the primary energy is found in this component, because almost $30 \%$ of the secondary products are neutral pions.

* Hadronic: this component comprises the charged fragments of the first and subsequent collisions, which can hit other atmospheric atoms. Even the secondary charged pions can strike new nuclei, starting again the cycle. The hadronic interactions can continue as long as the available energy is higher than the pion critical energy ( $\sim \mathrm{GeV}$ ).
* Muonic: this component is fed by the decay of the charged pions.

$$
\begin{align*}
& \pi^{+} \rightarrow \mu^{+}+\nu_{\mu}  \tag{2.2a}\\
& \pi^{-} \rightarrow \mu^{-}+\bar{\nu}_{\mu} \tag{2.2b}
\end{align*}
$$

The weak interacting neutrinos travel undisturbed, while some of the unstable muons can further decay, through the reactions:

$$
\begin{align*}
& \mu^{+} \rightarrow e^{+}+\nu_{e}+\bar{\nu}_{\mu}  \tag{2.3a}\\
& \mu^{-} \rightarrow e^{-}+\bar{\nu}_{e}+\nu_{\mu} \tag{2.3b}
\end{align*}
$$

At this point, the new born $\mathrm{e}^{ \pm}$can start another electromagnetic component. In addition, also charged kaons can directly contribute to the muonic component, according to the processes:

$$
\begin{align*}
& \mathrm{K}^{+} \rightarrow \mu^{+}+\nu_{\mu}  \tag{2.4a}\\
& \mathrm{K}^{-} \rightarrow \mu^{-}+\bar{\nu}_{\mu}  \tag{2.4b}\\
& \mathrm{K}^{+} \rightarrow \pi^{+}+\pi^{0}  \tag{2.4c}\\
& \mathrm{~K}^{-} \rightarrow \pi^{-}+\pi^{0} \tag{2.4d}
\end{align*}
$$

The latter two relations (2.4c \& 2.4d), which have a branching ratio of $63.4 \%$, supply again the hadronic shower.


Figure 2.1: Left: an hadronic shower generated by a cosmic ray. The three components, electromagnetic, hadronic and muonic, are illustrated. Right: an $E A S$ initiated by a $\gamma-$ ray. It is a continuous repetition of $\mathrm{e}^{ \pm}$pair-production and bremsstrahlung. (Courtesy of Konrad Bernlöehr)

In the previous considerations, it has been exposed the general case of hadronic showers. It is possible to simplify substantially the scenario, assuming that cascades, originated
by heavy nuclei with mass number A, can be handle as the superimposition of A proton sub-cascades with energy E/A.

The second kind of showers, the so-called electromagnetic shower, is induced by a high energy photon ${ }^{1}$ (Fig. 2.1(b)). A secondary $\mathrm{e}^{ \pm}$pair is formed by electron pair-production. Subsequently, the electrons and positrons radiate new photons via bremsstrahlung, as in the electromagnetic component of the hadronic shower. The growth continues in a recursive way, until the shower particles reach the critical en$\operatorname{ergy}^{2}\left(\mathrm{E}_{c}=\sim 83 \mathrm{MeV} / \mathrm{Q}\right.$, where Q is the particle charge in electronic units) and cannot trigger so frequently the electron pair-production. Hereafter, the ionization of atmospheric atoms becomes the dominant process, the electrons rapidly cool off through the thermalisation and the shower quickly dies out. The whole process lasts about $10^{-4}$ seconds.
The electron's radiation length ${ }^{3}\left(\mathrm{X}_{0}\right)$ is approximately $36.7 \mathrm{~g} / \mathrm{cm}^{2}$. After a distance of $9 / \mathrm{X}_{0}$ from the first collision, approximately the mean free path, $63 \%$ of all incident cosmic $\gamma$-rays are converted in $\mathrm{e}^{ \pm}$. The maximum development of the cascade, namely the maximum number of electrons, is closely proportional to the primary energy. The higher the original photon energy, the larger the number of permitted electron pairproduction processes. Also the position of the maximum ${ }^{4}$ is logarithmically correlated to its energy. For primary $\gamma$-rays of 20 GeV to 20 TeV , it spreads in the range of 250 to $450 \mathrm{~g} / \mathrm{cm}^{2}$, corresponding to a height of about 7 to 12 km above the sea level.

In 1954, Heitler proposed a relatively simple model to describe in first approximation the development of an electromagnetic shower [69]. Assuming that the primary energy


Figure 2.2: The Heitler model for an electromagnetic shower. Every segment corresponds to $5 R$ the mean free path of secondary particles.
is equally split into the secondary products, every collision halves it. The mean free path $(\lambda)$ between two interactions is indicated with a segment in figure 2.2. At an atmospheric depth $X$, every path counts $n(n=X / \lambda)$ branches, forming a shower of $2^{n}$ particles with a single energy of $\mathrm{E}_{0} \cdot 2^{-n}$. The maximum atmospheric depth ( $X_{\max }$ ) is achieved when the particles energy approaches $\mathrm{E}_{c}$.

$$
\begin{equation*}
E\left(X_{\max }\right)=E_{0} \cdot 2^{-n_{\max }}=E_{0} \cdot 2^{-\frac{x_{\max }}{\lambda}} \cong E_{c} \tag{2.5}
\end{equation*}
$$

[^27]From the previous equation the maximum shower depth can be obtained:

$$
\begin{equation*}
X_{\max } \cong \lambda \log _{2} \frac{E_{0}}{E_{c}} \tag{2.6}
\end{equation*}
$$

Changing the logarithm base

$$
\begin{equation*}
X_{\max } \cong \lambda \frac{\ln \frac{E_{0}}{L_{c}}}{\ln 2} \tag{2.7}
\end{equation*}
$$

An improved Heitler model, proposed by Rossi and Greisen, predicts precisely the longitudinal development of an electromagnetic shower, hence the total number of $\mathrm{e}^{ \pm}$ as a function of the atmospheric depth [115]. Some curves are illustrated in figure 2.3, where the parameter "s" specifies the first interaction point ( $s=0$ ), the shower maximum ( $\mathrm{s}=1$ ) and the its extinction ( $\mathrm{s}=2$ ).


The most distinctive characteristic between hadronic and electromagnetic showers is their lateral extension (Fig. 2.4). This property is due to the considerable transverse


Figure 2.4: The different spatial distribution of gamma and hadronic showers. The first is slim and loosely concentrated along the direction of the primary. The second one is irregular and spread out containing several electromagnetic sub-showers with divergent directions. (Adapted from [130])
momentum in hadronic interactions. The difference is evident above 100 GeV , where it represents one of the most powerful discriminator factors in the distinction between gammas and hadrons.

### 2.1.3 The Čerenkov light

Charged particles in electromagnetic cascades emit Čerenkov ${ }^{5}$ photons, if their energy exceeds the threshold value. The energy must be greater than $\mathrm{m}_{0} \mathrm{c}^{2} / \sqrt{1-n^{2}}$, where $m_{0}$ is the particle mass and $n$ is the refractive index. For an electron, which is the main Cerenkov emitter due to its low energy threshold, the minimum energy corresponds to $\sim 21 \mathrm{MeV}$ in air at sea level ${ }^{6}$. When the charged particles pass close to the air atoms, they can temporally polarize it in distinct modes tied to their speed, as illustrated in figure 2.5. The following reorientation of the electric dipoles induces light emission. As for the shock sound wave in the domain beyond Mach's number, the light wave front

(a) Slow particle

(b) Fast particle

Figure 2.5: Left: the air polarization induced by a slow moving charged particle. Right: the same effect due to a high speed particle.
propagates on a cone with the opening angle $\theta$. The angle is a function of the particle speed and the local atmospheric refraction index:

$$
\begin{equation*}
\cos \theta=\frac{1}{\beta n} \tag{2.8}
\end{equation*}
$$

where $\beta=\mathrm{v}_{\text {particle }} / \mathrm{c}$. Only particles that move with a velocity faster than the speed of light in the medium can radiate ( $\mathrm{v}_{\text {particle }}>\mathrm{c} / \mathrm{n}$ ). In figure 2.6, a graphical explanation of the angle $\theta$ is given. The light emission is described by the superposition of spherical waves using Huygens's principle. Only when the particle is faster than the electromagnetic wave induced by the polarization, a constant phase wave comes out. In the atmosphere, the refraction index is not constant, but it changes due to the air density variation, decreasing with altitude ( $h$ ). Applying the isothermal atmosphere approximation model, both pressure and density decrease exponentially with increasing

[^28]the altitude [135]. Consequently, the refractive index becomes:
\[

$$
\begin{equation*}
n(h)=1+n_{0} e^{-\frac{h}{h_{0}}} \tag{2.9}
\end{equation*}
$$

\]

where the fluctuations due to the air temperature and the wavelength of the radiation are neglected. According to equation $2.8, \beta$ changes along the shower's path, but continuously produces $\theta$ values inside an upper limit, which is a little more than $1^{\circ}$ in the lower atmosphere. The emitted electromagnetic waves generate a front that can be schematized in a disc, with a thickness of only few meters. This also explains the arrival time distribution at the telescope level, which is contained in $10 \mathrm{~ns}^{7}$.


Figure 2.6: Simple sketch of the Čerenkov effect. When a charged particle moves slower than the speed of light in the medium, the electromagnetic waves, initiated along its trajectory, are not superimposed (left side). Differently, when its velocity exceeds the local speed of light, a surface of constructive interference appears. This effect causes the light to be emitted under an angle $\theta$ (right side). (Courtesy of C. Fruck)

Considering the largest shower expansion point at 10 km , the light spreads mainly in an area of around $50000 \div 100000 \mathrm{~m}^{2}$ at the ground level. As for the shower development, even the generated Čerenkov light is roughly proportional to the primary energy. However, the flash is very faint, counting only $\approx 4000 \div 5000$ photons per GeV , so a density of 10 particles in a square meter for a primary $100 \mathrm{GeV} \gamma$-ray.
Another parameter that influences the photons density is the the zenith angle of observation. For high values, the atmosphere thickness along the primary photon path increases substantially. This changes the relative distance between the maximum development of the shower and the ground, spreading the light in a greater area (Fig. 2.7).

The original light spectrum is altered by the mediums transparency (Fig. 2.8). In fact, photons are attenuated by scattering and absorption proportionally to the crossed atmosphere. For instance, photons can be deflected by small air atoms, in a process called Rayleigh scattering. The photon intensity reduction can be expressed by the following equation [18]:

$$
\begin{equation*}
\frac{d I}{d x}=-I \cdot \frac{32 \pi^{3}}{3 N \lambda^{4}}(n-1)^{2} \tag{2.10}
\end{equation*}
$$

where N is density of scattering particle and $\lambda$ is the Čerenkov photon wavelength.

[^29]

Figure 2.7: The total number of Čerenkov photons as a function of $\gamma$-rays' primary energy for several zenith angles $\left(0^{\circ}, 25^{\circ}, 40^{\circ}, 50^{\circ}\right.$ and $70^{\circ}$ ). The La Palma observation level, with its magnetic field, was chosen. The average total number of photons depends on zenith angle and increases with the primary energy. (Image credit: D. Sobczyńska)

The UV range is the most affected, because the cross section is tied to the mutual wavelength $\left(1 / \lambda^{4}\right)$. Another important scattering is called Mie scattering and it is due to the dispersion on aerosols and clouds. Typically its contribution is modest, but can become important during poor atmospheric conditions. On the other side, the absorption processes act below $\sim 300 \mathrm{~nm}$ with the ozone $\left(\mathrm{O}_{3}\right)$, the oxygen $\left(\mathrm{O}_{2}\right)$ and the nitrogen ${ }^{8}\left(\mathrm{~N}_{2}\right)$. In the infrared region, the absorption is mainly due to the rotational and vibrational transitions of water $\left(\mathrm{H}_{2} \mathrm{O}\right)$ and carbon dioxide $\left(\mathrm{CO}_{2}\right)$ molecules.
In air, the spectrum peaks around 330 nm , rather close to the ultraviolet and blue region. Consequently, one attempts to maximise the Čerenkov light sensitivity of detectors in the interval between 300 and 450 nm .


Figure 2.8: The differential spectrum of Čerenkov photons, calculated for different energies, before (continuous lines) and after (dotted lines) atmospheric absorption as a function of wavelength. (From [131])

[^30]
### 2.2 The IACT technique

The IACT telescopes are furnished with a large reflective surface, which focuses the Čerenkov light into a camera covered by photosensors. The photons, yielded at different heights, hit the mirrors with various angles, ending their travel in diverse PMTs. Hence, the light, converted in electrical signals, forms an image of the EAS in the camera plane. The conversion of a real three dimensional air shower into a projection on a flat surface is the base of the IACT technique (Fig. 2.9). Then the technique studies the reconstructed images of the EASs.
Photons emitted at the upper part of the shower have small Čerenkov angles, so they


Figure 2.9: Left: an illustration of the Čerenkov light pool, initiated by a primary $\gamma$-ray coming from an astronomical source (e.g. a Supernova remnant), which illuminates an array of telescopes. Right: the subsequent creation of the shower imaging in one telescope (bluish ellipse). Along the shower longitudinal propagation, the light is emitted with different angles (coloured lines) and afterwards focussed in distinct photosensors. In the particular presented case of an electromagnetic shower, the shape is elliptical, but in general it could be irregular. The contour lines indicate the light intensity. (Adapted from [130])
are focused onto a region close to the camera centre. The others, generated at the end, have a large angles and are therefore mapped further away from the camera centre.

This method allows to study the main features of particles that do not reach the ground level, through the information that is carried by the Čerenkov light. The morphology of the images is used first to distinguish between electromagnetic, hadronic or muonic showers, then to characterize the event. Considering the particle cascades in the space-time ${ }^{9}$ mathematical description, they appear with various geometries due to the internal processes involved. The main differences and how they affect the image parametrization are listed below.

* The hadronic showers have the broadest lateral distribution due to the high transverse momentum of the secondary interactions. This results in a wider width parameter, which is the half width of the minor axis of the shower projection. Moreover, they are also subject to considerable fluctuations in the shower development, generating a lot of irregularities.

[^31]* The hadronic showers are the most extended. In fact, the air radiation length of hadronic particles is higher than the photons one. The longitudinal evolution is calculated with the variable length, which is the second moment of the charge distribution along the major axis of the shower image.
* Cosmic rays from the same source, deflected by the magnetic fields they have traversed, hit the atmosphere at different angles. The induced Čerenkov photons reach the telescope isotropically from everywhere, while gammas travel along the pointing direction. This property is transferred to the image orientation. The angle between the image major axis and the line passing through its core and the source nominal position on the camera is called alpha. For events induced by $\gamma$-rays from the source the telescope points at, it is close to zero: i.e. the major axis of the camera image points to the camera centre, where photons coming parallel to the telescope axis are focused.
* The spread arrival time of the photons, in the camera plane, changes depending on the nature of the shower component: $1 \div 2 \mathrm{~ns}$ for the muonic component, $2 \div 3 \mathrm{~ns}$ for the electromagnetic one and $10 \div 20 \mathrm{~ns}$ for the hadronic one. The root mean square of the arrival times, taken for all the pixels associated to the shower projection, is calculated (time RMS).
* Another important timing parameter is time gradient, which estimates how much the arrival time varies along the major image axis. For an electromagnetic cascade the timing gradient is related to the longitudinal development, while it is not so evident for hadrons, which suffer larger shifts due to to the lateral expansion.

These parameters are used in the gamma-hadron separation ${ }^{10}$ procedure. This technique is crucial to reduce the huge hadronic background (for weak sources roughly one good event every ten thousand) and to extract the characteristics of the primary $\gamma-$ rays.
There are still other parameters that are utilized for the event reconstruction.

* A preliminary estimation of the primary particle energy is calculated with size. It is the total number of photoelectrons counted in the shower image. For the same energy, the Čerenkov light emitted by hadron-induced showers is smaller compared to that produced in a gamma air showers. As explained in subsection 2.1.2, only a fraction of the original primary hadron energy is converted into the electromagnetic component.
* The image concentration is dug out of the variable $\boldsymbol{\operatorname { c o n }} \boldsymbol{c}(\boldsymbol{n})^{11}$. It is defined as the ratio between the charge contained in the $n$ brightest pixels and the total image size.
* The events that occur at very high impact parameters (distance between the shower axis and the point of detection) could be only partially recorded. The leakage is the portion of equivalent photoelectrons contained in the outermost ring of the camera per total image size. This parameter is important, because it estimates the fraction of signal lost because of too large impact parameter.

[^32]* The shower maximum and its impact parameter is obtained by mean of the dist parameter. It is the distance between the image centre of gravity (the weighted average position of charge in the image) and the position of the source in the camera plane.
Most of these parameters, except the timing ones introduced recently by the MAGIC collaboration [37], are commonly used in the IACT experiments. They are called Hillas parameters, from the name of its inventor Anthony M. Hillas [72]. Some of them are illustrated in figure 2.10


Figure 2.10: Representation of the Hillas parameters width, length, dist and alpha in a recorded event. (Adapted from [111])

The air shower image induced by an electron is similar to that of a photon. Only the orientation respect to the pointed source could change. This should be considered as an isotropic background, which is not possible to eliminate at very low energies.

### 2.3 The MAGIC analysis

The recorded shower projections are examined by the MAGIC analysis software tools. The main framework is called MARS (MAGIC Analysis and Reconstruction Software), an object oriented program written in C++ and developed in the ROOT environment [99]. It is composed of several sub executables, each realized for a specific commitment in the analysis chain (Fig. 2.11). The logical flow of data is seen in:

* Callisto: the pulses generated by the PMTs are calibrated and converted in photoelectrons (2.3.1).
* Star: in each telescope the shower image is first cleaned by the noise and afterwards parametrized by image parameters (2.3.2).
* SuperStar: the information from both telescopes are merged and the stereo parameters are extrapolated (2.3.2).
* Melibea: the $\gamma /$ hadron separation is performed with the help of the random forest algorithm ${ }^{12}$ outputs. The energy is estimated in the selected events (2.3.3).
* Odie: the signal excesses are estimated and the significance is determined in a specific source position (2.3.4).

F Fluxlc: the differential energy spectrum and the light curve are produced (2.3.4).

[^33]

Figure 2.11: Flow diagram of the MAGIC standard analysis chain. (© F. Dazzi)

### 2.3.1 Signal extraction and calibration

The two telescopes use different readout electronics (4.6) and consequently distinct algorithms to extract the signal. The extraction procedure provides essential quantities, as charge, amplitude and signal arrival time, after the pedestal ${ }^{13}$ subtraction. MAGIC-I applies a cubic spline extractor in a sampled range of 50 time slices ${ }^{14}$, whereas MAGICII a sliding window algorithm in 80 slices.
The first one interpolates the pulse with a cubic spline curve [33]. The maximum of the obtained function represents the amplitude, while the charge is calculated performing the integral in a fixed window centred around the signal peak. The arrival time is defined at the rising edge at the voltage level of half maximum.
In the sliding window extractor, a routine searches the time range with a predefined dimension of 4 ns , where the signal integral is maximized. The peak inside the selected interval provides the amplitude, while its weighted average corresponds to the arrival time. The pedestal is estimated from the first 16 time slices of the readout window.

The Čerenkov light, collected by the PMTs, is converted into electrical signals that can be characterized by voltage measurements. A conversion factor is mandatory to connect the two quantities, photons and charge. Both telescopes are equipped with a calibration box in the middle of the reflector dish, which can emit known light pulses (4.7). Dedicated runs, so-called calibration runs, trigger only light flashes generated by the calibration system. These short flashes illuminate the whole camera with a constant intensity, so it is possible to study the behaviour of every single photosensor and calculate the proper conversion factor. Its value is constantly updated during datataking through interleaved calibration events ${ }^{15}$, activated at a frequency of 25 Hz . This allows to keep under control the fluctuations of the electronic chain.

[^34]The first step is to move from incident photons to photoelectrons, by mean of the PMT quantum efficiency. Then, the method called $\boldsymbol{F}$-Factor is applied to correlate the charge. It is based on the fact that the photoelectrons flux excess noise, introduced by the $P M T$, is proportional to the generated photoelectrons [98]. In general it can be expressed as:

$$
\begin{equation*}
F=\frac{\left.(\text { Signal } / \text { Noise })\right|_{\text {input }}}{\left.(\text { Signal } / \text { Noise })\right|_{\text {output }}} \tag{2.11}
\end{equation*}
$$

namely a quantification of the additional noise introduced by the device under test. Assuming that the original photoelectrons distribution is Poissonian with mean $N$, the measured output charge, in $F A D C$ counts multiplied time (proportional to the voltage multiplied time) returns a mean $\langle Q\rangle$ with a spread $\sigma$. The equation 2.11 becomes

$$
\begin{equation*}
F=\sqrt{N} \frac{\sigma}{\langle Q\rangle} \tag{2.12}
\end{equation*}
$$

where $F$ is an intrinsic feature of each $P M T$ measurable in the laboratory before the final installation. On the other side, $\langle\mathrm{Q}\rangle$ and $\sigma$ are computed from the calibration runs, hence the conversion factor is

$$
\begin{equation*}
C=\frac{N}{\langle Q\rangle}=F^{2} \frac{\langle Q\rangle}{\sigma^{2}} \tag{2.13}
\end{equation*}
$$

where the relation 2.12 is used. Once the parameters to equalize the electronics are available, the recorded event can be nicely extracted and calibrated.

### 2.3.2 Image cleaning

The cleaning stage reconstructs the shower projection, rejecting all the pixels that do not contain information about the shower itself. All the pixels, whose charge is related to fluctuations, NSB (Night Sky Background) or stars, are excluded.
It is fundamental to optimize this procedure as much as possible to intercept the all spurious events that can be confused with good data. This field is improving constantly, mainly at the very low energies, where the shower projection shape is not well defined, because it involves few pixels as well as the $N S B$ or star images. There are several cleaning tools, but the most utilized are currently two: the standard image cleaning and the sum image cleaning.

In the standard image cleaning, an image generated by an $E A S$ is assumed to be composed of a central part, in which a considerable fraction of the charge is concentrated, and an adjacent ring with typically less photoelectrons. Two charge thresholds are required to sort out the image core and the boundary pixels. The core must be formed by at least two neighbour pixels above the first threshold ( $T h_{\text {core }}$ ). Boundary pixels have first to be in contact with a core pixel, then to exceed the second threshold ( $T h_{\text {boundary }}$ ), which is smaller than $T h_{\text {core }}$.
The arrival time information allows to relax the charge thresholds and to reconstruct dim Čerenkov flashes, without loosing in sensitivity (Fig. 2.12). Two new constraints are implemented: a) the arrival time spread of core pixels must stay inside a restricted window, called TimeOffset; b) the time difference between a boundary pixel and its neighbour one must be smaller than a fixed variable, called TimeDifference [37].

Besides the standard image cleaning, there is the innovative sum image cleaning, which improves the sensitivity by $15 \%$ below 150 GeV . It relies on the same concept of core and boundary pixel, but further constraints are added, forcing to a stringent


Figure 2.12: Left: the event before the cleaning. Centre: the event arrival time expressed in time slices. Right: the same event after the standard timing cleaning. The ellipse and the associated lines represent some image parameters.
timing and new topological rules. Core pixels must be arranged in a close compact configuration of $x$ units $(x N N$, where $x$ is $2 \div 4)$. The charge of each core pixel is clamped at a certain level $\left(T h_{\text {clip }}\right)$ to get rid of the effect of the $P M T$ afterpulses ${ }^{16}$, and then the total charge of the $x N N$ group is calculated. The second selection step is fulfilled if the sum exceeds another threshold $\left(T h_{\text {sum }}\right)$. The new constraints are expressed as a functions of $T h_{\text {core }}$,

$$
\begin{align*}
T h_{\text {sum }} & =S_{\text {sum }} \cdot x \cdot T h_{\text {core }}  \tag{2.14}\\
T h_{\text {clip }} & =C_{\text {clip }} \cdot \frac{T h_{\text {sum }}}{x} \tag{2.15}
\end{align*}
$$

where $S_{\text {sum }}$ and $C_{c l i p}$ are new parameters telescope independent.
Also in this case the timing constraints are considered and well tuned for each multiplicity. They are even a factor 5 more stringent than the limits imposed in the standard cleaning.

In table 2.1 the used values in both methods are listed. The choice of the parameters is driven by the compromise between the efficiency detection of low energy events and the introduction of noise, which can degrades the image parametrization and the subsequent reconstruction.

The graphical event representation is then parametrized with the Hillas parameters, explained in the previous section (2.2). Up to this stage the analysis chain runs independently for each telescope. When pairs of events recorded by the two telescopes are matched, the three dimensional stereo parameters are computed. In this way, the same shower is traced by two projections obtained from different points of view.
One of the most important is MaxHeight, namely the height of the shower maximum, which depends on the primary energy. MaxHeight is indeed very helpful in the following $\gamma /$ hadron discrimination at low energies.

### 2.3.3 Event classification

From this moment on, a Random Forest $(R F)$ algorithm is executed in a dedicated program, called Coach. By analysing the position of the event in multi-dimensional space, the $R F$ estimates the hadronness variable, which represents how much the primary particle is hadron-like [34]. The algorithm learns how to classify events depending on

[^35]| STANDARD IMAGE CLEANING |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Telescope (name) |  | $\mathbf{T h}_{\text {core }}$ (phe) | $\mathbf{T h}_{\text {boundary }}$ (phe) | TimeOffset (ns) | TimeDifference (ns) |  |
| $M A G I C-I I$ |  | 6 | 3 | 4.5 | 1.5 |  |
|  |  | 9 | 4.5 | 4.5 | 1.5 |  |
| SUM IMAGE CLEANING |  |  |  |  |  |  |
| $\begin{gathered} \text { Tel. } \\ \text { (name) } \end{gathered}$ | $\begin{gathered} \hline \mathrm{xNN} \\ (\mathrm{Nr} .) \end{gathered}$ | $\mathrm{Th}_{\text {core }}$ (phe) | Th $_{\text {boundary }}$ (phe) | $\mathrm{C}_{\text {clip }} \mathrm{S}_{\text {sum }}$ | $\begin{gathered} \hline \text { TimeOff. } \\ (\mathrm{ns}) \\ \hline \end{gathered}$ | TimeDiff. (ns) |
| M-I | 2NN | 4 | 3 | $2.20 \quad 1.8$ | 0.9 | 1.5 |
|  | 3NN | 4 | 3 | 1.051 .3 | 1.2 | 1.5 |
|  | 4NN | 4 | 3 | $1.05 \quad 0.7$ | 1.9 | 1.5 |
| M-II | 2NN | 7 | 4 | $2.20 \quad 1.8$ | 0.9 | 1.5 |
|  | 3NN | 7 | 4 | 1.051 .3 | 1.2 | 1.5 |
|  | 4NN | 7 | 4 | $1.05 \quad 0.7$ | 1.9 | 1.5 |

Table 2.1: The parameters for the standard and the sum image cleaning.
their nature, by training on Monte Carlo and real data samples. The hadronness spans between 0 and 1, representing a $\gamma$-like or a hadron-like event respectively (Fig. 2.13(a)). Melibea applies the resulting $R F$ matrices to the recorded data with the aim to reject the hadronic component of the background. A typical hadronness cut, used to reject most of the hadrons (mainly protons), is 0.1 (Fig. 2.13(b)). This cut is optimized by


Figure 2.13: Left: the classical output plot from the random forest algorithm. Gamma-ray events (blue area) are peaked around zero, whereas the hadronic ones (black area) increase the rate approaching the unit. In this distribution the reconstructed energy is above 100 GeV . (From [26])
Right: the fraction of surviving background events with different cuts in the hadronness parameter performed in the stereo analysis of Crab Nebula. (Adapted from [40])
using the quality factor, which is expressed by the relation

$$
\begin{equation*}
Q_{\text {factor }}=\frac{N_{\gamma}}{\sqrt{N_{p}}} \tag{2.16}
\end{equation*}
$$

where $N_{\gamma}$ and $N_{p}$ are respectively the fraction of gammas and protons passing the selection cut.

Once $\gamma$-like events are selected, their energy is currently ${ }^{17}$ estimated by using lookup tables based on Monte Carlo simulations. The creation of the look-up tables assumes that, at a given zenith angle, the light distribution at the ground is correlated with the parameters size, impact parameter and MaxHeight. The look-up tables are prepared independently for each telescope, then the final energy value is found as their weighted average.
It must be underlined that the estimated energy $\left(E_{\text {est }}\right)$ is not equal to the real energy ( $E_{\text {true }}$ ). Their discrepancy is determined by the relation 2.17.

$$
\begin{equation*}
D\left(E_{\text {est }}\right)=\frac{E_{\text {est }}-E_{\text {true }}}{E_{\text {true }}} \tag{2.17}
\end{equation*}
$$

The $D\left(E_{\text {est }}\right)$ distribution can be fitted with a Gaussian function, whose $\sigma$ represents the energy resolution. The position of the peak is the energy bias, which should be as close as possible to zero.

The source position in the camera plane can be calculated in two ways: a) as crossing point of the main axes of the two single telescope images; b) in terms of a new parameter called Disp, defined as the angular distance between the image centre of gravity and the reconstructed source position along the major axis. Disp is calculated by means of a parametrization of the shower elongation (width/length). Currently this method is enhanced by taking advantage of the $R F$ algorithm in the computation of the space parameters. In the analysis of mono data, this updated method is called Disp RF.
For stereo observations, if the Disp $R F$ values, estimated in each telescope separately, agree inside a certain threshold, then the event is accepted and the final direction will be the weighted average of all of them, otherwise it is rejected. This procedure is called stereo Disp RF.

The Disp RF method allows to introduce a new important image parameter, so called $\theta^{2}$. It is defined as the square of the angular distance between the reconstructed and the catalogue position of the source on the camera plane. For $\gamma$-like events, its distribution is concentrated at small values, whereas it is flat for hadron-like images.

### 2.3.4 Source detection and characterization

This is the final step of a basic analysis. After the calibration, the cleaning and the classification of the recorded data sample, the $\gamma$-ray events are accumulated to achieve sufficient statistics to characterize the observed source. There are several tools to compute the celestial object properties. The principal ones are Odie, which calculates the parameter $\theta^{2}$, and Fluxlc for the energy and intensity spectrum.

The estimation of the $\gamma$-ray signal from the reconstructed source position is done through the distribution of alpha and $\theta^{2}$ parameters, which should peak at very small values (Fig. 2.14(a)). Hence, they indicate the place where there is the $\gamma$-ray emission, defining the signal region. The alpha analysis is typically applied for mono data of point-like sources with known positions, whereas in the case of stereo data the $\theta^{2}$ computation shows better performance. Most of its power, comes from the utilization of parameters, which do not depend on an a priori known source position.

The $\theta^{2}$ distribution is shaped by the overlap of $\gamma$-rays, peaked around zero, and the flat spectrum of the surviving hadrons ${ }^{18}$. In the signal region the number of events $\left(\mathrm{N}_{\text {ON }}\right)$ that have passed the cut selections are counted. There are still some hadron-like

[^36]events that have survived the previous discriminating stages, and must be accounted. The same analysis, applied to the off data sample ${ }^{19}$, allows to get a good approximation of the background events ( $\mathrm{N}_{\text {OFF }}$ ) in the signal region. The estimated number of $\gamma$-rays excesses is:
\[

$$
\begin{equation*}
N_{\gamma}=N_{O N}-\alpha N_{O F F} \tag{2.18}
\end{equation*}
$$

\]

where $\alpha$ is a time normalization factor. In order to exclude that the signal excess is due to background fluctuations, the significance $(S)$ is compute by using the Li \& Ma formula [93]:

$$
\begin{align*}
S= & \sqrt{2}\left\{N_{O N} \cdot \ln \left[\frac{1+\alpha}{\alpha}\left(\frac{N_{O N}}{N_{O N}-N_{O F F}}\right)\right]+\right.  \tag{2.19}\\
& \left.N_{O F F} \cdot \ln \left[(1+\alpha)\left(\frac{N_{O F F}}{N_{O N}-N_{O F F}}\right)\right]\right\}^{\frac{1}{2}}
\end{align*}
$$

It is commonly assumed that a detection to be publishable should have at least a significance of $5 \sigma$.
An important index of the telescope performance is expressed by the sensitivity, defined as the minimum $\gamma$-rays flux, which returns $5 \sigma$ significance in 50 h of observation. Using a Gaussian approximation of the equation 2.20 , it can be expressed as:

$$
\begin{equation*}
\text { Sensitivity }(t)=\sqrt{\frac{t}{50}} \frac{N_{\gamma}}{\sqrt{N_{O F F}}} \tag{2.20}
\end{equation*}
$$

where $t$ is the time of observation.


Figure 2.14: Left: an example of $\theta^{2}$ plot obtained from Crab Nebula observed in stereo mode. The signal is marked with black points, while the background area is coloured in red. The $\theta^{2}$ cut is shown with the dashed blue vertical lines. (Adapted from [40])
Right: an example of sky map of the Crab Nebula. The position of the Pulsar Wind Nebula is marked by the black plus sign and the angular resolution is indicated by the circle. (Adapted from [32])

Once a gamma signal is detected, the source morphology can be studied by producing sky maps, which show the arrival directions in sky coordinates (RA \& DEC) (Fig. 2.14(b)). To take into account the pointing uncertainty, the sky map is smoothed with a Gaussian function with $\sigma$ equal to the angular resolution.

[^37]The differential energy spectrum is calculated in Fluxlc with the following formula

$$
\begin{equation*}
E_{\gamma}^{d i f f}=\frac{d N_{\gamma}}{d E_{e s t} \cdot A_{e f f} \cdot d T_{e f f}} \tag{2.21}
\end{equation*}
$$

where $\mathrm{A}_{e f f}$ is the effective collection area and $\mathrm{T}_{\text {eff }}$ is the effective observation time. The effective area represents the geometrical region, corrected by the detection efficiency, in which a $\gamma$-ray triggers the telescope. The effective observation time is the temporal interval, during which the telescope is recording data, excluding the dead time of the detector.

Finally, the true energy is derived by the estimated one through an unfolding procedure. Assuming to know the telescope response function, it is possible to extract the true energy from the measured one by mean of a conversion matrix.
In addition, Fluxlc allows to produce light curves, namely the integral $\gamma$-ray flux as a function of time for energies larger than a certain value.

### 2.3.5 Data-taking modes

The MAGIC experiment is composed of two telescopes that can operate independently ( mono data-taking) or synchronously (stereo data-taking). The first mode is typically used either when a telescope is under maintenance, while the other can take normal data, or when the performance of both detectors must be compared. The tracking of two distinct sources at the same time is never enforced, because the main target of MAGIC is the study of astronomical processes at very low energies, where the stereoscopic data-taking shows higher performance. In fact, the primary particle direction, the energy and in general the event reconstruction are more precise, because the same shower is registered from different point of views. Also the efficiency of the background rejection is much better. This theory is presented in detail in chapter 6.

In MAGIC there are two observation modes, which determinate the estimation procedure of the surviving background. To be sure that the observed region of the sky emits a signal, the number of recorded events is compared with the one extracted tracking a dark zone, where no signal is expected. The data set is accumulated in different moments, first pointing to the source and subsequently to a nearby darkpatch ${ }^{20}$, trying to match the same outline conditions. This mode is called ON/OFF mode.
Currently, the standard observations are performed in the so-called wobble mode. The pointing source position is set $0.4^{\circ}$ away from the camera centre. This allows to get simultaneously the signal and the background estimations. As show in figure 2.15, the background is estimated at symmetrical offsets from the telescope pointing direction. In order to avoid systematic bias due to detector inhomogeneities, every 20 minutes the wobble position is swapped.

The MAGIC telescopes can operate only during dark nights, when the faint Čerenkov flashes are not dominated by other sources of photons in the optical wavelengths. In addition, the photosensors are so sensible, that the full moon is enough to saturate them. Nevertheless, the electronics amplification has been conceived to take data even with moderate moon light.
Another essential condition for data tacking is good weather. The camera electronic cannot be exposed to high humidity and the telescope structure cannot be moved under strong wind. Finally, the presence of clouds or calima ${ }^{21}$ in the sky increases the Mie

[^38]

Figure 2.15: Representation of wobble mode observation in MAGIC-II. The source is placed at the green circle, whereas the yellow ones indicate the background regions. The gray line connects the source and the antisource, which are swapped every 20 minutes. Differently, the blue circle shows the source position when the ON/OFF mode is activated. (C) F. Dazzi)
scattering and affects the light collection.

## Low size events morphology


#### Abstract

In the energy domain between a few GeV and 50 GeV , gamma astrophysics is still full of uncertainties, so it needs the development of new strategies. A high sensitivity and a low energy threshold are key parameters to operate in a spectral region where the overlapping with satellite experiments is essential. MAGIC has been designed with this clear objective in mind and nowadays further investigations are still ongoing. Technological innovations in the field of light collection and light conversion can favour the performance of the telescope, but it is also important to study the main features of the Cerenkov radiation generated by low energy particles and its interaction with the detector. The event's morphology and its charge distribution at the camera level should be understood to optimize the selection algorithms and the shower reconstruction. In this chapter, a general and basic introduction to this problem area is presented.


### 3.1 Physics motivations

There are strong scientific motivations to cover the gap between the space-based and ground-based observations, extending the $I A C T$ technique down to 10 GeV .

Gamma-rays, emitted by extragalactic sources, can interact with diffuse low energy photons of the EBL (Extragalactic Background Light), which is an evolving isotropic radiation due to stars and dust that fills the entire intergalactic space. Electron pairs are produced in the interaction, so the original gammas disappear. The interaction probability increases with distance and energy, so the observed spectrum of distant sources at high energies is depleted respect the original one [57]. Assuming to know the $E B L$ spectral density, the attenuation factor represents a direct estimation of the source distance. However, sources at very high redshift are only accessible at low energies, where the flux suppression in not dominating. This effect strongly limits the study of a large amount of $A G N s$, which lie at high redshift. At low energies, below 50 GeV , the Universe is expected to become more transparent and distant sources can be detected. This opens an important window to a further understanding of the socalled $\gamma$-ray horizon.
In addition, the analysis of many distant sources allows to reduce the substantial uncertainties of the current $E B L$ models, providing a better understanding of the stars and galaxies formation and their evolution [83].

It is commonly assumed that about $23 \%$ of the energy density in the Universe consists of an unknown, non-luminous, and non-baryonic matter called dark matter ( $D M$ ). According with particle physics theories beyond the Standard Model, as Supersymme$\operatorname{try}{ }^{1}(S U S Y)$ and multidimentional models, the best candidates for the $D M$ are the WIMPs (Weakly Interactive Massive Particle) [10]. These particles are supposed to be massive (between some GeV to 1 TeV ), electrically neutral, stable ${ }^{2}$ and could annihilate or decay into $\gamma$-rays. Among them, a good candidate is the supersymmetric neutralino $(\chi)$, which is the lightest supersimmetric particle.
Since the expected annihilation flux of $\gamma$-rays is proportional to the $D M$ density, the $I A C T$ telescopes can search signatures of the $D M$ particle existence observing regions of the sky with foreseen high $D M$ density as the Galactic Centre, Dwarf spheroidal satellite galaxies of the Milky Way, and galaxy clusters.

Some models predict an energy dependence of the speed of photons due to quantum gravity fluctuations of vacuum [87]. Cosmological $\gamma$-rays emitted simultaneously, but of different energy, should arrive at the Earth's atmosphere in different moments.
In order to be sensitive to this infinitesimal effect in the GeV domain, two ingredients are absolutely mandatory: a considerable distance to cover and a strong energy variability. Obviously the main candidates are rapidly flaring distant AGNs and GRBs that appear typically at large redshift [22]. Unfortunately, only detectors with a low energy threshold have the chance to reveal them, because of the energy cut-off caused by the $E B L$ absorption.

Another argument that engenders interest are the Blazar jets, very powerful nonthermal emissions of $A G N s$ that expand in the surrounding medium. The emitted electromagnetic radiation spreads over a huge interval of the energy spectrum, so it is a matter of study for many experiments with different detectors. How the energy of the jet is converted into radiation and which is the working of the central engine are still not fully understood. There are controversial models that predict a pure leptonic or hadronic $\gamma$-ray emission and even some innovative hybrid explanations. Disentangling the various flux contributions to the emission will help to understand the production and acceleration mechanisms [20].
By lowering the $I A C T$ energy threshold, it is possible to extend the spectrum of the detectable $\gamma$-rays emitted by Blazars and to measure the emission evolution in a wider redshift range.

In the $\mathrm{GeV} \div \mathrm{TeV}$ range, Supernova Remnants are likely the main sites for the cosmic ray acceleration [17]. It is quite evident that the electrons are accelerated to TeV energies, but the proton case is still not so obvious, as much as the answer to the origin of the cosmic rays in this domain is unresolved. More sensitive measurements would open the activity to search the two components of the $\gamma$-ray spectrum, one linked to the leptonic channel and the other to the hadronic one.

A special attention is dedicated to Pulsar physics in the GeV domain. The best qualified models propose different cut-off energies to describe the emission from the neutron star. These breakpoints are, again, in the energy range that is presently difficult to access.
A low energy threshold is crucial to have an overlap with satellite detectors, which allows to compare the measurements of the tail of the Pulsar spectra. Some important studies are just now in progress, as reported in more detail in subsection 5.1.3.

[^39]
### 3.2 Low energy atmospheric air showers

The physics principles, that describe the extended air shower at very low energies $(10 \div 50 \mathrm{GeV})$, still remain the same as for higher energies. The difference lies in the available amount of energy that gets converted crossing the atmosphere. The cascades die out relatively soon ${ }^{3}$, reaching their maximum development around a depth of $180 \div 240 \mathrm{~g} / \mathrm{cm}^{2}(11 \div 12 \mathrm{~km}$ a.s.l. $)$, thus very far away from telescopes as MAGIC, installed at $\sim 2000 \mathrm{~m}$ of altitude. Adding the fact that the energy threshold for the Čerenkov photons production is double in the upper layers of atmosphere $(35 \div 40 \mathrm{MeV}$ for electrons), the number of emitted photons is very small. Furthermore, the higher is the altitude, the lower is the refraction index and the smaller is the Cerenkov angle, so the generated photons are strongly collimated along the charged particles trajectory.
In the case of showers initiated by $\gamma$-rays, which have a modest transversal development, the main consequences are small shower projections (small size) and a limited number of triggered events at large impact parameters.

These three parameters, energy, size and impact parameter, have been studied to reveal their correlation in low energy $\gamma$-rays, simulating the MAGIC-II telescope with the following conditions: mono ON/OFF data, standard trigger $4 \mathrm{NN}^{4}$ and size $<250$ phe. Up to 200 GeV , the energy and the size are linearly proportional, while beyond this value some Cerenkov light components with large emission angles with respect to the pointing direction, are focused outside the camera and hence lost (Fig. 3.1(a)). The curve's trend starts to become flatter.
Figure 3.1(b) shows that the mean impact parameter as a function of energy lies at a


Figure 3.1: Left: the correlation between the energy of simulated $\gamma$-rays and the size of the projections in the camera plane. The black crosses show the average points. Centre: dependency of the gamma energy with the impact parameter. Right: the size as a function of the impact parameter. (Images credit: E. Prandini)
constant value of 120 m up to 100 GeV . This corresponds to the Čerenkov pool border, a thin ring where the photons are concentrated, because a fraction of the light emitted at the beginning of the cascade with small angles meets the following emissions at larger angles. The whole blob spans between 50 m and 150 m and only at higher energies the contribution close to the shower axis ( $50 \mathrm{~m}<$ impact parameter $<100 \mathrm{~m}$ ) disappears, giving way to some very distant events. This is due to the long longitudinal development of energetic showers.
The last illustration, size versus impact parameter, confirms again what has been explained previously (Fig. 3.1(c)). The blob is slightly more smeared, still in agreement

[^40]with the size spread presented in figure 3.1(a).
The CoG (Centre of Gravity) plot, obtained with the same set of Monte Carlo data, shows an interesting structure (Fig. 3.2), which is a consequence of the plots 3.1. There is a hot ring around the camera centre, which points out that most of the events at low energies are concentrated in a thin doughnut shaped region. This suggests some interesting technical conclusions: a) it is fundamental the maintenance of this portion of both camera and trigger; b) the trigger design and its algorithm should be optimized at least for this region; c) in case the trigger area could not be large (limitations due to the cost, space, weight, etc...), it has to be restricted to this ring.

The thickness of the $C o G$ ring in-


Figure 3.2: The $C o G$ of events with size less than 250 phe. The simulated conditions are: ON/OFF mono data set using the MAGIC-II camera and standard trigger multiplicity 4NN. (Image credit: E. Prandini) dicates that in average the amount of angles involved in the light emission is limited, as expected by the fact that both the lateral and the longitudinal shower developments are relatively narrow. Even the spread of the Čerenkov light angle, due to the refractive index variation, extends in a tiny interval because most of the production occurs in a quite thin layer of the atmosphere. The recorded image size is small, containing typically less than $70 \div 80$ phe distributed in few pixels. The projection's reconstruction becomes problematic and the event selection inefficient. The orientation and the concentration of the images are degraded and the parametrization described in sections 2.2 and 2.3 is no longer an effective tool. Finally, the energy and the angular resolution deteriorate, being dominated by statistical fluctuations, as it happens in a calorimeter ${ }^{5}$.
In this energy domain it is crucial to consider the photon arrival time on neighbouring pixels and benefit from its small dispersion. The typical difference is less than 2 ns , so the reflective surface, the photosensors and the electronic chain of an IACT telescope should be designed to keep the isochronism well under this limit.

Another influential factor, in the regime of few GeV , is given by the background scenario. The cosmic hadrons, which are the main background source above 100 GeV , are less influential, because the momentum of the hadronic and muonic components approach the Čerenkov production threshold. Below 30 GeV the hadronic contribution is negligible and in turn the cosmic electrons continue to play an important role.
Unfortunately, there is a physical limit in the IACT technique. The electromagnetic showers initiated by primary electrons are similar to those due to $\gamma$-rays, independently of the energy. Even the electromagnetic component, generated by the neutral pion decay in the proton-nucleon interaction, presents the same characteristics. This kind of $E A S$ cannot be distinguished by the current IACT telescopes and in principle it cannot be removed, contributing to limiting the flux sensitivity. However, for point-like sources and telescopes with a good angular resolution, a fraction of this background can be

[^41]rejected reducing the timing gate of stereo trigger (see subsection 6.2.1). Nevertheless, simulation studies predict an electron trigger rate of few Hertz, for a telescope as MAGIC that can operate at 30 GeV , which is only one order higher than the gamma one [46].

Another intrinsic limitation is due to the action of the geomagnetic field on low energy showers. Sometimes charged particles get trapped in the atmosphere, because the Lorentz force deflects them in the East-West direction [47]. Therefore, the information provided at the telescope level is further reduced.

### 3.3 Event features at camera level

For a successful event detection and a subsequent image analysis, one needs to measure a minimum number of signal photoelectrons in at least some camera pixels. The number of photoelectrons produced in the PMTs photo-cathode, is proportional to the number of collected photons. Considering again the theory presented in subsection 2.1.2, it is possible to calculate approximately the number of photons involved, for instance, in a $\gamma$-ray of $\sim 20 \mathrm{GeV}$. An electromagnetic shower generates $2^{n}$ particles with a single energy of $\mathrm{E}_{0} \cdot 2^{-n}$, until they reach the critical energy of $\sim 83 \mathrm{MeV}$ (Eq. 3.1).

$$
\begin{align*}
E_{0} \cdot 2^{-n} & =E_{c}  \tag{3.1}\\
20 \cdot 10^{9} \mathrm{eV} & =2^{n} \cdot 83 \cdot 10^{6} \mathrm{eV} \\
n & =\log _{2} 241=7.91
\end{align*}
$$

The cascade consists of $\sim 241$ particles and it propagates to a depth equivalent to $7.91^{6}$ interactions. One third of these particles are photons, whereas the rest are electrons and positrons. Only the latter, roughly 160 relativistic charged particles, can produce Čerenkov light.
Assuming to be in saturation ${ }^{7}$, roughly $4000 \div 5000$ Čerenkov photons are produced per GeV , so a $\gamma$-ray of 20 GeV emits roughly 100000 photons [78]. This light spreads at the telescope level in a huge area of $\sim 100000 \mathrm{~m}^{2}$, namely one photon every square metre. For instance, a telescope like $M A G I C$, with a reflective area of $\sim 236 \mathrm{~m}^{2}$ and a local reflectivity around $80 \%$, can collect something like 190 photons. In case the light is not well focused or some mirrors are damaged, the counting could be even smaller. In average, for every charged particle generated in the electromagnetic shower, one photon is collected by the telescope.

Monte Carlo studies of low energy gamma showers confirm these important features concerning the photon distribution in the camera plane (MAGIC-I), after the reflector focusing. In figure 3.3, three exhaustive examples are illustrated.
Although the primary shower energy is very low, the photons ( $200 \div 250$ units) span a wide region, over the border of the trigger area. However, most of them are isolated or their density in a single pixel is very low. Considering that the conversion factor of a $P M T$ is around $30 \%$, often no photoelectrons, or only one, are produced in that channels (violet and blue pixels). There are then few compact pixels (green, yellow and red) that present a sufficient amount of photons ( $>10$ ), which can be detected. These hot pixels are typically arranged in a compact area of 3,4 or 5 units. There is always one core pixel which contains most of the light ( $20 \div 40$ photons) and others which are

[^42]

Figure 3.3: The distribution of Čerenkov photons (black dots) of simulated $\gamma$-rays in the camera of the MAGIC-I telescope. The programs used for the simulation are Corsika and Reflector. The figure (d) is a zoom of figure (a), (e) is a zoom of (b) and (f) is a zoom of (c). Note that the Čerenkov photons cover a large area containing several pixels within the camera plane, but only few pixels count enough photons to trigger the detector. (Adapted from [111])
close to the detection limit of around $10 \div 15$ photons, namely $3 \div 5$ phe, typical threshold for the MAGIC experiment.
Often, as in the example at 24 GeV , additional concentrated packets of photons appear. It seems that the number of small hot bunches increases with energy, so that at a certain point, their density is so high that the images become uniform and well defined by a single block. To check this behaviour, $\gamma$-rays at different energies from $\sim 10 \div 60 \mathrm{GeV}$ have been recorded (Fig. 3.4). Actually, up to $\sim 25 \mathrm{GeV}$ it is common to see 2 or three bunches. For very low energies, around 10 GeV , the packets are well noticeable, because only one or two pixels are involved in each of them. Then, they become larger and so frequent that they start to overlap $(25 \div 40 \mathrm{GeV})$ and finally they form a single huge blob ( $\mathrm{E}_{0} \gtrsim 40 \mathrm{GeV}$ ). The core pixels are always located in the apex of the image which is closest to the camera centre. This part of the projection, called head, represents the upper part of the shower, hence the first interactions. In this phase, the electrons are very energetic and practically undeflected by bremsstrahlung scattering. They are so collimated that the produced Čerenkov light is concentrated in only few pixels. Approaching the critical energy, the angular dispersion increases.
Considering the relativistic beaming effect, the angular dispersion is approximately inversely proportional to the Lorentz factor, hence it changes as a function of the interaction number (Eq. 3.2).

$$
\begin{equation*}
\alpha_{\text {scattering }}(n) \simeq \frac{1}{\gamma}=\frac{m_{e} c^{2}}{E(n)} \tag{3.2}
\end{equation*}
$$



Figure 3.4: The distribution at the camera plane of Čerenkov photons due to $\gamma$-rays of different energies, from 10.8 GeV to 58.6 GeV . The main properties of the primary $\gamma$-rays and the number of recorded photons in the core pixels are reported in table 3.1.

Up to the critical energy, the electron deflections are reported in table 3.2 as a function of some energy values. Assuming that at every collision the electron energy is halved, it is possible to associate the deflection with the interaction number. The deflections undergone by the electrons are negligible up to the interaction n-4. Their Čerenkov projections are still contained inside a single pixel or at maximum shared between two pixels, if the edge effect is taken into account. In the last interactions, the angular dispersion becomes important and some electrons can be scattered more than 6 equivalent pixels away from the original trajectory. However, a consistent fraction continues to feed the central core around the earlier collimated electrons.
It must be added that even the Čerenkov angle variation contributes. Photons produced near the first interaction ( $\sim 20 \mathrm{~km}$ ) have an angle up to $0.3^{\circ}$ smaller than the

| Event <br> $($ Name $)$ | Energy <br> $(\mathrm{GeV})$ | Impact parameter <br> $(\mathrm{m})$ | Total photons <br> $(\mathrm{ph})$ | Bunches <br> $(\mathrm{Nr})$. |
| :---: | :---: | :---: | :---: | :---: |
| a | 10.8 | 124.8 | 171 | 2 |
| b | 12.9 | 125.1 | 57 | 2 |
| c | 15.6 | 130.9 | 95 | 3 |
| d | 18.8 | 135.8 | 116 | 2 |
| e | 21.5 | 54.5 | 340 | 2 |
| f | 23.1 | 179.1 | 113 | 2 |
| g | 23.4 | 176.4 | 200 | 2 |
| h | 25.2 | 67.8 | 460 | 1 |
| i | 27.4 | 90 | 408 | 1 |
| j | 29.3 | 129.2 | 440 | 2 |
| k | 31.8 | 53.7 | 459 | 3 |
| l | 34.0 | 96.7 | 662 | 1 |
| m | 36 | 128.3 | 630 | 1 |
| n | 42.2 | 166.4 | 590 | 1 |
| o | 48.3 | 192.6 | 436 | 1 |
| p | 58.6 | 151.3 | 869 | 1 |


| Event <br> $($ Name $)$ | Pix. core <br> $(\mathrm{ph})$. | Pix. 1 <br> $(\mathrm{ph})$. | Pix. 2 <br> $(\mathrm{ph})$. | Pix. 3 <br> $(\mathrm{ph})$. | Pix. 4 <br> $(\mathrm{ph})$. | Pix. 5 <br> $(\mathrm{ph})$. | Pix. 6 <br> $(\mathrm{ph})$. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| a | 43 | 1 | 5 | 11 | 5 | 5 | 4 |
| b | 11 | 0 | 1 | 3 | 2 | 0 | 3 |
| c | 11 | 1 | 5 | 5 | 0 | 0 | 0 |
| d | 28 | 7 | 3 | 6 | 12 | 8 | 5 |
| e | 39 | 20 | 11 | 22 | 33 | 10 | 29 |
| f | 20 | 2 | 0 | 11 | 16 | 4 | 1 |
| g | 23 | 0 | 4 | 10 | 19 | 8 | 0 |
| h | 76 | 11 | 60 | 62 | 37 | 19 | 28 |
| i | 102 | 15 | 13 | 91 | 23 | 4 | 12 |
| j | 52 | 17 | 18 | 18 | 12 | 6 | 7 |
| k | 43 | 24 | 6 | 14 | 16 | 22 | 20 |
| l | 95 | 23 | 9 | 10 | 71 | 57 | 29 |
| m | 72 | 63 | 19 | 2 | 5 | 47 | 34 |
| n | 132 | 11 | 29 | 25 | 36 | 48 | 32 |
| o | 32 | 33 | 21 | 29 | 33 | 10 | 5 |
| p | 149 | 87 | 30 | 38 | 95 | 59 | 29 |

Table 3.1: The main proprieties of the events displayed in figure 3.4. In the upper table, the bunches are the well recognized photon clusters. In the lower table, the monitored pixels are the six ones around the core pixel. The numeration starts from the pixel closest to the camera centre and moves clockwise.
photons generated in the last cascade development [78]. This is another factor that enlarges the dispersion of 3 equivalent pixels, but it is important at the analysis level because it empathizes the elongated shape.
A $\gamma$-ray of 40 GeV is initially submitted by $4 \div 5$ strongly collimated interactions, where most of the Cerenkov photons are collected in few pixels, then the last scatterings smear the image, creating a uniform blob. Differently, a low energy event of 10 GeV

| Interaction <br> $(\mathrm{Nr})$. | Energy <br> $(\mathrm{GeV})$ | $\alpha_{\text {scattering }}$ <br> $\left({ }^{o}\right)$ | Equivalent pixel <br> $(\mathrm{Nr})$. |
| :---: | :---: | :---: | :---: |
| n | 0.083 | 0.34 | 3.4 |
| $\mathrm{n}-1$ | 0.166 | 0.17 | 1.7 |
| $\mathrm{n}-2$ | 0.332 | 0.08 | 0.8 |
| $\mathrm{n}-3$ | 0.664 | 0.04 | 0.4 |
| $\mathrm{n}-4$ | 1.3 | 0.02 | 0.2 |
| $\mathrm{n}-5$ | 2.7 | 0.01 | 0.1 |
| $\mathrm{n}-6$ | 5.3 | 0.005 | 0.05 |
| $\mathrm{n}-7$ | 10.6 | 0.003 | 0.03 |
| $\mathrm{n}-8$ | 21.2 | 0.001 | 0.01 |
| $\mathrm{n}-9$ | 42.4 | 0.0007 | 0.007 |

Table 3.2: The angular deflections of a relativistic electron due to bremsstrahlung scattering, as a function of some energy values. Starting from the critical energy, the value is doubled, because it is assumed that the electron energy is halved every interaction, as in the Heitler model. The equivalent pixel is the number of MAGIC-I camera pixels $\left(0.1^{\circ}\right)$ contained in the angle $\alpha_{\text {scattering }}$.
is subjected only to $2 \div 3$ collimated interactions, whereas the rest, which is dominant, is scattered significantly. This is the explanation of the multiple small, well separated bunches.
Finally, it is evident that most of the core pixels distribute in a ring around the centre, at not very large impact parameters. The main points can be summarized as:

* The camera region hit by the Čerenkov light is extended, but the light density is concentrated in few pixels.
* At very low energies the projections contain several small separated bunches of hot pixels.
* Most of the Čerenkov light is distributed within a ring around to the relative source position.
* Most of the Čerenkov light arrival time, in the camera plane, is contained inside a window of around 2 ns .

It is interesting to observe that by a full analysis of the light distribution, even if there is only one single photon in a pixel, it is possible to obtain an indication of the shower's orientation. On the contrary, taking into account only the dense small packets of photons, it is impossible to extrapolate the classical Hillas parameters. This feature suggests that there is still room for the classical Hillas imaging reconstruction. Obviously the photosensors size must be reduced to define perfectly the projection contour and the quantum efficiency should be at least higher than $50 \%$.

The time is another component, which plays a crucial role in the low energy domain. To detect a faint event, the acceptance threshold should be very low, close to the noise typically dominated by $N S B$. For the current $I A C T$ telescopes, the $N S B$ rate in a single pixel could reach several MHz with a low threshold of $3 \div 4 \mathrm{phe}$. The contamination due to this noise can be partially removed imposing a narrow time gate in the event selection and special algorithms in the reconstruction. However, a tight gate also causes the loss of some Čerenkov photons, deleting part of the image (more details in subsection 3.4.1). In figure 3.5, the arrival time simulation in the camera plane of an event of 10 GeV [84]
is presented. Most of the photons arrive within 2 ns , forming an image that initially is


Figure 3.5: The projection of Čerenkov light emitted by a $\gamma-$ ray of 10 GeV and an impact parameter of 150 m . The simulated photons are collected by a telescope of 30 m located at 2 km a.s.l.. The last figure (bottom) illustrates the original event without any particular arrival time cut. The first four figures show the projection in distinct temporal intervals. The arrival time windows are not equal because every image contains approximately the same number of photoelectrons. (Adapted from [84])
very concentrated, then spreads as a tail of a comet. The light emitted at the beginning of the shower development forms the head-on part of the image, while the delayed one is caused by the shower electrons that propagate further into the atmosphere. In fact, this component of light has larger Čerenkov angles and hits the camera further away from the nominal source position. The image profile becomes broad and the photon density somewhat lower. The large fluctuations are due to the multiple scattering of relatively slow electrons close to the critical energy.
The images in figure 3.5 demonstrate that a tight temporal constraint could be very useful in the selection algorithm to discriminate the $N S B$, but it affects the event reconstruction. Considering only a small duration of the image evolution, we obtain rather symmetric shapes, without an evident direction. Conversely, as already written during the comment of figure 3.3, the entire projection points out an orientation with
the classical elliptical shape. Anyhow, one should not be fooled by the nice appearance of the simulated photons. Introducing the camera pixelization and the correct reflector area, it becomes worse, with one or two pixels hot and the rest very faint.

Concluding, it seems that the time information could be applied with a tight threshold during the trigger phase in order to reject the background, but the threshold should be relaxed in the analysis reconstruction to form the complete image. Maybe the evolution of the arrival time could be used to extrapolate additional information.

### 3.4 Technical strategies at low energies

On the base of what has been described in the previous section, the performance of an $I A C T$ detector, at very low energies, is essentially determined by three conditions.

* The light detection efficiency has to be maximized. The quality of the information in the recorded event depends critically on the number of detected photons respect to the original quantity. Faint Čerenkov flashes contain a small amount of photons, which must not be lost. Even the leak of a small fraction of light could prevent either the detection of the event at the trigger level, or its reconstruction in the analysis. There are three important parameters that should be considered to improve this aspect: a) the telescope altitude; b) the light collection; c) the light focusing and its conversion.
At higher altitudes, the photons density of an $E A S$ increases, because the light pool covers a smaller area. Comparing the MAGIC altitude with a site at 5 km a.s.l., the photon density is a factor 2.5 lower, for an impact parameter below 100 m . Beyond 125 m where the low energy events are less concentrated, it becomes identical [84]. Moreover, the absorption of light crossing the atmosphere is reduced by $\sim 15 \%$ for a telescope at altitude of 5 km . The disadvantage is that at high altitude, the probability of ionizing particles hitting the PMTs is increased. Secondly, a larger reflector allows to collect more light from the shower. The signal to noise ratio and the sensitivity for weak fluxes improve significantly.
Third, the fraction of photons lost in the dish's reflection, in the focusing towards the camera and in the conversion in the photosensors, has to be reduced as much as possible. Therefore, the unique strategy is to enhance the available information and subsequently to maintain its integrity.
In figure 3.6(a), the energy threshold is expressed at different altitudes as a function of the equivalent telescope aperture $(S)$. $S$ represents the equivalent reflective surface area for an ideal light collection efficiency. It can be expressed as:

$$
\begin{equation*}
S=\varepsilon \cdot A \tag{3.3}
\end{equation*}
$$

where $A$ is the real telescope reflective surface and $\varepsilon$ is the light collection efficiency (for more details see section 4.4). For the MAGIC telescopes, $S$ is in the range $40 \div 50 \mathrm{~m}^{2}$, namely only the $20 \%$ of the real dish's dimension. The corresponding theoretical energy threshold is around 20 GeV , as shown by the blue line. At an altitude of 3500 m a.s.l., where more photons are collected, the limit is lowered to $\sim 15 \mathrm{GeV}$, so $25 \%$ better (red line).

* The trigger algorithm, namely the strategy to alert the data acquisition system that there is an event of interest, has to be able to reveal faint gamma images without being dominated by the background, especially the $N S B$. The usual criterion is to demand signals above threshold in some neighbour pixels. Unfortunately,

(a) IACT energy threshold

(b) Alpha distribution vs size

Figure 3.6: Left: the energy threshold of an imaging Čerenkov telescope as a function of the equivalent telescope aperture and its altitude. The vertical green line represents the MAGIC equivalent aperture ( $40 \div 50 \mathrm{~m}^{2}$ ), while horizontal lines indicate the correspondent energy threshold at different altitudes. The $N S B$ effect is not considered in this simulation. (Adapted from [1])
Right: the alpha distribution of simulated $\gamma$-ray events as a function of size. Red stars indicate the cut values, which maximize the quality factor defined in equation 2.16. The black and white vertical line shows the best alpha cut for an event containing 25 phe ( $\sim 25 \mathrm{GeV}$ ). The high value, around $50^{\circ}$, demonstrates a significant uncertainty in the estimation of the arrival direction. (Adapted from [39])
the electrical signal produced by an atmospheric shower below 50 GeV is quite small and it requires accepting even pulses with low charge and amplitude. At these low levels, the probability that the $N S B$ fluctuations exceed the threshold is so high that the original shower projection can be distorted or it can be lost because the acquisition is saturated by accidental events. It is then important to study how the image topology appears, how the charge is distributed and which is the arrival time evolution at the camera level, to try to improve the trigger efficiency.

* The analysis algorithm has to classify properly the events, even if the image contains few photoelectrons. The standard imaging technique seems to be inefficient at low energies, when the shower projections appear less elongated and less regular, introducing significant uncertainties in the calculation of the arrival direction, as well as the gamma/hadron separation (Fig. 3.6(b)). For instance, in the interval between $10 \div 50 \mathrm{GeV}$, the image typically consists of $20 \div 70$ phe distributed in a number of pixels which depends on their size. Lowering the pixel size and increasing the QE, the image becomes better defined and it is more easy to apply imaging filters to determinate the shower nature. In addition, it is possible to enlarge the number of pixels in coincidence at the trigger level, getting rid of spurious signals and facilitating the analysis cleaning. However, increasing the number of channels introduces new technical and financial problems.
Another useful information comes from the shower maximum, whereof an accurate determination can correct the energy fluctuations, which dominate over the uncertainty of measuring the impact distance. To this aim the stereoscopy is helpful, but it is not sufficient and it is mandatory to introduce innovative analysis,
which combine spatial and temporal algorithms at the same time.


### 3.4.1 Performance of trigger algorithms

All current IACT telescopes use similar trigger strategies, seemingly leading to similar performance numbers at the TeV regime, but they can differ notably in the detection of low energy events. Nowadays, a digital and an analogue approach exist to plan a trigger system. The first searches for N pixels (multiplicity) with a signal above Q photoelectrons, the second requires a signal formed as the sum of M pixels, above P photoelectrons. The latter solution has been tried with success only by the MAGIC collaboration and will be discussed in detail in chapter 5.

Since the aim of this chapter is to study the event morphology at low energies, only the digital solution is considered, because they are based on stringent topological and temporal constraints that can be studied. The analogue technique does not involve any particular topology, therefore it does not allow to understand the event shape. However, this is one of the most important reasons that make it very powerful in the detection of faint events.
As explained in the previous section 3.4, a standard trigger system has to satisfy to two contradicting conditions: the restricted number of available photoelectrons, which translates into low thresholds, and the $N S B$ rate, which asks for the contrary. For those algorithms, the afterpulse rate is not so problematic and can be ignored in first approximation.
To find the best compromise, one has to play with the duration of the trigger time gate and the minimum number of pixels involved in trigger (multiplicity). Lowering the time gate or increasing the multiplicity dimension, the accidental triggers induced by the $N S B$ are reduced. On the other hand, a large multiplicity is inefficient when the image size is very small and a too stringent temporal constraint could cause the loss of photons of the shower. In figures 3.7 (a) and 3.7 (b) the simulated trigger rate due to $N S B$ for different close compact configurations is shown. Closing the gate at 3 ns , it is possible to lower in average the threshold of 0.3 phe, keeping the same accidentals rate. Checking the probability to trigger $\gamma$-rays, it seems that down to a gate of 3 ns , there


Figure 3.7: Left: the trigger rate due to the $N S B$ for different close compact multiplicities and a temporal gate of 6 ns . The threshold is calculated at 400 Hz , which is the limit (The limit of the data acquisition system is $\sim 1 \mathrm{kHz}$, but in addition to the $N S B$ the contribution from hadrons must be included.) for an experiment as MAGIC. One mV corresponds to 1 phe. Right: in this case the temporal gate is imposed at 3 ns . (Images credit: M. Lopez \& F. Dazzi)
are no lost events, confirming again the fast evolution of the core pixels (Fig. 3.8(a)
\& Fig. 3.8(b)). It seems that the multiplicity of 3 pixels leads to a slightly better result, because it has a good rejection power and its size is similar to the core bunches described in section 3.3. However, except for the multiplicity 2 , the others are very close.


Figure 3.8: Left: the trigger probability to detect a $\gamma$-ray in function of the single pixel threshold, using different multiplicities and a trigger gate of 6 ns . The dotted lines indicate the probability at thresholds extrapolated in figure 3.7(a). Right: as before but with thresholds calculated from figure 3.8(b) and gate of 3 ns . (Images credit: M. Lopez \& F. Dazzi)

It is important to evaluate the topology of the multiplicity. Usually it is distinguished in three categories:

* Next Neighbour: N neighbour pixels above the discriminator threshold, so that any $\mathrm{N}-1$ of them are still neighbours. This is the multiplicity used in the previous analysis and its topological constraint is really strong as well as the $N S B$ rejection.
* Majority: N pixels in a pre-defined region of the camera (e.g. hexagon of 19 pixels) above the discriminator threshold. The topological constraint is absent and more background is accepted.
* Central pixel: one pixel (central) and N-1 of their neighbours are above the discriminator threshold. This strategy is based on a soft topological constraint.

Assuming to apply the multiplicity 3 at the few images in figure 3.4, it is evident that between $10 \div 20 \mathrm{GeV}$ only the majority trigger could work, because the photon packets are strongly dissociated. Then, up to 30 GeV even the central pixel trigger could become efficient and only beyond the next neighbour can be used.
Monte Carlo studies, comparing the performance of the central pixel trigger versus the next neighbouring one, reveal that effectively several faint events can be detected only relaxing the topological constraint. In figure 3.9 (a) the three possible shapes of the central pixel trigger are illustrated. The next neighbour trigger, which is also the standard trigger used in MAGIC, contains only the red configuration. Only $40 \div 45 \%$ of the total fraction of triggered events has been selected by the close compact arrangement. Another $40 \div 45 \%$ comes form the cyan disposition and the rest from the yellow stick shape.

Concluding, for energies higher than $\sim 40 \mathrm{GeV}$ the strategy to impose at the same time stringent topological and temporal constraints is successful, but going further


Figure 3.9: Left: the three possible topologies in a central pixel trigger with a multiplicity of 3 . The red shape is the only one used in the next neighbour trigger. Right: Frequency of the low energy gamma events in function of the topology. The topology distance has been defined as $\sum_{i}^{\text {pixel }} \sum_{j}^{\text {pixel }} d_{i j}$, considering a pixel with a diameter of 25.4 cm . (Adapted from [59])
down, the Čerenkov projections loose their coherent aspect forming small blobs, sometimes distinct. In this scenario it is mandatory to relax as much as possible the topological constraint and try to reduce the background contribution applying a more selective timing.

## The MAGIC Telescopes

he two MAGIC telescopes are located at Roque de Los Muchachos on the
Canary Island of La Palma $(\sim 2200 \mathrm{~m}$ a.s.l). These are IACT instruments made for the study of the astrophysical events in the VHE range. They can only operate during the night and observe a restricted portion of the sky at a time. The MAGIC telescopes are the largest IACTs in operation in the world. Thanks to its low energy threshold, MAGIC is the only instrument which can fill the energy gap between satellite and ground-based detectors.
The MAGIC design concept differs from the other IACT telescopes. First, an innovative carbon fibre structure allows very fast movements. Secondly, the readout electronics is not integrated into the camera frame, but is placed in a remote control house. The dislocation of most electronics from the camera body has many advantages. In first place the weight and the cooling power of the camera are reduced significantly. Another advantage is that one is not limited in space and can access the electronics more easily; maintenance and improvements can be done in a simply way. In fact, the renewal of both $D A Q s$ is in progress. In this chapter, the technical description and working principles of the main subsystems of MAGIC are presented.

### 4.1 Telescope design

The idea of a big, single telescope ( $M A G I C-I$ ) was born at the end of the ' 90 s , following the same concept as the parabolic solar concentrator, built near Stuttgart, Germany. The construction of the first MAGIC-I telescope ended in fall 2003 and it operated in single mode up to summer 2009. In 2009, the second telescope (MAGIC-II) was built, opening the possibility to operate in full stereo mode (Fig. 4.1). Basically, MAGIC$I I$ is an improved clone of the former telescope, with some novel technical solutions ${ }^{1}$, which became only recently available.

During the design phase it is important to define the goals of the project. MAGIC has been conceived to reach the lowest energy threshold in the VHE domain, where many unanswered physics questions loom and an overlap with satellite experiments is feasible. The energy threshold $\left(E_{t h}\right)$ is defined as the peak of the $\gamma$-ray energy distribution. It can be expressed as

$$
\begin{equation*}
E_{t h} \propto \sqrt{\frac{\phi_{N S B} \cdot \Omega \cdot \Delta t}{\varepsilon \cdot A}} \tag{4.1}
\end{equation*}
$$

[^43]

Figure 4.1: A photo of both MAGIC telescopes. On the left $M A G I C-I$ and on the right MAGIC-II. (Adapted from a photo made by R. Wagner)
where $\phi_{N S B}$ is the $N S B$ flux, $\Omega$ is the solid angle subtended by a $P M T, \Delta \mathrm{t}$ is the signal integration time, A is the reflective surface area and $\varepsilon$ is the light collection efficiency [133].
From relation 4.1, it is evident which are the technological strategies to be able to detect faint events. Considering the numerator, either the $N S B$ effect is minimized reducing the PMTs diameter, or the integration time is shortened with dedicated high-speed electronics. In the denominator, it is clear that the number of recorded photoelectrons has to be increased, focusing more photons with larger reflective surfaces and higher conversion efficiency on the camera. For this reason, MAGIC took advantage of the engineering progress in light detection and in the building of large and light structures. As of now MAGIC has reached an energy threshold of 50 GeV for the stereo data-taking with the standard trigger, whereas it is lowered to 25 GeV using the Sum-Trigger in mono tracking.

Based on the previous assumptions, one can summarize the key elements of MAGIC as:

* A light-weight rotating structure, which allows to precisely track the astrophysical sources and to activate the fast repositioning movement, when alerted by the $G R B$ monitoring network.
* A large reflective surface to capture and focus the faint Čerenkov flashes initiated by $\gamma$-rays in the Earth's atmosphere.
* A camera equipped with adequate light concentrators and high quantum efficiency photosensors to efficiently convert the photons into electrical signals.
* A low latency trigger system which has to identify very small shower projections and, at the same time, has to reject most of the events due to the NSB noise.
* A high sampling $D A Q$ (Data AcQuisition system), which digitalizes and stores the triggered signals, preserving both charge and timing information.
* Powerful analysis tools which can classify and reconstruct the recorded events, as described in section 2.3.

The performance of these elements also characterizes the telescope sensitivity in a specific energy domain.

Some of the above listed elements cannot be upgraded and remain frozen as in the original plan. Others can be replaced with innovative systems based on new ideas and new technologies. For instance, it is impractical to enlarge the mirror dish diameter, but it is feasible to improve the light conversion efficiency, as the MAGIC collaboration is doing in the current upgrade of the first telescope.

### 4.2 The telescope structure

The telescope structure, shown in figure $4.2(\mathrm{a})$, is a space frame based on carbon fiberepoxy tubes, joined by aluminium knots (Fig. 4.2(b)). Three tubular layers are laid upon each other and surrounded by as many stiffening rings. The resulting construction is fixed at two sides onto the vertexes of two pyramidal towers. This structure has advantageous features: it is rigid, light weight ( $\sim 5.5$ tonnes without mirrors), has negligible thermal expansion and an excellent oscillation damping.
The lateral geometry approximates an octagon of 7 m side length, supported by an


Figure 4.2: Left: the MAGIC structure layout and the correspondent dimensions from the front and side views. Right: an image of the carbon fiber-epoxy tubes, which sustain the reflective surface. (Image credit: MPI für Physik München)
alt-azimuth mount. The camera, located 17 m away from the reflector, is sustained by a metallic Gothic arch, which is stabilized by 10 pairs of 8 mm steel cables tied to the main frame. In this way, the resulting camera bending is kept within an acceptable limit.
Following a circular shape, the arch continues also over the back of the dish for two reasons: first it acts as a rail for the altitude drive, secondly the counterweight is placed on its upper apex.

Simulations performed with a finite elements program return a structure deformation less than 3 mm with respect to the ideal zero weight geometry. Furthermore, the atmospheric conditions at the telescope site could be very adverse and the building has been designed to be resistant to strong storms and ice loads. The idea of a protective dome has been abandoned due to costs.

### 4.3 Drive system

The structure can be oriented to point and track the sources in the sky [21]. Two types of servo-motors (Bosch Rexroth MHD112C-058) move the telescope in the azimuth
(Fig. 4.3(a)) and in the altitude directions (Fig. 4.3(b)). The allowed movement covers the interval from $100^{\circ}$ to $-70^{\circ}$ in declination and from $-90^{\circ}$ to $318^{\circ}\left(0^{\circ}\right.$ corresponds to the North) in azimuth. For the azimuth motion around the fixed central joint (Fig. 4.3(c)), two 11 kW motors are mounted in opposite positions on two out of the six bogeys connected on the space frame base, resting on the metal circular rail. Fixed chains form a mechanical drive link for the motors, which are engaged by toothed wheels. The third motor, for the elevation motion, is installed on the arch base, a couple of metres out of its lower apex to increase the declination on the side towards the camera access tower ${ }^{2}$. The elevation drive is also equipped with a holding brake, activated in the case the motor power is switched OFF.
The mechanical position is measured every millisecond by two absolute shaft-encoders


Figure 4.3: Left: a photo of the azimuth motor that pushes the telescope to rotate on a circular rail. Centre: a photo of the elevation motor used to move the structure to different zenith angles. Right: a photo of the rotative central axis joint, planted into the ground. (Image credit: MPI für Physik München)
(Heidenhain ROQ425) of 13-bit precision $/ 360^{\circ}$. The shaft-encoders give a sinus function between two steps so that a relative resolution of a 15 -bit encoder can be reached. One shaft-encoder is placed on the azimuth axis, while the other one is installed on the elevation axis. Then, the real pointing coordinates are verified by a star-guider camera, mounted at the centre of the mirror dish structure. It compares the tracking position of the telescope camera, obtained with a ring of LEDs placed at the edges of the camera, with the pointing direction in the sky, calculated using reference stars. Safety end-switches, connected to the motor controller units, prevent movements beyond the allowed ranges.

During normal operation, the $\approx 65$ tonne telescope can track a source with an accurate precision of the order of $0.02^{\circ}$, including systematics. When a $G R B$ alarm arrives, the drive system can reposition the telescope, completing a rotation of $180^{\circ}$ in less than 20 s .

### 4.4 Optics

In the relation 4.1, a significant factor for the threshold energy of an $I A C T$ telescope is the light collection efficiency $(\varepsilon)$. For a camera equipped with PMTs, the $\varepsilon$ is a combination of several components, as shown is the following equation:

$$
\begin{equation*}
\varepsilon=\int_{300 \mathrm{~nm}}^{700 \mathrm{~nm}}\left[R_{d i s h} \cdot\left(1-L_{f o c .}\right) \cdot\left(A_{p m t}+A_{l c} \cdot R_{l c}\right) \cdot Q E \cdot C_{d y_{-} 1} \cdot\left(1-L_{d y_{-} 1}\right)\right] d \lambda \tag{4.2}
\end{equation*}
$$

[^44]where $R_{\text {dish }}(\lambda)$ is the dish reflectivity, $L_{f o c .}(\lambda)$ is the fraction of light not reaching photosensors due to bad focusing or photon scattering, $A_{p m t}$ is the PMT fraction of active area, $A_{l c}$ is the fraction of active area of the light concentrators, $R_{l c}(\lambda)$ is the reflectivity of the light concentrators, $Q E(\lambda)$ is the $P M T$ quantum efficiency, $C_{d y_{-} 1}$ is the photoelectron collection efficiency onto the first dynode and $L_{d y_{-} 1}$ is the loss at the first dynode stage. The chosen integration interval is very conservative, because the main Čerenkov contribution is below 450 nm . The two functions $R_{\text {dish }}(\lambda)$ and $L_{f o c} .(\lambda)$ are strongly related to the performance of the telescope's optics.

The profile of the MAGIC reflector approximates a parabola with a diameter of 17 m . This choice is forced to keep the information of the photon arrival time, since the distance between the mirror facets and the camera is always isochronous. Parallel light rays are focused on the same $P M T$, hence every pixel represents a small range in the incident angles. Photons travelling along the telescope axis are concentrated on the central pixel, as shown in the left sketch of figure 4.4. When the incident light is tilted a little bit, as in the right sketch, the hit pixel is off-centre by an amount $\rho$ that in first approximation is given by:

$$
\begin{equation*}
\rho \sim \sin (\beta f) \sim \beta f \tag{4.3}
\end{equation*}
$$

where $f$ is the parabolic mirror surface focal length.


Figure 4.4: Focusing of parallel photons coming from different angles. The photosensors lie in the focal plane F of the mirror reflective surface.

The reflector focal length is 17 m as the dish diameter (D). The ratio $(f / \mathrm{D})$ is 1 , which assures a low astigmatism over the FoV of $3.5^{\circ}$.

### 4.4.1 MAGIC-I mirrors

The MAGIC-I octagonal reflector of $236.2 \mathrm{~m}^{2}$ area is segmented with 964 square allaluminium mirrors of 49.5 cm by side (Fig. 4.5(a)), attached on 247 support panels (Fig. 4.5(b)). Some of them (223) house 4 mirrors, others, placed mainly on the surface edge, only 3 mirrors.
Not all mirrors are equal, but in general they follow the same sandwich concept used in the aeronautical environments. Each element is an assembly of an open box filled with hexcell honeycomb ${ }^{3}$ (Al 3003-5.2-1/4-003P), and a top plate (Fig. 4.5(c)). The parts are glued using structural adhesive films from $3 \mathrm{M}^{\text {TM }}$ (Scotch-Weld AF-163-2K). The result is a robust and light-weight ( $\sim 3 \mathrm{~kg}$ ) aluminium box, dubbed raw blank. Originally

[^45]two slightly different designs have been mounted on the reflector. One produced by the MPI group ( 224 units), which does not present the lateral wall, another realized in Padova ( 740 units), in which the honeycomb is surrounded by walls of the Al box. When studying the behaviour of the mirror over time (ageing), it was discovered that water could condense inside the honeycomb cells, deforming the raw blank original shape during the formation of ice at low temperatures during winters. A third design has been realized to improve sealing. The heating circuit has been moved outside the raw blank to increase the compactness. The contact point between the plate and the box has been changed to favour a sealing with a specific bi-component epoxy-glue $\left(3 \mathrm{M}^{\top \mathrm{M}}\right.$ DP190).


Figure 4.5: On the left, a photo of one of the last produced small aluminium mirror made by the Padova group. In the centre, a sketch of the support panel for four mirrors. (Image credit: MPI für Physik München)
On the right, the general exploded view of the MAGIC-I raw blank. In the last version, the heating circuit is connected externally on the back of the aluminium box. (From [9])

The transformation from raw blank to mirror is completed when the upper Alplate is diamond turned to obtain a local reflectivity of $80 \div 90 \%$ in the optical range (Fig. 4.6(a)). To avoid corrosion, the reflecting surface is finally coated with a protective thin transparent layer of quartz [13].
At the end of the whole process, the roughness $R M S$ is well below 10 nm (Fig. 4.6(b)).


Figure 4.6: Left: mirror reflectivity measured at different wavelengths with a double-beam spectrophotometer. Right: roughness of a mirror sample after milling and coating. The central spike is caused by the milling machine. (From [9])

However there are some regular spikes, which are produced during the passage of the milling machine. Sometimes a reticle is formed and the incident light can be diffracted.

Due to the intrinsic roughness of the mirror surface, in this technique a significant part (up to $15 \%$ ) of the reflected light is diffuse scattered and not focussed at the focal point. One has to find a compromise between the mirror reflectivity and the costs of the production. The longer the surface is polished with the diamond the lower the surface, however, the higher the costs for the machining.

The mirror profile of each segment is spherical with a curvature radius that spans between 34.018 m and 36.715 m . The radius is dependent on the position of the mirror on the parabolic dish. The typical point spread function is less than 1 cm , so most of the reflected light is contained inside a single $P M T$ (more details is subsection 4.5.1).

### 4.4.2 MAGIC-II mirrors

In MAGIC-II two different technologies have been applied. There are $1431 \mathrm{~m}^{2}$ allaluminium mirrors, mounted in the central area of the dish, and 104 cold slumped glass mirrors in the outer rings (Fig. 4.7(a)). The total reflective surface is a little bit larger than MAGIC-I, about $236.8 \mathrm{~m}^{2}$, because the outer ring of the reflector is assembled with $1 \mathrm{~m}^{2}$ mirrors and not with 3 small mirror facets. The support panels have been eliminated, and the facets are connected directly to the frame structure through the actuators of the Active Mirror Control (AMC) system, described in the next subsection (4.4.3). The total weight reduction is around $30 \%$, namely from $\sim 25 \mathrm{~kg} / \mathrm{m}^{2}$ to $\sim 18 \mathrm{~kg} / \mathrm{m}^{2}$.

The aluminium raw blank is an expanded version of the MAGIC-I production. The assembled block is composed of an upper plate ( $985 \times 985 \times 3 \mathrm{~mm}$ ), a honeycomb panel $(971 \times 971 \times 60 \mathrm{~mm})$, an aluminium back box $(973 \times 973 \times 61.9 \mathrm{~mm}) 2 \mathrm{~mm}$ thick and 3 fixing pads ( $100 \times 100 \times 12 \mathrm{~mm}$ ) inserted for the mounting (Fig. 4.7(b)). There is a central hole to house the AMC laser to control the mirror position [50]. The increased


Figure 4.7: On the left, a photo of a small portion of the MAGIC-II reflector, which is reflecting the camera lid image. The ones with the central hole are $1 \mathrm{~m}^{2}$ aluminium mirrors, the others are glass mirrors. (Courtesy of M. Garczarczyk)
On the right, the general exploded view of the MAGIC-II aluminium raw blank. (Image credit: M. Zago)
thickness of the honeycomb enhances the raw blank rigidity. The consequent diamond
milling is less affected by local deformations and the curvature radius nicely matches the nominal value. The focusing power reaches a resolution of 0.5 mrad for a pointlike source. On the other hand, it is more hard to fit the parabolic profile of the ideal dish. The best solution should be astigmatic mirrors with two radii of curvature. Unfortunately, this kind of mirror is still very difficult to produce.

The alternative technological process, developed in collaboration with the INAF group and Media Lario Technologies company, deforms elastically a glass plate ( $985 \times-$ $985 \times 1.7 \mathrm{~mm}$ ), forcing it to take the shape of a convex mould. Using a vacuum suction, the glass adheres perfectly to the mould surface and a honeycomb foil ( 20 mm thick) is glued above it to provide the structural rigidity. The sandwich is completed sticking a second glass plate on the top, applying a structural epoxy resin adhesive. The final steps of the production consist in the vapour deposition on the concave side of a reflective coating layer of aluminium and another protective quartz $\left(\mathrm{SiO}_{2}\right)$ layer. The sandwich borders are assured by a silicon based sealant, reinforcing the lateral protection [110]. This technique takes advantage of the large required curvature radius and the thin thickness of the glass sheet. Using the same master mould, it is possible to obtain various curvature radii controlling the spring-back effect during the gluing phase.
Compared with the aluminium facets, the glass mirror presents a higher reflectivity $(85 \div 90 \%)$, a lower roughness $(\sim 2 \mathrm{~nm})$, but a worse focusing ( $0.5 \div 2 \mathrm{mrad}$ ). The weight of a single facet is $12 \mathrm{~kg}, \sim 35 \%$ less than the aluminium unit. The last difference is the laser position for the $A M C$ system. It has been fixed to one of the four corners of the mirror, as it is to difficult to drill a hole in the centre of the glass mirror.

### 4.4.3 Active mirror control

The light-weight tubular frame of the MAGIC mirror dish deforms slightly, when changing the telescope orientation. The orientation of the mirrors follows directly the dish deformations and is subjected to small misalignments that needs to be corrected. An active mirror control $(A M C)$ automatically corrects such changes [14].
The support panel in $M A G I C-I$ and directly the $1 \mathrm{~m}^{2}$ mirror in $M A G I C-I I$ are joined to the space frame at 3 points. One of them is fixed, the others are connected through two longitudinally movable actuators having one and two dimensional lateral degrees of freedom respectively. Each actuator contains a two phase stepping motor and a ball-bearing spindle, which assure a minimum step of $10 \mu \mathrm{~m}$. Hence, the focused light spot position on the camera plane can be moved with a precision of 1.7 mm .
Each panel/mirror is equipped with a guidance laser ( $645 \div 665 \mathrm{~nm}$ ) pointing to the camera centre. For MAGIC-II, a new laser, not problematic for the PMTs, has been installed. It works in the infrared spectrum ( 1300 nm ), where the PMTs are completely insensitive.
The laser spot was used initially to estimate the misalignment of the mirror with respect to four reference $L E D s$ mounted on the camera lids. The $A M C$ system uses a $C C D$ camera, which is mounted in the centre of the mirror dish structure. This camera monitors the position of the laser spots on the telescope camera lids. Using this position, respect to the reference $L E D s$, the correction of the inclination of the panels can be calculated and applied with the two actuators.
Nowadays, a high sensitivity $S B I G S T L-1001 E$ camera is utilized. It allows one to see the reflected spot of a star from each mirror segment and to focus the mirrors using stars.
The system is completed by 62 water tight (IP67) boxes, which contain the control electronics for the actuators and the lasers. The boxes are connected to the computer
using eight independent $R S-485^{4}$ lines for parallel operations (Fig. 4.8).


Figure 4.8: General overview of the $A M C$ system. On the left, the stuff mounted on the camera structure, in the centre an adaptive optics module and on the right the control electronics. (From [14])

In the first design of the $A M C$, the use of laser pointers was thought to be the standard focussing method. The advantage of the laser pointers is that the mirror position is adjusted, independently from the deformation of the telescope dish. A change of loads on the dish is therefore automatically corrected. The main disadvantage of this procedure is the time needed to focus all 247 panels of each telescope. The fastest way is to adjust in parallel about 30 panels/mirrors at a time, according to a pre-calculated grid arrangement. The operation is completed in a few minutes, since only eight cycles are necessary. However, it is not possible to apply it during data-taking or after a $G R B$ alert. The reduction of the observation time (the telescope camera needs to be closed during the usage of the lasers as the PMTs are sensitive to the red light, which is also reflected on the closed lids) and the time needed to start $G R B$ observations are too long.
Studies of the dish deformations versus zenith angles have showed that the misalignments can be reproduced on large time scales. Using look-up tables containing the position of each actuator at different zenith angles, the overall focussing is replicated very well. An adjustment of the complete reflector takes at maximum 10 s and can be performed while moving the telescope to the next coordinates. In addition this procedure does not require closing the lids and switching on the lasers.

### 4.5 Camera

The remaining parameters of equation 4.2 are related to the telescope camera, where the light concentrators and the PMTs constitute the central elements. With present technology, many of them are, unfortunately, inversely related. The PMTs used in the $I A C T$ experiments present an extended active area, but a poor quantum efficiency $(25 \div 35 \%)$. On the other side, there are silicon photosensors with high $Q E(\lambda)$ available

[^46]on the market, but they are small in size and in $A_{p m t}$. The solution usually adopted is to connect, just in front of the sensor, a light concentrator in order to focus photons in the active area. Even if this technique returns good results, part of the light is lost during the internal reflections of the focusing phase $\left(R_{l c}(\lambda)\right)$. Moreover, a small fraction of dead area still survives $\left(1-A_{l c}\right)$.
In this field, technological progress may bring significant improvements to new generation IACTs.

### 4.5.1 MAGIC-I camera

The MAGIC-I camera is an hexagon of $114 \times 104 \mathrm{~cm}$, which covers a field of view of $3.5^{\circ}$ in the vertical direction and $3.85^{\circ}$ in the horizontal one. It is composed of PMTs of two different sizes. The central hexagonal region, $69 \times 61 \mathrm{~cm}$, is covered by 397 small pixels $1^{\prime \prime} \varnothing\left(0.1^{\circ} \mathrm{FoV}\right)$ and the external ring by 180 large pixels $1.5^{\prime \prime} \varnothing\left(0.2^{\circ} \mathrm{FoV}\right)$.
The central pixel has been modified for optical observations. It is mainly used for Pulsars studies, where there are periodical and simultaneous emissions in the optical and gamma regime [8]. The typical Pulsar frequencies are in the range $1 \mathrm{~Hz} \div 1 \mathrm{kHz}$. The Pulsar emission changes the output current of the central pixel which is digitized and stored in a dedicated chain for off-line analysis.

The PMTs, Electron Tubes 9116A and $9117 A^{5}$ (Fig. 4.9(a)), have been modified to enhance the probability to produce photoelectrons in the Cerenkov spectrum peak. A special lacquer ${ }^{6}$, doped with a wavelength shifter P-Terphenyl, has been applied on the glass cover, in order to shift the UV component towards the more sensitive yellow band [108]. The quantum efficiency improvement is shown in figure 4.9(b). In addition, the light concentrator geometry has been studied in such a way that the reflected photons can cross twice the hemispherical photocathode, favouring the photoelectrons conversion by a factor of $20 \div 30 \%$ [105].
The PMT cathode is powered at the negative voltage of $(0.7 \div 1.45) \cdot 10^{3} \mathrm{~V}$. The internal


Figure 4.9: Left: a photo of both PMTs from Electron Tubes, installed in the MAGIC-I camera. (Photo by R. Wagner)
Right: the final quantum efficiency obtained with the special lacquer coating. (Adapted from [107])

[^47]amplification stage is made of 6 dynodes, limited to a gain of around $3 \cdot 10^{4}$, so that observations with moderate moon light are possible. Its typical DC current, in dark conditions, is $\approx 1 \mu \mathrm{~A}$.

Close to the PMT, there is a low noise transimpedance pre-amplifier, which further amplifies the signal. Then, the pulse is converted back into light, and transmitted by a VCSELs (Vertical Cavity Surface Emitting Lasers) into long ( 162 m ) multi-mode optical fibres to the counting house, where the electronics is located (Fig. 4.10(b)). The VCSEL, provided by Honeywell (HFE4080-321), is a product intended for high-speed data communications even in the GHz domain. It generates an output of 850 nm with a typical rise time of 100 ps .
For long transmissions, the optical fibres have practical advantages over standard cables.


Figure 4.10: Left: frontal view of MAGIC-I camera with opened lids. Right: the back view of MAGIC-I camera without the cover. The green optical fibres and the blue VCSEL light transmitters are clearly visible. (Photo by R. Wagner)

They are not affected by cross-talk, no electromagnetic interference and no grounding bounces. Moreover, their cross-section is very small and hence many fibres are packaged in a single narrow retaining cable. The resulting low-weight does not put strain on the telescope mount.

In the camera, the temperature is stabilized around $35 \div 40^{\circ} \mathrm{C}$ by a water cooling system regulated by feedback sensors. The most sensitive devices are the VCSELs, whose gain depends strongly on the temperature. Even the air is constantly exchanged to prevent the dew point.
The signal processing and HV control electronics inside the camera dissipate about 1 kW power.
The camera structure can be moved back-and-forth by about 30 cm to adjust the focal point. Usually it is not focused to infinity, but is shifted backwards by 3 cm to focus to $\sim 10 \mathrm{~km}$ above the telescope, where the maximum shower development takes place.
The camera is completed by two lids to protect photosensors from the daylight and strong light sources (Fig. 4.10(a)). The total weight is around 500 kg .

### 4.5.2 MAGIC-II camera

The MAGIC-II camera is quite different from the one of the first telescope [127]. The outside dimensions and the shape still remain similar (Fig. 4.11(a)), but the internal design and the components have been renewed, maintaining the same FoV (Fig. 4.11(b)). The number of PMTs (Hamamatsu R10408) is doubled (1039) in respect to MAGIC-I and all have the same size of $1^{\prime \prime} \varnothing\left(0.1^{\circ} \mathrm{FoV}\right)$. However, they belong to the same class of


Figure 4.11: Left: frontal view of MAGIC-II camera with opened lids. Right: the back view of MAGIC-II camera without the cover. The orange optical fibres and the yellow cables for the clusters control are clearly visible. The 19 black cables, that exit from the structure, contain the PMT optical fibres. (Photo by R. Wagner)
sensors, namely 6 stages with hemispherical photocathodes and a Cockcroft-Walton HV generator ${ }^{7}$ included. The quantum efficiency, without any special coating, is around $32 \%$ in the blue band (Fig. $4.12(\mathrm{~b})$ ) and the afterpulse rate is $0.3 \%$ at 4 phe. On the front side, the PMTs are equipped with Winston cone type light guides to minimize their dead area, same as in MAGIC-I.
At the base of each $P M T$, there are some additional circular circuit boards. They house a high bandwidth ( 800 MHz ) and low noise pre-amplifier (Sirenza SGA-5586) with a gain of 25.5 dB , a DC current and a HV monitoring, a charge injection input and a VCSEL with its bias current monitoring. As in MAGIC-I camera, the signal generated in the $P M T$ is amplified and immediately converted into an optical signal for the transmission to the control house, 165 m away. The transmission is driven by the VCSEL chip Avalon Photonics AVAP-850SM, which emits at the wavelength of 850 nm .
Long aluminium tubes cover both the photosensor and the additional devices, forming a compact cylinder, the so-called pixel-module. Seven of these pixel-modules, sorted in a hexagonal configuration, are grouped in 169 clusters (Fig. 4.12(a)). 127 clusters are fully assembled with PMTs, while 42 , placed in the circumference of the camera, are only partially equipped with PMTs in order to approximate a round configuration. The modular subdivision favours the maintenance and the substitution of broken units. Each cluster body incorporates the charge injector generation board, the slow control board and the distribution board for the distribution of power and control signals. This slow control electronics is controlled by a computer, connected via $R S-485$ and VME optical links.

An innovative feature of $M A G I C-I I$ camera is given by the pulse injector system. In each cluster, a test pulse, that simulates the $P M T$ response, can be injected in the electronic chain, enabling technical measurements even during the day, when the HV cannot be switched on.

A 8 kW water cooling system assures good temperature stability within $2^{\circ} \mathrm{C}$. The clusters are housed in vertical heat exchanging separator plates. The cooling liquid, from small pipes, flows inside these plates. The base of heat exchanging system is thermally connected to the clusters via aluminium rods.

[^48]

Figure 4.12: Left: a photo of a camera cluster of 7 PMTs. The zoom (yellow lines) of the upper part of the cluster shows the layout of a single pixel-module. Right: the MAGIC-II PMTs quantum efficiency (red curve) compared with that one of MAGIC-I photosensors (blue). The red band shows the spread over the measured PMTs. (Adapted from [128])

In the external ring there are 6 free clusters, which are used to test Hybrid avalanche Photon Detector (HPD) from Hamamatsu (R9792U-40). Currently, they are installed and are being commissioned. The entire camera will be upgraded with them if they prove to be significantly better than the PMTs.
The total camera's weight is around 600 kg for a diameter of 1.462 m and a thickness of 0.81 m .

### 4.6 Electronic chain

Differently from other IACT experiments, MAGIC has preferred the alternative solution to move the electronics in a dedicated data acquisition building, limiting the problems related to a heavy camera, the temperature control, the miniaturization of components and to difficult access for maintenance.
The PMT pulse, transmitted over an optical link, is first converted back into an electrical signal and amplified, then it is split into two parallel branches: the trigger and the data acquisition system. The trigger selects the interesting events and sends the enabling command to the data acquisition to start their sampling.

The trigger system is subdivided into three consecutive levels, with the main purpose to reject light flashes due to the fluctuations of the $N S B$.

* Level 0 (LTO): it is a simple discriminator with a programmable threshold. Only signals that exceed the set threshold pass to the next level. It fixes the minimum light quantity that should be present in each photosensor and the accepted $N S B$ rate. The $N S B$ photon flux $\left(\phi_{N S B}\right)$ has been measured at the MAGIC site and estimated:

$$
\begin{equation*}
\phi_{N S B}=(1.75 \pm 0.4) \cdot 10^{12} \frac{p h}{m^{2} \cdot s r \cdot s} \tag{4.4}
\end{equation*}
$$

where $p h$ indicates photon [97]. Assuming a reflective surface of $236 \mathrm{~m}^{2}$, a dish reflectivity of around $80 \%$ and a pixel radius of $0.05^{\circ}$, we can calculate the photon rate per pixel:

$$
\begin{equation*}
N_{p h}=\frac{\phi_{N S B} \cdot A_{d i s h} \cdot R_{d i s h} \cdot \Omega_{p m t}}{s} \simeq 0.8 \mathrm{ph} / \mathrm{ns} \tag{4.5}
\end{equation*}
$$

where $A_{d i s h}$ is the dish area and the $\Omega_{p m t}$ the solid angle of a single pixel. In the previous equation 4.5 , the diffraction of the mirror is not taken into account, because for small deviations from the nominal angle, it marginally affects the pixel rate due to the isotropic $N S B$. At the utmost, some photons fall in the neighbour photosensors.
The mean number of photoelectrons $\left(\bar{n}_{p h e}\right)$ is:

$$
\begin{equation*}
\bar{n}_{p h e}=N_{p h} \cdot Q E \cdot \Delta t \simeq 1 p h e \tag{4.6}
\end{equation*}
$$

where $\Delta t$ is the integration time. Considering that the $N S B$ follows a Poissonian distribution, the probability that fluctuations exceed a threshold $n_{t h}$, expressed in photoelectrons, is:

$$
\begin{equation*}
P\left(x>n_{t h}\right)=1-\sum_{x=0}^{n_{t h}} P(x) \tag{4.7}
\end{equation*}
$$

where $P(x)$ is the probability (Eq. 4.8) to have $x$ photoelectrons in the pre-defined integration window time.

$$
\begin{equation*}
P(x)=\bar{n}_{p h e}^{x} \cdot \frac{e^{-\bar{n}_{p h e}}}{x!} \tag{4.8}
\end{equation*}
$$

The single pixel rate is then:

$$
\begin{equation*}
f_{\text {pixel }}=\frac{P\left(x>n_{t h}\right)}{\Delta t} \tag{4.9}
\end{equation*}
$$

where $P\left(x>n_{t h}\right)$ is obtained from equation 4.7. In table 4.1 some pixel frequencies are reported as a function of the threshold.

| Individual pixel rate |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{n}_{\text {th }}$ (phe) | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| $\mathbf{f}_{\text {pixel }}(\mathbf{M H z})$ | 160 | 68 | 21 | 5.1 | 1 | 0.17 | 0.03 |

Table 4.1: Some examples of the individual pixel rate as a function of the LT0 threshold.

Level 1 (LT1): It is a digital filter, which rejects most of the accidental events due to $N S B$, combining temporal and spatial information at the same time. It takes advantage of the fast evolution of compact projections, caused by the Čerenkov flashes associated to gamma showers, with respect to unrelated $N S B$ fluctuations. The algorithm verifies whether N next-neighbour pixels ( $\mathrm{N}=2,3,4,5$ dubbed $2 \mathrm{NN}, 3 \mathrm{NN}, 4 \mathrm{NN}$ and 5 NN fold) show a synchronous signal in a time gate of some nanoseconds. The topological constraint imposes that hot pixels must stay in a close compact configuration, so every pixel of that group should be in contact with other two ${ }^{8}$ [55]. The generating trigger rate ( $T_{N N-f o l d}$ ), only due to $N S B$ (accidental triggers), is a function of the selected $N N$-fold, the individual

[^49]pixel frequency $(R)$, the time gate duration $(G)$ and the total number of independent close compact combinations in the trigger area ( $\rho N_{C o m b}$.). It can be expressed as:
\[

$$
\begin{equation*}
T_{N N-\text { fold }}=R^{N N} \cdot G^{N N-1} \cdot C_{N N} \cdot \rho N_{C o m b} \tag{4.10}
\end{equation*}
$$

\]

where $C_{N N}$ is a geometrical coefficient, which arises from the intersection of the signal arrival time functions in the NN-dimensional space [49]. $N_{C o m b}$. is the number of close compact combinations in the whole trigger area. Due to the trigger modular design (see next subsections 4.6.1 and 4.6.2 for details), some combinations are repeated and others are not independent. $\rho$ represents the corrective factor to scale down to the effective number.
In a normal mono data-taking with a threshold of $\sim 6$ phe, only a few Hertz of accidentals pass the trigger selection, resulting in a rejection factor of the order of $10^{4}$.

* Level 3 (LT3): It is the timing coincidence between the LT1 (Level 1 Trigger) signals coming from different telescopes. Further details are available in section 6.2.

Up to one year ago, MAGIC-I was equipped with the level 2 trigger, designed for a preliminary topological analysis of the shower images. It was never completely commissioned and for a long time it was activated only in transparent or flag mode. At the present time it is not included in the trigger chain.

In both telescopes, the pulses in the second branch are sampled at the same speed of 2 Gsample/s. Nevertheless, the readouts make use of different electronics. A custom multiplexed system with commercial $F A D C$, so-called $M U X$, is adopted in MAGIC-I, whereas in MAGIC-II the digitization is provided by an analogue ring sampler ( $D R S 2$ ) and high resolution $A D C$.

### 4.6.1 MAGIC-I electronic chain

The MAGIC-I electronic chain is illustrated in figure 4.13. The two main systems, the trigger and the data acquisition are shown in the right side of the sketch, after the optical splitting.


Figure 4.13: The diagram blocks of the MAGIC-I electronic chain. (From [64])
The MAGIC-I trigger area has a FoV of $2.1^{\circ}$, restricted to 325 pixels. The optical
signals, converted again into electrical ones in the receiver board ${ }^{9}$, are digitalized by a programmable threshold (LTO) and then elaborated for the next stage, the LT1. In this phase, the signal is adjusted in time with $E C L^{10}$ delay lines, then its width is fixed varying the $R C^{11}$ value at the output of a flip-flop.
The transfer to the $L T 1$ electronics is done with 41 semi-custom $M D R$ differential cables, each one containing 8 channels. The distribution of these cables over the whole trigger area is shown in figure $4.14(\mathrm{a})$.

The LT1 modular design is shared out by 19 partially overlapped trigger cells, dubbed macrocells (Fig. 4.14(b)). Each macrocell, analysed by a single unit (LT1board), is a hexagon composed of 37 pixels, whereof one is specifically blind as 36 is the maximum number of signals that the LT1-board can handle with a good timing resolution ( 300 ps ). The macrocell overlap guarantees an efficient coverage of the logic combinations, avoiding macrocell edge effects ${ }^{12}$. The repetition of the channels and their routing to the proper macrocell, or better to the LT1-board, is performed by a large motherboard, called LT1-backplane.
The LT1 selection strategy, explained in the previous section 4.6, is implemented in PLDs ${ }^{13}$ EPLD128ATC100-7 from Altera. In the end, the triggered events from the 19 LT1-boards are merged in a global $O R$, processed by a dedicated board so-called Trigger Processing Unit. The resulting signal is sent either to the LT3, when the telescopes are in stereo data-taking, or directly to the data acquisition system for the event sampling.


Figure 4.14: Left: the subdivision of the trigger area into 41 groups of pixels. Each group symbolizes a connector/cable at the input of the trigger system. Right: the representation of the 19 trigger macrocells, partially overlapped within the inner part of the MAGIC-I camera. The coloured pixels are blind for the corresponding macrocell with the same colour. (Image credit: D. Corti)

In 2007, a novel trigger was installed in parallel to the standard one. This prototype

[^50]system, called Sum-Trigger, is largely discussed in section 5.1.
The data acquisition system is based on fibre optic multiplexers ( $M U X$ ), which allow to digitize consecutively 16 channels in a single commercial $F A D C$ [64]. The signals are opportunely delayed before the multiplexer, so they enter in the $F A D C$ occupying different time slots, spaced 40 ns far from the previous one. No delay is applied to the first channel, while the 16 th one is sampled 600 ns later. This approach is possible because the Čerenkov flash duration is very short respect to the trigger frequency (of the order of 1 kHz ).
The multiplexers are based on high bandwidth $M O S F E T^{14}$ switches with a low crosstalk of $0.1 \%$. They are controlled by a digital circuit clocked at 800 MHz , corresponding to a switch jitter of only 1.25 ns . The only disadvantage is the introduction of switching noise that affects the last 10 ns of each time slot. However, the peak noise is removed at the software level.
The FADC modules (Acqiris DC282) have a bandwidth of 700 MHz , a sampling speed of 2 Gsample/s and 10-bit resolution for an input voltage range of 1 V . Each module has $4 F A D C s$, hence it can handle up to 64 channels for a typical consumption of 60 W . The digitized data are temporally stored in four $512 \mathrm{kByte} R A M$ and read out at 64 MHz via a cPCI bus. Then, thanks to the fibre channel technology, the data throughput is $100 \mathrm{MByte} / \mathrm{s}$ for a trigger frequency beyond 1 kHz . The data acquisition dead time is about $25 \mu$ s and saturation appears at around 800 phe.
The main advantage of this solution is to maintain a high sampling resolution at a lower cost compared to using one ultra-fast $A D C$ per channel.

### 4.6.2 MAGIC-II electronic chain

The electronic concept utilized in $M A G I C-I$ is replicated in MAGIC-II, but most of the devices have been renewed. In this section only the differences between the two telescopes are presented.

The MAGIC-II trigger area has been enlarged to $2.5^{\circ} \mathrm{FoV}$, covering $559^{15}$ pixels. The number of macrocells and their shape remain the same, whereas the overlap is reduced to only one pixel (Fig. 4.15(b)). The advantage is motivated by the possibility to trigger showers at higher impact parameters, improving the wobble mode data-taking. It can happen that some events, that fall between two macrocells, are lost, but from Monte Carlo studies this is not sufficient to object to the new strategy.

The receiver board has been completely redesigned by the $I F A E$ group, but it is still fully compatible with MAGIC-I electronics (Fig. 4.16(b)). Compared to the MAGIC-I version, it is completely programmable and houses more functions as the $I P R^{16}$ for measuring the single pixel rate, the DC voltage injector to calibrate the analogue branch and the pattern injector for testing the digital trigger (Fig. 4.16(a)). It is characterized by a very high bandwidth limited at 750 MHz despite the gain of 18.5 dB and a negligible cross-talk ( $0.1 \%$ ). The working range spans from 0.25 to 1150 mV with an $R M S$ noise smaller than $200 \mu \mathrm{~V}$. The programming precision of the pulse width and its delay has been lowered to 10 ps , keeping a huge range respectively of $2.7 \div 12.7 \mathrm{~ns}$ and $0 \div 20 \mathrm{~ns}$. A single board manages 24 channels with a maximum power consumption of 75 W .

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Figure 4.15: Left: the subdivision of the trigger area into 70 groups of pixels. Each group symbolizes a connector/cable at the input of the trigger system. Right: the representation of the 19 trigger macrocells, partially overlapped within the inner part of the MAGIC-II camera. The coloured pixels are blind for the corresponding macrocell with the same colour. (C) F. Dazzi)

The receiver boards are accommodated in four $V M E$ crates and, as the entire $D A Q$ system, they are controlled by a multi-thread $\mathrm{C}++$ software called MIR (Magic Integrated Readout).


Figure 4.16: Left: the block diagram of the receiver board. (Courtesy of M. Barcelo \& J. M. Illa)

Right: a photo of the receiver board $P C B$. (From [124])
The number of cables that connects the receiver boards with the LT1 is increased to 70 units (Fig. 4.15(a)) to include the new channels. The new trigger area has forced the design of a new LT1-backplane, which takes into account the new distribution of the pixels over the macrocells. The board is a fully differential 20 layers $P C B$, where
the lengths of the traces have been notably reduced to around 25 cm respect to the backplane mounted in the first telescope. The performance follows the requirements of the system: it can handle more than 1 Gbps with a low multi cross-talk of $\sim 3 \%$ at the most.
Compact adapters have been introduced between the LT1-backplane and the LT1-boards in order to convert the differential $L V D S$ format into the single-ended $L V T T L$. The LT1boards have been replicated, exchanging only the obsolete $P L D s$ with the new version $E P L D 128 A E T C 100-5$. The TPU, which processes the trigger commands for the $D A Q$, is still the same.

The MAGIC-II data acquisition system is based on an ultra-fast analogue sampler, the so-called DRS2 (Domino Ring Sampler version 2), with a bandwidth of 200 MHz . Its working principle is summarized in figure 4.17(a). The signal charge is stored in 1024 small capacitors ( 200 fF ) arranged in a ring buffer layout. The sampled speed is determined by the clock of a shift register that sequentially enables the capacitors. Currently the clock is fixed at 2 GHz , locked by a $P L L$ synchronization circuitry. When the trigger command arrives, the sampling is stopped and the stored charge is read out at a frequency of 40 MHz . Finally, the voltage is digitized by a 12-bit resolution $A D C$ from Analog Devices (AD9235BRU-65).
A single DRS2 chip can handle up to 10 channels and two of them are integrated in


Figure 4.17: Left: a sketch of the $D R S 2$ principle. The green line holds the ring of inverters that sequentially enable the array of capacitors by means of fast switches (pink area), when a pulse (Domino wave) is injected. The analogue signal (red line) is sampled by the capacitors (yellow rectangles) until a trigger occurs and stops the Domino wave. The stored charge is successively read out at 40 MHz using a shift register. Right: a photo of the mezzanine card that accommodates 2 DRS2 chips (black squares in the centre). (Adapted from [15])
standard card mezzanines (Fig. 4.17(b)). Four mezzanines (80 channels) are plugged into a $9 \mathrm{U} V M E$ general purpose board, called $P U L S A R^{17}$. The $P U L S A R$ board processes the readout sequence and builds a formatted data packet for the recording phase. Through an optical link, the data are transferred to a single computer for the recording on a storage system. The entire system is composed of a set of 14 PULSARs, connected in two VME crates [15].
Two additional PULSARs are utilized for special control tasks. One, named DIGITAL,

[^52]is programmed to measure the arrival time of the trigger command with the aim to synchronize the acquisition on the same event. The second, named BUSY, returns the control to stop the acceptance of further triggers, when the acquisition is still on going. As reported previously, $M I R$ is also the slow control program of the readout system. Differently, the event building by merging data from different PMTs, the data integrity check, the calibration of the Domino chips response and the conversion to the raw data format are performed by another multi-thread C++ program, dubbed DominoReadout [124].

The advantage of this data acquisition system is the compactness, the low cost per channel and the low power consumption, keeping a sampling rate in the GHz domain. The main intrinsic disadvantages are the huge dead time of $512 \mu$ s due to the fact that all the 1024 cells must be read out every time, and both the residual charge effect and the leakage charge in the capacitors.

### 4.7 Calibration system

The calibration of the photosensors and the electronic chain is performed firing the camera with artificial light. A matrix of multi-colours LEDs is the core of the MAGIC-I calibration box, while in $M A G I C-I I$ there is a frequency tripled Neodym $Y A G$ microchip laser, which can be attenuated by a set of attenuation filters. The calibration light emission can be activated in special long runs, mainly used for technical reasons, or interleaved during data-taking for applying a precise scaling coefficient to the real events. Besides that, the calibration system can generate pulses to produce pedestal triggers, namely fictitious triggers to force the acquisition of empty events. This is an estimation of the baseline noise. During data-taking, the calibration system generates typically 25 Hz (calibration) plus 25 Hz (pedestal) of external triggers, so it is possible to keep under control most of the short-term time changes due to temperature, humidity and electronic fluctuations.

The MAGIC-I calibration box contains 64 powerful ( $10^{8} \div 10^{10}$ photons/sr) single quantum well ${ }^{18} L E D s^{19}$ programmable at three different wavelengths: 370 nm (UV), 460 nm (blue) and 520 nm (green) (Fig. 4.18(a)). The circuit, that activates at the most five $L E D s$ in parallel, consists of two avalanche transistors discharging a small capacitance $(33 \mathrm{pF})$ charged at 600 V . A very high current of around 10 A flows through the $L E D s$, discharging the capacitor in a short time. The emitted flash has a duration of about $3 \div 4 \mathrm{~ns} F W H M$.
The $L E D s$ are arranged in 16 slots, four containing the green ones, other four the UV ones and the rest blue $L E D s$. The slots are independently enabled via $G a A s$ analogue switches controlled by a $C A N^{20}$ bus controller. Each module generates between roughly $10 \div 500$ phe per pixel, depending on the colour and the number of $L E D s$. The standard flash, used in the interleaved runs, provides $35 \div 40$ phe.

An interesting feature of the calibration system is provided by the capability to produce continuous light, which simulates the response of the PMTs to the light of the night sky, even with the presence of the moon.

The MAGIC-II calibration system is based on a frequency tripled passively $Q$ Switched $N d-Y A G$ laser, installed at the centre of the dish. The emitted light flash

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Figure 4.18: Left: a sketch of the MAGIC-I calibration system. (From [63])
Right: a simplified scheme of the MAGIC-II calibration box mounted in the centre of the telescope dish.
has a wavelength of 355 nm and an intensity of $2 \mu \mathrm{~J}$, around 50.000 phe per pixel. Its duration is very short, around $700 \mathrm{ps} F W H M$. In front of the laser, there are two filter wheels with 10 attenuator glasses each, which allow up to a linearity calibration of 100 steps, from single to 1000 phe. The light emission homogeneity is then assured by taking advantage of an Ulbricht sphere with Si-diode (Fig. 4.18(b)).
The triggers for the calibration box are produced by a VME pulser board called $T C U$ (Trigger Calibration Unit) located in the counting house. The transmission to the calibration box is split into four RS232 links, managed by an optical multiplexer.

### 4.8 Central control and other subsystems

As previously described, the MAGIC telescopes are composed of different subsystems controlled by independent programs, which do not communicate with each other. A Central Control $(C C)$ software has been developed to coordinate all of them, with a single convenient $G U I$ interface, giving the full control over the telescopes to the operators. Hence, it is at the same time easy and quick to access the detector resources and monitor their status. Moreover, it forces the people on shift to operate the telescopes in an orderly manner and it contains automatic routines, which can be activated to check the correct configuration of the subsystems inside safety limits. For instance, when the humidity is too high or the light too strong, the camera automatically closes. The $C C$ is written in LabView $8.5^{21}$ and runs in a single computer under Linux operating system. A continuous polling at the frequency of 1 Hz keeps the $C C$ updated on the status of the subsystems. The reports are written in $A S C I I$ format and are transmitted over Ethernet using the $T C P / I P$ protocol.
Most of the subsystems are replicated in the telescopes, sometimes completely, other

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Figure 4.19: Flow diagram of the $M A G I C$ telescopes Central Control program. (Adapted from [137])
times only in functionality (in which case the specific software is adapted). For the drive systems the programs are called Cosy-1 and Cosy-2, for the active mirror control they are called $A M C-1$ and $A M C$-2, for the camera they are Guagua and Caco2 and for the readouts they are MuxDaq and DominoReadout. The calibration is included in Guagua in MAGIC-I or in MIR in MAGIC-II.
There are still few single subsystems that are common for both telescopes.

* Pyrometer: a system that measures the radiation, the temperature of the sky and the humidity, extrapolating the atmosphere conditions. This device is installed on the left side of the MAGIC-I dish and it is controlled via $R S$-232 protocol.
* Lidar: a device that estimates the differential atmospheric absorption and scattering losses along the light path. It is composed of a pulsed ( 1 kHz ) fast laser (source), a small optical telescope (photons concentrator) and a high quantum efficiency $H P D$ (detector). The Lidar requests the telescope coordinates to the $C C$, then it moves in that direction, takes data and reports the atmospheric parameters back to the $C C$.
* GRB alert: this program monitors the GCN (Gamma-ray burst Coordinates Network) messages and reacts to any interesting $G R B$ alert. The $C C$ is immediately noticed and the telescopes could be repositioned using the fast drive movement.
* Time stamp: the time stamp for the readout is provided by two autonomous
clocks, which are continuously compared through a NIM module. One comes from a $G P S$ receiver, the other from a rubidium atomic clock. The data transmission is sustained by a serial $R S 232$ connection.
* Weather station: it is a high quality steel Reinhardt MWS 5MV microprocessor with data logger. The data are sent via a serial connection and recorded onto a file shared with the $C C$.


### 4.9 The MAGIC upgrade

An upgrade is in progress ${ }^{22}$ with the main aim to have both telescopes identical, with some renewed subsystems, simplifying the controls, the analysis chain and the maintenance. The plan contains four main topics:

* The upgrade, with the new chip DRS4, of the data acquisition systems in both telescopes.
* A new LT1 system for MAGIC-I equal to MAGIC-II.
* Rearrangement and renovation of the electronic and computer rooms.
* A new camera for MAGIC-I equal to MAGIC-II.

The most important part of the upgrade involves the data sampler. The limitations of the DRS2 chip will be eliminated by the new version $D R S 4$. First, the dead time has been reduced of a factor 10, because it is possible to record only the region of interest ( $R O I$ ) where the analogue pulse lies. Secondly, the new chip is quite linear and not strongly temperature dependent. Furthermore, the introduction of the differential technology makes it immune to common noise. The resulting chip is more stable, especially in terms of noise. Finally the bandwidth of the new mezzanine, which hosts $3 \mathrm{DRS}_{4}^{23}$, has been increased to around $600 \div 700 \mathrm{MHz}$.

A LT1 system, with an enlarged area as in MAGIC-II, has been prepared. A single improvement has been done: the LT1-backplane routing has been redone paying attention to the signal integrity and has a lower skew. The result is a maximum skew of 360 ps with an $R M S$ of only 67 ps .

The motivation to renew the electronic room is driven by the necessity to place the new electronics, based on the $D R S 4$, in a temperature controlled and clean environment. The racks are kept closed and the internal temperature is stabilized by a powerful cooling system. The computers have been moved in a adjacent room, with another independent cooling system. The floor of the room has been covered by an antistatic paint to prevent the deposit of dust.
Moreover, the arrangement of the racks has been studied to both minimize the propagation time of the local triggers (see subsection 6.3.1 for more details) and to facilitate the access and maintenance to the electronics (Fig. 4.20).

The main design of the new camera is basically equal to that one mounted on MAGIC-II. Some mechanical changes are mandatory because the structures of the two telescopes are slightly different. In addition, even the entrance window has been refined, supporting the plexiglas in four isostatic floating pins. The electronics of the pulse injector system has been modified, improving the signal stability, fundamental to

[^55]

Figure 4.20: A temporal sequence of the renovation of the electronic room. (Images credit: J. L. Lemus)
perform reliable test during the day. The only parts completely redesigned are the low power boxes, metal containers that host the low power supply and its control for the whole camera. They will be changed in both telescopes.

## 5

## The Sum-Trigger-II

NE OF THE main goals of the new generation IACT telescopes, is to lower the energy threshold in the unknown, but promising, domain under 50 GeV . In 2007, MAGIC already succeeded in this sense, developing an innovative analogue trigger able to operate down to 25 GeV . For the first time, the Pulsar Crab nebula was detected in the gamma field, opening a new window to amazing physics. That system was designed as a prototype to demonstrate the feasibility of the technique, and no effort was applied in terms of reliability, stability and resilience. In this chapter, a professional new analogue trigger, which is an evolution of the old system, is presented. Obviously, a quick introduction is dedicated to the prototype Sum-Trigger as the starting point of the new project, called Sum-Trigger-II.

### 5.1 The original Sum-Trigger

Gamma-ray induced showers are strongly concealed by hadrons and $N S B$ light. The current IACT telescopes take advantage of special trigger techniques to get rid of the dominant background processes. However, these techniques considerably reduced the rejection power and the efficiency of observation, lowering the event size. This has greatly limited the energy threshold, preventing new prospects in the observation of Pulsars, distant $A G N s$ and $G R B s$.
As explained in chapter 3, the Čerenkov photon distribution of low energy events, in the camera plane, is complex and not easy to parametrize. The total amount of light is very poor and often not well concentrated in just a few neighbouring pixels. The technological solution, proposed by the MAGIC collaboration, tried to relax the topological constraints and, at the same time, to minimize the acceptable time gate.
In October 2007, a prototype Sum-Trigger was installed on MAGIC-I. It had a dedicated electronic path, independent of the standard trigger, allowing an easy integration and commissioning.

### 5.1.1 Sum-Trigger description

The basic principle of the analogue trigger was to add neighbouring pixels belonging to a small area (macrocell) and then apply a threshold to the final signal (Fig. 5.1). This changed the sequence present in the standard digital trigger, where first the individual channel is digitalized and subsequently the selection algorithm enters into play. In the

Sum-Trigger, even very small events, below the standard digital threshold, participated in the final decision.
This reversal approach favoured the contribution of all the pixels hit by the Čerenkov


Figure 5.1: The principle of the original Sum-Trigger installed in MAGIC-I in 2007. 18 clipped channels from a macrocell are added and then digitalized. The camera is subdivided by 24 partially overlapped macrocells. The output trigger is the OR function of these macrocells. (C) F. Dazzi)
light, even if they were not necessarily connected. In fact, inside a macrocell every distribution of photons was considered and processed. Furthermore, it increased the signal to noise ratio ${ }^{1}$ and relaxed the strong topological constraint of the standard trigger to request, at the same time, a group of close compact pixels above threshold. To keep a low noise rate, even if any particular shape restriction was applied, the Sum-Trigger used a narrow effective coincidence time between pixels of around 3 ns , sufficiently small since the spread time of a low energy $\gamma$-ray event is below 3 ns . A pulse width of this dimension optimized the trigger efficiency and so the discriminator threshold could be pulled down without being dominated by Poissonian fluctuations of the $N S B$. Monte Carlo studies have revealed that the best summation threshold should stay in the range $25 \div 30$ phe [111].

This idea is simple to apply, but it is affected by the intrinsic $P M T$ spikes, called afterpulses. The main cause of afterpulses is an imperfect vacuum sealing of the tube. Residual molecules, staying between the cathode and the first diode, can be ionized by collision with electrons. Then, these ions are accelerated backwards by the electric field and when they strike the photocathode, additional electrons are generated. The result is a huge noise pulse, following the primary signal pulse (Fig. 5.2(a)).
As shown in figure $5.2(\mathrm{~b})$, the afterpulses became relevant above $\sim 7$ phe and still maintained a rate of some hundreds hertz above 25 phe. This prevented the use of the Sum-Trigger as a simple analogue sum of adjacent PMTs, for the detection of faint events that require a low threshold. The adopted solution was to clip every signal at the amplitude of $6 \div 8$ phe, just before the summation stage. The signal cuts did not affect the gamma events, but rejected the afterpulses (Fig. 5.3).

Several trigger configurations and different overlapping regions were simulated to obtain the largest collection area and the lowest trigger threshold. The final layout covered a ring between $0.26^{\circ} \div 0.86^{\circ}$ in the camera, for a total of 216 pixels (Fig. 5.4(a)). This was a compromise between a simplified electronic design and the maximized distribution of Čerenkov photons between 20 and 30 GeV , which is of the order of $80 \%$ in this

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Figure 5.2: Left: a record of the $P M T$ afterpulse signal shape at the input of the SumTrigger. It is a narrow signal of $\sim 2 \mathrm{~ns}$. (Courtesy of M. Shayduk)
Right: the count rate above a discriminator threshold for a single PMT exposed to $N S B$ (black points). The red crosses denoted the simulation with a $N S B$ level of 0.18 phe/ns. The afterpulse trend matches with an exponential threshold spectrum, which extends beyond the $N S B$ curve. (Adapted from [112] and [65])


Figure 5.3: A scheme of the clipping principle. The blue signals come from Čerenkov events, while the red ones are $P M T$ afterpulses. Dashed curves represent the continuation of the pulse, if the clipping is not applied (green line). The blue pulses are synchronous and their addition exceeds the discrimination threshold (brown line). The red pulses are not correlated in time, and after the clipping they do not activate the trigger. (From [65])
region. The overlap required each $P M T$ to lie inside two different macrocells. Hence, every macrocell of 18 pixels was divided in 3 sub-macrocells of 6 elements (Fig. 5.4(b)), which were shared with another macrocell.

The electronic system, as shown in figure 5.1 with different colours, was divided in four main stages.
(1) Clip stage (orange). There were 27 Clip-boards with eight input channels each.
(2) Sum stage (yellow). This stage was divided into two different kind of boards. There were 36 boards to add signals inside every sub-macrocell, providing three


Figure 5.4: Left: the Sum-Trigger area (salmon) and the macrocell shapes (other colours). Right: the sub-macrocells are displayed. Each macrocell consists of 3 sub-macrocells with 6 PMTs each. One macrocell is underlined with a thick blue line, another with a thick yellow line and finally other two with thin black and brown lines. (Adapted from [111])
output copies for the macrocells' overlap. Then, in other 24 boards, the results of three sub-macrocells were piled up.

3 Discriminator stage (violet). The same boards that hosted the second sum stage, managed this function. Once the signals belonging to a macrocell were added, a programmable discriminator threshold was applied.
(4) OR stage (green). There was a single board to generate the final trigger from the OR of 24 discriminator stage outputs.

### 5.1.2 Sum-Trigger advantages and limitations

The aim of the Sum-Trigger was to lower the energy threshold, recording events in the domain under 50 GeV , where the standard digital trigger was not so efficient. The SumTrigger was built with a meticulous fine tuning, while the standard trigger, to this day, is configured in a conservative way. The most evident discrepancies between the sum and digital trigger were the effective coincidence gates, respectively $\sim 3 \mathrm{~ns}$ and $\sim 6 \mathrm{~ns}$, and the trigger rates, $\sim 250 \mathrm{~Hz}$ and $\sim 800 \mathrm{~Hz}$. The trigger rate is inversely proportional to the trigger threshold, which was so low for the Sum-Trigger that about $50 \%$ of the recorded events were NSB.
In figure 5.5(a), it is possible to compare the trigger threshold, as the energy distribution peak of a $\gamma$-ray source with a spectral index of -2.6 , for both systems. The energy threshold went down by about a factor of two, while the rate was boosted by $50 \%$. The higher sensitivity at low energies is shown in the plot 5.5(b). This is not the case for energies above 200 GeV , where the wider area of the digital trigger dominates.

The Sum-Trigger manifested excellent performance, although it was a prototype with many limitations. Following a list of drawbacks is reported.

* The trigger area was small and did not allow the telescope to be run in wobble mode ${ }^{2}$. This doubled the data-taking duration, because the time slot was shared

[^57]

Figure 5.5: Left: the differential rate for simulated $\gamma$-rays with a power law spectral index of -2.6 , using the standard digital trigger and the Sum-Trigger, both in mono configuration. The peaks of the distributions represent the energy thresholds, 55 GeV for the digital trigger and 25 GeV for the analogue one. Right: the collection area for the two systems. (From [111])
out between the ON (source) and OFF (background). Moreover, a wider trigger region increases the collection area.

* The channel delays adjustment was made by hand, adding cables with different lengths. This method was very time-consuming and not so precise. The adjustment resolution was determined by the minimum cable step of 0.5 ns . The process was done once at the beginning of the system set-up and never repeated due to the cable-routing complexity. This caused a continuous and unavoidable decline of the signals' synchronization.
* The signals' amplitude equalization was performed manually using the oscilloscope. It was a time-consuming and inaccurate measurement, renewed very rarely, about once per year.
* The lack of an automatic and fast amplitude equalization, made it impossible to perform independently both the pixels charge flat-fielding and the PMTs replacement. The operation was authorized only just before the Sum-Trigger annual maintenance.
* The system layout is very far from being compact and the accessibility to the boards is problematic.

The system operated very well for a couple of years, showing the feasibility of this innovative idea for a single telescope configuration. The defects described above have compromised a long and extensive deployment of the instrument, but have opened a lot of room for further improvements.

### 5.1.3 Physics discoveries

The Sum-Trigger was employed to detect Pulsars and to monitor distant $A G N s$, such as for instance the BL Lac object $P G 1553+113$. However, the analysis chain was only optimized for Pulsar studies, so the main discovery has been related to the Crab Pulsar [36]. A good data set was collected between October 2007 and February 2008 for a total
amount of 22.3 hours. The achieved low energy threshold enabled an interesting comparison with data measured by satellite detectors, leading to elaborate and interesting discussions on the best theoretical scenario. As explained in 1.4.2, the spectrum cut-off changes depending on which model of Pulsar emission is taken into consideration. The Polar cap predicts a super-exponential cut-off around some GeV , while the Outer gap foresees an exponential cut-off at higher energies. Therefore, detection of $\gamma$-rays above 10 GeV would allow one to discriminate between different Pulsar emission mechanisms. The detection of the pulsed signal from Crab Pulsar has demonstrated that the spectrum extends into the GeV domain, favouring $\gamma$-ray production far away from the neutron star surface, as in the Outer gap model [35]. A joint fit is performed on the MAGIC and EGRET data with the following generalized function:

$$
\begin{equation*}
f(E)=A E^{-a} \cdot \exp \left[-\left(\frac{E}{E_{0}}\right)^{\beta}\right] \tag{5.1}
\end{equation*}
$$

where $A$ is a normalized constant, $E_{0}$ is the cut-off energy, and $\beta$ measures the steepness of the cut-off. Figure 5.6(b) shows all three fitted functions for $\beta=1$ (red line), $\beta=$ 2 (blue line), and the best fit, $\beta=1.3$ (green line). In figure 5.6(a), the associated


Figure 5.6: Left: the shaded areas show the signal regions for $P 1$ and P2. They are in phase for all shown energies and the ratio of P2/P1 increases with energy from (d) to (a). Right: the Crab Pulsar spectrum. The solid circles and triangles represent flux measurements from $E G R E T$, while the arrows on the right denote upper limits from various previous experiments. The black line indicates the energy range, the flux and the statistical error of MAGIC measurement. The yellow band illustrates the joint systematic error of all three solutions. (From [35])
pulse phase diagram shows the pulsed signal in 11 bins for $\gamma$-ray events above 25 GeV and the counterparts in the $H E$ and optical range. The optical emission was measured simultaneously by MAGIC in winter 2007-2008, using its central pixel. The overall
obtained significance was $6.4 \sigma$, with $8500 \pm 1330$ events. The main pulse (P1), at phase zero, had a significance of $4.3 \sigma$, while the inter-pulse ( $P$ 2) , at phase around 0.4 , had a significance of $7.4 \sigma$.

Data taken in the winter 2008-2009, which did not manifest a significant yearly variability, were combined with data from the previous year and compared with the energy spectra measured by the Fermi-LAT instrument [29]. The results revealed that the spectrum is not compatible with an exponential cut-off, but its trend followed a power law [39]. Considering the event excesses in both P1 and P2 (Fig. 5.7(a)), the function which best describes data is a power law:

$$
\begin{equation*}
f(E)=F_{30}\left(\frac{E}{30 \mathrm{GeV}}\right)^{-\Gamma} \tag{5.2}
\end{equation*}
$$

where the best parameters are $\mathrm{F}_{30}=(14.9 \pm 2.9 \mathrm{stat} \pm 9.6 \mathrm{syst}) \times 10^{-9} \mathrm{~cm}^{-2} \mathrm{~s}^{-1} \mathrm{TeV}^{-1}$ and $\Gamma=3.4 \pm 0.5$ stat $\pm 0.3$ syst. This fit was inconsistent with any standard pulsar model.

(a) The Crab pulsed emission adding data of winter 2008 2009

(b) The new computed Crab Pulsar spectrum

Figure 5.7: Left: the pulse profile of the Crab Pulsar adding the new data set of winter 2008-2009. The red shaded area indicates the signal phases P1 and P2, while the black shaded area indicates the background control phases. Right: the energy spectra P1 + P2. The black solid line and dots are obtained from the public Fermi-LAT data, while red points denote the MAGIC measurements. The pink line and a butterfly shape indicate the power law fit to the MAGIC data and its statistical uncertainty. The gray shade with a black line and open diamonds show the VERITAS measurements. The dotted line is the combined fit above 5 GeV . (From [39])

The recent announcement of signal from the Crab Pulsar above 100 GeV [43], by the VERITAS collaboration, has consolidated the MAGIC position in favour of a spectrum described by a broken power law with $\gamma$-ray production more than ten stellar radii away from the neutron star. The extended fit in figure 5.7(b), seems to be in agreement with the new VERITAS data. Nevertheless, it is important to verify this assumption by an in-depth study in the overall VHE domain or eventually foresee the presence of another component above 100 GeV , as announced by MAGIC in a recent publication [38]. For this reason, a higher sensitivity is essential, as well as a wide dynamic range and a low energy threshold, all of which could be provided by a stereoscopic analogue trigger system.

Thank to these promising outcomes, which stimulate new investigations, it has been decided to upgrade the original Sum-Trigger, including a new one for the MAGIC-II telescope.

### 5.2 The Sum-Trigger-II system

Several reasons urged the MAGIC collaboration to develop a revised stereoscopic SumTrigger. The first was the poor reliability and difficulty to adjust the original SumTrigger which necessitated both a complex manual tuning and constant maintenance. An improved automatic computer control ${ }^{3}$ is essential to calibrate the system and precisely adjust its settings. Another reason was the desire to improve the telescopes' performance at very low energies, where Pulsars, distant $A G N s$ and $G R B s$ can provide fundamental information relating to extreme acceleration mechanisms and exotic physics. A more precise signal synchronization and a higher bandwidth favour a better topological and temporal selection of faint events. Last, but no less important, a larger trigger area similar to the standard trigger was considered to be essential.
The project of the new Sum-Trigger-II, at the same time, tries to sort out the weak points of the old system and to improve its functioning, in order to ensure new useful results.

### 5.2.1 Sum-Trigger-II simulation

At the beginning, different designs were taken into account in order to find the best compromise between performance, costs, complexity and easy integration into the preexisting electronic chain. The decision is based on the comparison of the energy distribution for different numbers and layout of the macrocells in the camera. The choice of the most reasonable arrangements is forced by the request to cover, as much as possible, the same area as the standard digital trigger, which imposes the cabling that can be put in place.
The preference for the single macrocell dimension is dictated by Monte Carlo studies, which demonstrate that about 20 pixels are optimal in the energy range of $10 \div 30 \mathrm{GeV}$ [111]. In fact, involving few pixels increases the probability of losing part of the faint Čerenkov flash, while conversely a larger macrocell might be dominated by accidental triggers. The hexagonal shape is the preferred one, because it guarantees both a symmetrical overlap and a central symmetry. In most of the simulated configurations, the macrocell is defined as a hexagon of 19 pixels.

Five possible macrocell mappings have been analysed with the MAGIC standard simulation program (CameraSim) (Table 5.1). The first mapping (Fig. 5.8(a)) is the

| Name | Nr. <br> macrocells | Nr. pixels <br> in macrocell | Macrocell <br> shape |
| :---: | :---: | :---: | :---: |
| Sum_mapping_V1 | 37 | 19 | Hexagon |
| Sum_mapping_V2 | 47 | $19(18 ; 17)$ | Hexagon |
| Sum_mapping_V3 | 46 | 19 | Hexagon $+\left(^{*}\right)$ |
| Sum_mapping_V4 | 55 | $19(15)$ | Hexagon |
| Sum_mapping_V5 | 51 | $19(18 ; 17 ; 15)$ | Hexagon |

Table 5.1: The main properties of the studied trigger configurations for the Sum-Trigger$I I$. The first column indicates the configuration's name, the second the total number of macrocells that compose the mapping and the third one shows the number of pixels inside a macrocell. Sometimes the number could be lower (in brackets), if the macrocell exceeds the standard trigger layout.
$\left(^{*}\right)$ : it is an irregular polygon, designed to obtain a complete overlap.

[^58]

Figure 5.8: The five simulated mapping configurations. The full coloured pixels are outside the standard digital trigger area and cannot be routed in the Sum-Trigger-II. (© F. Dazzi)
simplest layout, with only 37 macrocells. It shows a nice circular symmetry, but the overlap is very poor (Fig. 5.9(a)), limited to one pixel. The second mapping (Fig. 5.8(b)) increases the number of macrocells to 47, in order to improve the common regions (Fig. 5.9(b)). The macrocells' arrangement follows the digital trigger numbering path, resulting in a global shape, which is a little bit asymmetric. The fifth version (Fig. 5.8(e)) is simply an upgrade of the previous one, where four macrocells are added on the top and bottom side with the aim to obtain a more circular shape and a homogeneous overlap of the trigger area (Fig. 5.9(e)). The main source of inspiration for the third layout (Fig. 5.8(c)) is to have a complete and equally distributed overlap (Fig. 5.9(c)). The unavoidable drawback is the resulting odd shape, consequent to the irregular polygon used in addition to the hexagon. Finally, the fourth mapping (Fig. $5.8(\mathrm{~d})$ ) tries to cover the digital trigger area with a precise circular symmetry. The final shape provides a good and regular overlap (Fig. 5.9(d)), but it needs the highest number of macrocells: 55.

The first simulated parameter is the number of triggered gamma events as a function of the energy (Fig. 5.10(a)). All layouts offer very similar detection capabilities within $\sim 1 \%$, and a very close distribution peak (trigger threshold), in the interval $20 \div 25 \mathrm{GeV}$. However, the Sum_mapping_V2 (consequently Sum_mapping_V5 too) and the Sum_mapping_V4 are slightly better, especially in terms of energy threshold, which is lowered to 20 GeV .
The second study verifies the trigger efficiency with a fixed standard clipping of 6 phe and a variable final sum threshold between 25 and 29 phe (Fig. 5.10(b)). Even in this case, the difference is minimal, but again always a little bit in favour of the second and fourth version.
The last investigation treats the spatial trigger response homogeneity. The centre of


Figure 5.9: The overlap of the five simulated mapping configurations. The colours show the overlap size between macrocells. (Images credit: M. Lopez \& J. L. Lemus)


Figure 5.10: Left: the energy distribution for gamma events using different macrocell layouts. The peak of the curve corresponds to the energy threshold. The electronic parameters are 6 phe for the clipping level and 27 phe for the final threshold. Right: the trigger efficiency as a function of the final applied sum threshold in the range $25 \div 29$ phe. The clipping level is fixed at the standard value of 6 phe. (Images credit: M. Lopez).
gravity $(C o G)$ distributions of the triggered events are outlined in figure 5.11. Obviously, a circular mapping assures a rotational symmetry, which is the best geometry for the wobble data-taking and from the analysis point of view.

The best solution seems to be the Sum_mapping_V4, having the highest number of macrocells. However, the mechanical layout and the electronic scheme do not change


Figure 5.11: Left: the simulation of the mono $C o G$ using the Sum_mapping_V4 and applying a size cut at 40 phe. Centre: the same plot as before, but with a cut in size of 200 phe. Right: the stereo $C o G$ with again a cut at 200 phe. (Images credit: T. Schweizer \& E. Prandini).
significantly up to 57 macrocells, thanks to the introduced modular design. It could be argued that the Sum_mapping_V1 is composed of $33 \%$ less macrocells ( 37 vs 55 ) and offers similar performance, thus reducing the production time, the routing complexity and the cost of the components. However, the limited overlap makes it too sensitive to the dead pixels. For these reasons, Sum_mapping_V4 was selected for the final design.

In the Sum_mapping_V4, each macrocell is surrounded by six other macrocells, equally disposed every $60^{\circ}$. It can be divided in three layers, two out of three with the same shape, but a different rotation (Fig. 5.12). It is comprised of 529 channels, which become 997 after the splitting due to the macrocells' partial overlap. Some parameters of the selected mapping are reported in table 5.2.


Figure 5.12: The three layers of the Sum_mapping_V4. The layers number 2 and 3 present the same arrangement, but a different orientation. The full coloured pixels are outside the standard digital trigger area and cannot be connected. (C) F. Dazzi)

It is fundamental to compare the performance of the new Sum-Trigger-II versus the old one. In order to find the best configuration for the selected mapping, the $N S B$ influence has been analysed by scanning a high number of setting combinations. The program used is called CameraSim ${ }^{4}$, which simulates the reflector, the photosensors and the electronic chain of the telescopes.
The accepted accidental rate was fixed at 400 Hz , because the global mono trigger rate,

[^59]| Sum_mapping_V4 parameters |  |
| :--- | :---: |
| Total pixels | 529 |
| Blind pixels | 48 |
| Total pixels after the split stage | 997 |
| LT1 pixels not covered | 30 |

Table 5.2: Some important parameters of the selected configuration Sum_mapping_V4.
including the cosmic ray contribution, will be around $800 \div 900 \mathrm{~Hz}$, a little bit less than the $D A Q$ saturation limit. As for the old system, the best clipping level and the sum threshold still remain confined around respectively 6 phe and 27 phe.
Subsequently, a gamma source with spectral index - 2.6 has been simulated at low energies and the events have been processed by CameraSim, configured with the new extrapolated threshold. For the time being, the clipping level is left as a tunable parameter. Finally, the energy distribution of triggered events (Fig. 5.13(a) \& Fig. 5.13(c)) and the collection area (Fig. 5.13(b) \& Fig. 5.13(d)) are computed for the old and the new Sum-Trigger-II.
Considering, for instance, the green curves (clipping at 6 phe), the energy threshold


Figure 5.13: Top left: the simulated differential rate of the old Sum-Trigger for a $\gamma$-ray source with a power law spectral index of -2.6 . The peak of the distribution represents the energy thresholds: $\sim 25 \mathrm{GeV}$. This plot is a repetition of figure $5.5(\mathrm{a})$, but obtained with the new program CameraSim. Top right: the collection area with the same conditions of the adjacent figure. Bottom left: the differential rate of the new Sum-Trigger-II. The energy threshold is around 20 GeV . Bottom right: the collection area of the new analogue trigger. (Images credit: M. Lopez).
is lowered by $20 \%$, that is from 25 GeV to 20 GeV . The fraction of triggered events is
more than doubled, especially in the range $10 \div 40 \mathrm{GeV}$. Moreover, the collection area shows promising results too. At 20 GeV it is doubled from $\sim 12000 \mathrm{~m}^{2}$ to $\sim 25000 \mathrm{~m}^{2}$. It is very interesting to see that the collection area still continues to be more efficient at standard energies, above 100 GeV .
In stereoscopic data-taking mode, the performance of the new Sum-Trigger-II seems even better. In figures 5.14(a) and 5.14(b), the energy distribution and the collection area for the stereo mode are shown. Assuming an analogue pulse width of 3 ns , a


Figure 5.14: Left: the simulated differential rate of the stereo Sum-Trigger-II for a $\gamma$-ray source with a power law spectral index of -2.6 . The peak of the distribution represents the energy thresholds: $\sim 17 \mathrm{GeV}$. Right: the collection area with the same conditions as in the adjacent figure. (Images credit: M. Lopez).
stereoscopic trigger gate of 70 ns and an accidental rate of 50 Hz , the results are quite impressive. The energy threshold is lowered to $\sim 17 \mathrm{GeV}$ and the number of trigger events is increased by $25 \%$ in respect of the mono data-taking. Finally, the collection area becomes more than three times larger than the prototype system, namely $\sim 40000 \mathrm{~m}^{2}$ at 20 GeV .

The conclusion is that the extended Sum-mapping_V4 layout, composed of overlapping hexagonal macrocells, ensures a slightly lower energy threshold and in addition a much higher number of triggered events. This means that the time required to detect a source will be considerably reduced.

### 5.2.2 System overview and subsystem description

The main concept of the Sum-Trigger-II project is identical to the previous version. The flow chart is reported in figure 5.15. The signals (green pulses) are originated in the camera, which is divided into 55 partially overlapping macrocells of 19 PMTs. The analogue pulses are first synchronized and equalized in amplitude, then are clipped to reject the PMT afterpulse noise. This is done in the boards dubbed Clip-boards (paleorange). Later on, the pulses belonging to a macrocell are added and compared with a programmable threshold, as in the original system. These functions are performed in the boards called Sum-boards (orange). The part relevant for the control, processing and interface has been completely redesigned and exhibited in blue. The main board is called Astro-board, which receives the discriminator's output and splits it in three paths. One goes to the global OR trigger, another to the single macrocell counting unit and the last one to a D flip-flop to verify the pulse arrival times with respect to the reference signal. Finally, the data are downloaded and analysed by a dedicated computer, which then uploads the proper parameters.

The implementation of the programmable analogue delay lines and attenuators in the


Figure 5.15: The principle of the new Sum-Trigger-II. (C) D. Häfner \& F. Dazzi)
Clip-board is completely innovative. Another important upgrade is made in the control and processing stage, which is more powerful and automated.

The system is very compact and based on modular boards, which can be easily exchanged and swapped. It fits in an 18-crate unit, where the top side is assigned to the 18 Clip-boards and the Astro-board. The bottom is designated to the 19 Sum-boards (Fig. 5.16(a)).
The fast analogue pulses come from the receiver boards, where dedicated mezzanines (Sum-mezzanine) are plugged to interface with the Sum-trigger-II system. The signals travel for 5 m , before reaching the Clip-boards. Here, they are synchronized using programmable analogue delay lines, equalized in amplitude using programmable attenuators and clipped using amplifiers with programmable clamp thresholds. Finally, each signal is split three times to ensure the required overlap between different macrocells (top left in figure 5.16(b)).
Afterwards, each signal must be connected to the assigned macrocells, through a com-


Figure 5.16: Left: the frontal view of the Sum-Trigger-II crate. In the upper part, the 18 Clip-boards and the Astro-board (yellow) are shown. In the lower side, there are the 19 Sum-boards. Right: the lateral view of the crate. In this sketch, the connection between the Clip-boards and the Sum-boards through the Sum-backplane is emphasized. (C) F. Dazzi)
plete passive backplane, so-called Sum-backplane, which works as an interface between the Clip-boards and the Sum-boards. Here, the analogue summation of 19 pixels is gen-
erated (on the bottom of figure 5.16(b)) and compared to a programmable threshold. When exceeded, a trigger is sent to the Astro-board for the global OR (Fig. 5.17(b)). Each Sum-board manages three macrocells.


Figure 5.17: Left: the frontal view of the bus for the control of the Clip-boards and Sumboards parameters. Right: the lateral section of the Astro-board, located in the top right side of the crate. This board, with the assistance of the software control, prepares and sends the configuration data through the SPI-backplane and the Sum-backplane. (C) F. Dazzi)

All the programmable parameters, such as delays, attenuations, thresholds, macrocell trigger counters and global trigger $O R$ are in the charge of the Astro-board and a dedicated computer.
Commercially available $A D C s^{5}$ and $T D C s^{6}$ are the optimal solution for measuring the signals' amplitude and their arrival time, but the global cost for the implementation is prohibitive. The alternative simple solution, adopted in the Astro-board, is based on the coincidence rate of the signal under test and a reference one ${ }^{7}$. This approach requires a quite long iterative procedure, but it can be done with a basic circuitry, disposed in a compact area.

The Astro-board and the Sum-boards communicate by means of a parallel bus in the Sum-backplane, while the data transmission with the Clip-boards passes through the SPI-backplane ${ }^{8}$ (Fig. 5.17(a)).

### 5.2.2.1 Mechanics layout

The electronic system is accommodated in a Schroff composite crate of the EuropacPRO series. Every metal piece and all the additional attachments are designed for a complete shielding against electromagnetic noise and to avoid electrostatic discharges. Furthermore, even the shielding to the front of the crate is achieved by electromagnetic-

[^60]compatible textile gaskets, glued on the left side of the panel profiles with temperatureresistant adhesive. Their semi-spherical shape allows a good metal continuity and their CuNi coating guarantees high shielding for a long time, typically 40 dB at 2 GHz .
The structural layout and some important dimensions are documented in figure 5.18. The power supplies are laid on the back, very close to the Sum-Trigger-II boards, but in distinct cases. Their position can be regulated on site to obtain the best connection to the electronic devices and an easy accessibility during maintenance.


Figure 5.18: The mechanical overview of the Sum-Trigger-II crate and the power supply modules. All the blocks in red are electronic boards, while the connectors are indicated in yellow. The metal components are coloured in blue. The power supply position can be modified to optimize the arrangement on site. (Image credit: D. Corti \& A. Bortoluzzi)

Below the crate, a 2U fan system (Schroff LE2 60713-002) is installed. This is a high-air capacity tangential blower, which produces a flux of $330 \mathrm{~m}^{3} / \mathrm{h}$ (Fig. 5.19(a)). This facilitates the air flow to regulate the correct stable temperature.


Figure 5.19: On the left photo, the blower located on the bottom of the Sum-Trigger-II crate. On the right, one power module used to supply the Sum-boards ( $\pm 5 \mathrm{~V}$ ).

The power system is divided in two parts. The first feeds the Clip-boards, recycling the old power switching modules (Lambda JWS600-5 \& JWS600-3) of the former

MAGIC-I racks. The nominal output voltage is respectively 5 V and 3.3 V , for a maximum current of 120 A . The dominant noise is the voltage output ripple, which is always below 70 mV in $A C$ mode. Considering also the common mode, the noise tolerance should be extended to 150 mV .
The second feeds the Sum-boards and it consists of two low-noise switching power supplies (Fig. 5.19(b)). They are provided by Power Control Systems company, model S402-P. Each module delivers 5 V for a maximum of 100 A with a maximum noise and ripple level of less than 50 mV . The ground of the first power pack is connected to the positive of the second, to deliver $\pm 5 \mathrm{~V}$.

### 5.2.2.2 Sum-mezzanines and FCl cables

The Sum-mezzanine is the interface between the Samtec $Q M S S$ output connector of the receiver board and the FCI cables ${ }^{9}$, which are connected to the Clip-board on the other end. Each receiver board can accept up to 24 optical fibres from the PMTs, so the Sum-mezzanine output stage is divided into three $F C I$ connectors ${ }^{10}$ with 8 differential channels each (schematics in appendix A).
The mezzanine is an eight-layer $P C B$ with the traces routed internally to reduce the noise effect. The differential wires have an impedance of $100 \Omega$ and their length is equalized inside 1.5 mm , namely $\sim 10 \mathrm{ps}$.


Figure 5.20: Left: the top and bottom side of the Sum-mezzanine board. Right: the mezzanine connected to a receiver board (Medusa version).

The main design constraint is to preserve the features of the fast analogue signal, $\sim 2.6 \mathrm{~ns} F W H M$, which determines the right pile-up. This implies high bandwidth electronics, high signal integrity, low cross-talk and very low skew between channels. To measure these parameters, a simple set up has been prepared with the following devices.

A pulse generator HP 8082A.
A VCSEL laser transmitter with a DC current of 3 mA .
An optical fibre 1 m long with $L X 5$ connectors.
One receiver board (Medusa version).

[^61]One Sum-mezzanine (Version 1.1).
A FCI cable 5 m long (Fig. 5.21(a)).
An adapter board from FCI to SMA (Fig. 5.21(b)).
An oscilloscope Tektronix DPO 7354 with a bandwidth of 3.5 GHz and a sample rate of $40 \mathrm{GS} / \mathrm{s}$.


Figure 5.21: On the left photo, the FCI 10054999-N0500AULF cable and connectors. On the right, a photo of the adapter board used to read the signals from the $F C I$ cable with an oscilloscope.

The output signal is shown in figure $5.22(\mathrm{a})$. Its quality is very high, neither oscillations nor noise are visible and the positive and the negative components are perfectly synchronized. The rise time of the pulse ( $\sim 1.3 \mathrm{~ns}$ ) is a little bit larger than the typical value obtained from the camera $P M T s$, because it is limited by the generator slew rate and the receiver output bandwidth of $\sim 300 \mathrm{MHz}$. In fact, it is very similar to the rise time of the input signal.
It is not possible to quantify precisely the cross-talk, because it is so small that it is


Figure 5.22: Left: the analogue differential signal at the end of a test chain composed of a pulse generator, a laser injector, an optical fibre, a receiver board, a Sum-mezzanine, a $F C I$ cable and an adapter $F C I$ to $S M A$. The yellow pulse is the positive, the blue one the negative, while the orange is their subtraction. Right: the maximum cross-talk between two close channels.
dominated by the electronic noise. In figure $5.22(\mathrm{~b})$, the aggressor signal amplitude is

84 mV and the victim's response seems to have no cross-talk. The electronic noise level is around $\sim 3 \div 3.5 \mathrm{mV}$ peak-to-peak, even in other channels with higher amplitude, up to 100 mV . We conclude that the cross-talk is lower than $3 \%$.

The FCI cable is designed for high-speed transmission over long distances. Its low profile allows a compact cable routing, even in a very dense system, such as Sum-Trigger-II. It can work perfectly up to $2.5 \mathrm{~Gb} / \mathrm{s}$, keeping an excellent signal integrity performance and an independent pair shielding. Other important characteristics are listed in table 5.3.

| FCI CABLE SPECIFICATIONS |  |
| :--- | :--- |
| Electrical performance |  |
| Differential impedance | $100 \pm 10 \Omega$ at $100 \mathrm{ps}(20-80 \%)$ |
| Insertion loss connector | $<1.0 \mathrm{~dB}$ at $0 \div 3 \mathrm{GHz}$ |
| Insertion loss cable | $<5.0 \mathrm{~dB}$ at $0 \div 1 \mathrm{GHz}$ |
| Near-end multi-line crosstalk | $<1.5 \%$ at $50 \mathrm{ps}(20-80 \%)$ |
| Within pair skew | 10 ps per metre |
| Pair-to-pair skew | 50 ps per metre |
| Current rating | 0.5 A per contact |
| Shielding | $>45 \mathrm{~dB}$ at $0 \div 1.2 \mathrm{GHz}$ |
| Mechanical performance |  |
| Durability | 200 mating cycles |
| Mating force | 50 N max |
| Cable strain relief | 50 N min |
| Side load resistance | 75 N min |

Table 5.3: The electrical and mechanical specifications of the FCI cable.

### 5.2.2.3 Clip-board

The Clip-board, designed by the MPI group, shapes the signal and prepares it for the selection logic. The embedded processes involved an amplification ${ }^{11}$, a delay and a clipping stage. In the chosen design architecture, these three stages are laid out in long and low modules (Fig. 5.23(b)), which are vertically plugged and equally spaced in the 9U Clip-board PCB (Fig. 5.23(a)).

In the upper side of the module, the signal is converted from differential to singleended, then it is attenuated with a high bandwidth $(2.4 \mathrm{GHz})$ radio frequency chip, the DAT-31R5-SP+ from Mini Circuits. It offers an attenuation range up to 31.5 dB with a resolution of 0.5 dB step, controlled by a six-bit serial interface. The gain flat-fielding is important to balance any contributions in the final summation and to make easier the conversion from voltage to photoelectrons.
Then, the signal passes a disable switch enclosed in the amplifier, which can be used to black out some channels during tests or calibration runs.

On the Clip-board the different signal arrival times, due to the transition time in PMTs and delays in both long optical fibres and electronic devices, are compensated by adjustable analogue delay lines (Fig. 5.24). This operation is fundamental to allow a perfect pile-up of very narrow signals of a few nanoseconds, getting rid of the uncorrelated spurious NSB events [65].

[^62]

Figure 5.23: On the left, the partially routed Clip-board $P C B$ layout. On the top left side of the image, there are four $F C I$ connectors which receive 32 signals from the receiver boards. On the top centre, there is the communication controller and, a little bit to the right, the power stage. In the centre, the long vertical module arranged to cover the available space and to minimize the traces' skew. On the bottom right, each channel is replicated three times and transmitted to the proper Sum-board. (Courtesy of MPI electronic workshop) On the right, a simple sketch of the Clip-board main functions placed in a single long vertical module. The upper part contains an input differential amplifier, an attenuator and a disable switch. In the centre, there is the analogue delay line, while the end hosts the clipping amplifier. (Courtesy of D. Häfner)

Each prototype delay module is a ladder-unbalanced network composed of a series of 25 variable small $L C$ filters ${ }^{12}$. This design is more efficient, in terms of bandwidth and signal quality, than using a single inductor plus a capacitor. The inductance is fixed, while the capacitance can be changed applying the right voltage to the varactor diodes ${ }^{13}$. This modifies the transmission line impedance, and consequently the signal propagation speed, which is $1 / \sqrt{L C}$. The total delay range spans continuously up to 6 ns (Fig. 5.25), and the acquired precision is correlated to the resolution of the voltage, set to the diodes.
The drawback is the production of small reflections, caused by the impedance mismatch. The termination is inserted at the end of the delay line, but it cannot always match the variable impedance of the network, function of the varactor capacitance. Figure 5.25

[^63]

Figure 5.24: On the top, the circuit of the prototype analogue delay line. On the bottom, the image of the small module. In the final design, this function will be completely integrated in the main vertical module. (Adapted from [65])


Figure 5.25: The analogue signal delayed in a delay line prototype module. The green pulse is measured at the input of the analogue delay line. The blue one is recorded at the line output, imposing the minimum delay. The propagation time is $\sim 5.4 \mathrm{~ns}$. For the red pulse, the maximum delay is uploaded, which is 6 ns after the previous one. (Adapted from [65])
shows an example of undershoot, 7 ns after the peak (blue pulse), whose amplitude is $\sim 40 \mathrm{mV}$, that corresponds to $6 \%$ of the delayed signal. However, the reflection is far from the pulse peak, so it does not affect the Sum-Trigger-II concept. Even the pulse amplitude variation, when the minimum and maximum delays are applied, is limited to less than $3 \%$, so it can be easily corrected during the flat-fielding process.
The comparison of signal specifications, before and after the delay line, is pointed out in table 5.4. When the minimum delay is loaded, the FWHM does not change and the rise time increases a little bit ( 340 ps ). This aspect is worst at the maximum delay. The signal widens by 0.2 ns and its edge is 620 ps slower. A small distortion is present, but it does not drastically affect the signal shape. On the contrary, the resulting pulse is more symmetrical, which could be better in the summation stage.
The average delay line bandwidth is higher than any commercial product on the market that can delay a signal up to 6 ns . To obtain this product, a varactor diode with a very low serial resistance $(0.35 \Omega)$ is chosen: SMV1413 from Skyworks Solutions.
The bandwidth is a function of the transmission line parameters, so it is correlated to the required delay. The frequency response has been measured with a network analyzer (Fig. 5.26). The high cut-off frequency appears around 200 MHz for both curves. This is the worst case, which considers even very low frequency components. Typically, the $P M T$ pulse is very fast and its frequency spectrum stays above $\approx 50 \mathrm{MHz}$. Calculating

| Signal | FWHM <br> $(\mathbf{n s})$ | Rise time <br> $(\mathbf{n s})$ | Amplitude <br> $(\mathbf{m V})$ |
| :--- | :---: | :---: | :---: |
| Input - green curve | 1.66 | 0.82 | 985 |
| Minimum delay - blue curve | 1.63 | 1.16 | 690 |
| Maximum delay - red curve | 1.86 | 1.44 | 675 |

Table 5.4: The summary of the signal timing and amplitude features as a function of the applied delay. The bandwidth is lower for higher delay, smoothing a little bit the signal shape.
the $-3 \mathrm{~dB} \operatorname{limit}^{14}$, starting from this new point, the cut-off enhances to $\approx 240 \mathrm{MHz}$ for the maximum delay and $\approx 270 \mathrm{MHz}$ for the minimum [65].


Figure 5.26: The bandwidth of the analogue delay line. The blue line represents the minimum delay, while the red one the maximum. The high cut-off frequency is indicated by the cross point between the green line and the curves ( $\sim 200 \mathrm{MHz}$ ). Considering that the analogue pulse is made of frequencies above $\approx 50 \mathrm{MHz}$ (yellow zone), the -3 dB green line can be shifted 1 dB down. (From [65])

At the end of the main module, the signal is clipped at a programmable level ${ }^{15}$. This operation is carried out with the current feedback amplifier LMH6553, from National Semiconductor. It is a 900 MHz full differential amplifier with an integrated adjustable output limiting clamp. However, it can even be configured as single-ended input to differential output gain block. The bandwidth has been simulated in this configuration (the same used for the clipping circuit), achieving 635 MHz .
A simple test board has been built to test the clipping circuit (Fig. 5.27). The measurements, obtained with the LLP8 package, have been presented in figure 5.28. The signal quality after the clipping is quite poor, regardless of the input amplitude or the clipping level, but it gets worse for very huge input signals and clipping levels below 500 mV .
The circuit has been simulated to understand if the output deformations are intrinsic to the design or are due to some problems related to the $P C B$. In figure 5.29, the results are presented. The differential pulses are measured at the output pins of the LMH6553 amplifier. For clarity, the negative signal is artificially inverted.

[^64]

Figure 5.27: The clipping circuit under test, based on the amplifier LMH6553. (Courtesy of D. Häfner)


Figure 5.28: On the top, the positive and negative outputs of the clipping circuit at different levels. On the bottom, the same measurement, but changing the input amplitude with a fixed clamp voltage of 100 mV . (Courtesy of MPI electronic workshop)

The signal's quality is very much better than that shown in figure 5.28. There is a small overshoot and an undershoot, respectively on the positive and negative pulse edges, of the order of $\sim 4 \%$. This effect appears only for clamp levels higher than 300 mV , so it should not affect the sum stage, because this is more or less the voltage that corresponded to $\sim 6 \div 7$ phe in the prototype Sum-Trigger. The positive and the negative pulses are very similar, but displayed a constant relative offset of $\sim 20 \mathrm{mV}$. This is also not a problem, because an eventual $D C$ component is completely eliminated by the following bypass capacitors.
In contrast to the signal integrity, the clipping function shows a couple of defects. The working clamp level is not equal to the set voltage. For low clipping voltages, the offset


Figure 5.29: Left: the simulation of the differential output (blue \& red pulses) clipping circuit at different clamp levels and an input of 1 V (green). Right: the same simulation with a fixed clamp at 100 mV and different input amplitudes. The input signal, which matches the PMT pulse, is described by this function: $f(t)=\sum_{i=1}^{5} a_{i} e^{-\frac{\left(t-b_{i}\right)^{2}}{2 c_{i}^{2}}}$, where $a_{i}, b_{i}$ and $c_{i}$ are constants. (C F. Dazzi \& G. Galeazzi)
error can reach even $50 \%$ (e.g. clipping set at 100 mV and clipping measured $=150 \mathrm{mV}$ ). This offset is not constant, but it is a function of the input signal amplitude and the clipping level, namely it gets worse with huge pulses and low clamps. It seems that the discrepancy becomes more noticeable as the differences between the clamp voltage and the input signal amplitude increase. Only for ratios below 2.5 , it is negligible. Considering a clipping level of 6 phe, the offset is problematic for very high energetic events, containing more than 15 phe per pixel. This changes a little bit the trigger efficiency in the very high energy domain, which is not essential. Nevertheless, a slightly higher clipping level could allow a higher afterpulse accidental rate. This must be evaluated in the future on-site measurements.
The simulation demonstrates the suitability of the circuit design. The low signal integrity of the prototype clipping board is likely due to the $P C B$ layout. The signals in figure 5.28 seem to be affected by reflections and oscillations, typical of high frequency amplifiers.

Finally, the signals are repeated three times and transmitted to the Sum-backplane, using a differential amplifier $A D A 4927-2$ from Analog Devices.
The performance of the drivers is obtained with a dedicated test board, dubbed CTBFCI (Fig. 5.30), and designed by the Padova/Udine group. It groups eight equal blocks, each one formed by an input $S M A$ connector, a differential transmitter $A D A 4927^{16}$, a channel pair in a $F C I$ cable ${ }^{17}$, a differential receiver equal to the original one mounted in the Sum-board and an output SMA connector for the connection to the oscilloscope (schematics in appendix B). The CTB-FCI test board allows to test, at the same time, the Clip-board transmitter stage, the FCI cable and the Sum-board receiving stage. The measured bandwidth of the transmitter stage is around 1.3 GHz (Fig. 5.31(a)), although the $P C B$ presents a grounding problem and the contact point of the network analyzer's probe is not perfect. The thermal pads are not connected in the internal ground planes, which result in a floating voltage. Some blind holes have been made up to the copper surface of each internal ground plane. Then, the planes are shortcircuited to the ground line. This prevents a complete impedance mismatching of the

[^65]Figure 5.30: Picture of the $C T B-F C I$ board, designed to verify the performance of the transmitter stage of the Clip-board, the receiver stage of
 the Sum-board and the FCI cable. On the top, there are 8 single-ended inputs and just below the dual transmitters $A D A 4927-2$. On the right, the output and the return of the $F C I$ cable, while on the bottom the 8 current-feedback amplifiers OPA695 with the corresponding SMA output connectors.
internal traces and assures the ground shielding. However, it is mechanically impossible to drill a blind via every time there is a trace's passage between distinct layers, which can force the current return to be very close to the signal. For the same reason, the probe's terminals are a little bit spaced out.
The same measurement has been repeated, but adding a $F C I$ cable of 5 m . The band-


Figure 5.31: Left: The bandwidth of the transmitter output stage of the Clip-board. Right: The bandwidth adding the capacitive load due to the $5 \mathrm{~m} F C I$ cable.
width obtained is around 820 MHz (Fig. 5.31 (b)). In first approximation, the cable upper frequency cut-off can be extrapolated by the following formula:

$$
\begin{equation*}
\frac{1}{f_{\text {out }}}=\sqrt{\frac{1}{f_{\text {trans. }}^{2}}+\frac{1}{f_{\text {cable }}^{2}}} \tag{5.3}
\end{equation*}
$$

where $f_{\text {trans. }}$ and $f_{\text {cable }}$ are respectively the transmitter and the cable frequency cut-off. Substituting the previous bandwidth values, we obtain:

$$
\begin{align*}
f_{\text {cable }} & =\left(\sqrt{\frac{1}{f_{\text {out }}^{2}}-\frac{1}{f_{\text {trans. }}^{2}}}\right)^{-1}  \tag{5.4}\\
& =\left(\sqrt{\frac{1}{\left(0.82 \cdot 10^{9}\right)^{2}}-\frac{1}{\left(1.3 \cdot 10^{9}\right)^{2}}}\right)^{-1} \\
& =1.06 G H z
\end{align*}
$$

indicating a cable bandwidth of about 1 GHz .

Finally, even the receiving stage has been considered. Unfortunately, the bandwidth drops down drastically, dominated by the limited bandwidth ( $\sim 450 \mathrm{MHz}$ ) of this last stage. In subsection 5.2.2.5, this portion of the circuit has been thoroughly analysed and improved, resulting in a higher bandwidth of around 800 MHz .

### 5.2.2.4 Sum-backplane

The Sum-backplane is a passive 10U printed circuit motherboard (Fig. 5.32(a)), which connects the Clip-boards to the Sum-boards, following the mapping Sum_mapping_V4. To make future maintenance easier, the 19 bottom slots have a hardware coding, so the Sum-board address is bound by the board position in the crate and it is not necessary to change it every time. It makes the system swappable and board position independent.


Figure 5.32: On the left photo, the Sum-backplane 10 U motherboard. On the right, the board's dimensions. They are quite considerable, around $43 \times 44 \mathrm{~cm}$.

For the electronic point of view, this is the most critical part of Sum-Trigger-II. The $P C B$ layout has been projected considering that 997 fast differential analogue signals have to be routed to 55 macrocells, preserving the isochronism inside 50 ps , a bandwidth higher than 1 GHz and a low cross-talk $(<1 \%)$. These constraints demanded to an accurate design strategy, where the macrocell numbering, the $P C B$ stack-up, the trace impedance and the components' placement and routing have been studied and optimized in a very huge board (Fig. 5.32(b)).
All the traces must be adjusted to the longest one, applying meandering ${ }^{18}$ routing. It is fundamental to keep the maximum length difference as short as possible, to avoid extended and space-consuming paths, which affect the signal quality and make impossible the complete routing.
Considering the board's dimensions and the relative position of all connectors, different arrangements have been simulated to find the solution, which minimizes the length adjustment. The calculated skew, after the routing phase, is shown in figure 5.33. It is clear that the requirements are theoretically fulfilled, even if the average wire length

[^66]has been increased to 68.5 cm by some routing limits, far from the simulated value obtained in the place and route phase $(30 \mathrm{~cm})$.


Figure 5.33: The propagation time of the 997 traces routed in the Sum-backplane, calculated by the $C A D$ software. The trace's length and the line impedance are considered in the simulation. The propagation time is $\sim 4.5 \mathrm{~ns}$, the maximum skew between channels is 33 ps and the maximum skew inside a differential net is 26 ps .

Other parameters, such as for instance the trace's width, the differential line separation and the dielectric constant are mapping-independent, but they are relevant for the signal properties. The $P C B$ stack-up counts twenty layers, nine of which are reserved for signal routing. This is the cheapest layout that allows an efficient escape


Figure 5.34: This is the Sum-backplane stack-up. It is composed of twenty copper layers, nine dedicated to the signals routing. This means that the board thickness will be out of standard ( $\sim 2.8 \mathrm{~mm}$ ), even if the chosen support (Nelco N4000-13) has a low dielectric constant of 3.4. This material is an enhanced epoxy resin system engineered to provide both outstanding thermal and low signal loss properties for high-speed applications. For the purposes of the Sumbackplane, it is perfect, because it assures an optimum signal integrity and a precise impedance control.
routing from the backplane connectors. These pressfit connectors (ERmet ZD 223396) are provided by the ERNI company and are designed for high-speed and low-voltage differential transmissions, up to $10 \mathrm{~Gb} / \mathrm{s}$. They provide 30 contact pairs ${ }^{19}$, each one

[^67]with a differential impedance of $100 \Omega$ and a ground shielding.
The trace characteristics are summarized in table 5.5 and the features of the meandering delay lines have been selected to have, at the same time, a precise skew control and a low signal deterioration. The ratio between the meander height, typically around 2 mm , and its width is never more than 2.5. Up to 200 meandering curves are sometimes applied to match the required delay adjustments.

## TRACE SPECIFICATIONS

| Trace type | Min. width <br> (um) | Typ width <br> (um) | Max. width <br> (um) | Diff. pair <br> spacing (um) |
| :--- | :---: | :---: | :---: | :---: |
| Analogue pairs | 90 | 100 | 100 | 100 |
| Digital pairs | 90 | 100 | 100 | 100 |
| Others | 200 | 200 | 200 | 200 |

Table 5.5: The main properties of the Sum-backplane traces. For the analogue and digital pairs, they are calculated to obtain a differential impedance close to $100 \Omega$.

Another crucial point is the evaluation of the cross-talk, which could increase the signals' amplitude during the sum stage, resulting in fake triggers. The minimal trace separation, from edge to edge, is fixed to three times the line width to keep negligible the mutual electromagnetic interaction.
The cross-talk has been simulated with the Hyperlinx software. A step function with a rise time of $\sim 750 \mathrm{ps}$ and a voltage drop of $\sim 1200 \mathrm{mV}$ is injected in an aggressor line, while the output is calculated at the end of a victim adjacent wire ${ }^{20}$ (Fig. 5.35). The choice of a step function is determined by the desire to be very conservative in the estimation of the cross-talk. Its frequency components are extremely high, more than the $P M T$ analogue response, and the amplitude is fixed to four times the amplitude of a clipped signal ( $\approx 350 \mathrm{mV}$ ).
As displayed in figure 5.35, the cross-talk seems to have an inductive nature, because


Figure 5.35: The simulation of the Sum-backplane cross-talk between two close lines. A huge step function (orange curve) is injected in one line, while the amplitude in an adjacent one is calculated (blue curve). This could be considered the worst case, taking into account the characteristics of the aggressor signal. The maximum cross-talk is around $0.75 \%$. (Courtesy of INFN-Padova electronic workshop)
it appears in the correspondence of the signal edge and it is negative. The maximum

[^68]value is $\sim 9 \mathrm{mV}$, namely $0.75 \%$ of the aggressor amplitude. It should be underlined that the differential signalling offers superior immunity to common mode noise such as crosstalk and simultaneous switching noise.
Cross-talk coupled to a victim differential pair comes only from the differential component of the generated electromagnetic field, because the common mode is cancelled at the receiver. This contribution only exists because the distance between the aggressor and the victim slightly changes, when the inside or the outside trace is taken into account.
In figure 5.36 the real case of the Sum-backplane is illustrated. The aggressor is the


Figure 5.36: A sketch in scale that represents two close differential lines in the Sum-backplane. The green arrows show the dimensions and the violet ones the single contributions to the differential cross-talk. (©) F. Dazzi)
pair composed of the wire A and B, whereas the victim is the pair C and D. The signal is injected at the input of the aggressor line and the far cross-talk is registered at the output of the victim. Both lines are correctly terminated to prevent wrong estimations due to reflections. Then, the differential cross-talk component has been calculated superimposing the four contributions, marked with the violet arrows, between the two differential lines. The differential cross-talk can be expressed by the following equation:

$$
\begin{equation*}
X T_{d i f f}=X T_{C}-X T_{D} \tag{5.5}
\end{equation*}
$$

where $\mathrm{XT}_{C}$ and $\mathrm{XT}_{D}$ are the induced voltage fractions measured respectively at the line C and D. In first approximation they can be obtained from relations 5.6 and 5.7.

$$
\begin{align*}
& X T_{C}=X T_{A C}-X T_{B C}  \tag{5.6}\\
& X T_{D}=X T_{A D}-X T_{B D} \tag{5.7}
\end{align*}
$$

It must be underlined that the sources $A$ and $B$ have equal and opposite signals, so the same property is transferred in the generated electromagnetic field. This explains the negative sign before $\mathrm{XT}_{B C}$ and $\mathrm{XT}_{B D}$. Substituting the variables in equation 5.5, we get the final formula 5.8.

$$
\begin{align*}
X T_{\text {diff }} & =\left(X T_{A C}-X T_{B C}\right)-\left(X T_{A D}-X T_{B D}\right)  \tag{5.8}\\
& =X T_{A C}-X T_{B C}-X T_{A D}+X T_{B D}
\end{align*}
$$

Every single contribution has been quantified in the whole spectrum from 1 MHz to 1 GHz with a sinusoidal signal of 0 dBm (Fig. 5.37). The curves trends do not follow the same profile, so it is not trivial to combine them. A quantitative analysis tells us that one of the worst cases occurs, for instance, at $\sim 600 \mathrm{MHz}$. In table 5.6 the results


Figure 5.37: The far end cross-talk of a single differential line coupling to another differential line in the spectrum from 1 MHz to 1 GHz . The four contributions between traces are measured independently. Top left: the cross-talk spectrum in trace C , when A is the aggressor. Top right: the cross-talk spectrum in trace C, when B is the aggressor. Bottom left: the cross-talk spectrum in trace D , when A is the aggressor. Bottom right: the cross-talk spectrum in trace $D$, when $B$ is the aggressor.
extrapolated at different frequencies, including 600 MHz , are reported. It is evident that the cross-talk is dominated by the component $\mathrm{XT}_{B C}(0.6 \%)$, namely between only the closest traces. The rest is a factor ten lower, so practically negligible. In fact, increasing the separation between traces, their coupling is reduced following a power law. Moreover, in differential stripline there is an inherent shielding. The inside trace of the pair partially shields the coupling to the outside trace.

| DIFFERENTIAL CROSS-TALK |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| BW | $\mathbf{X T}_{A C}$ | $\mathbf{X T}_{B C}$ | $\mathbf{X T}_{A D}$ | $\mathbf{X T}_{B D}$ | $\mathbf{X T}_{\text {diff }}$ | $\mathbf{X T}_{\text {diff }}$ |
| $(\mathbf{u m})$ | $(\mathrm{dB})$ | $(\mathrm{dB})$ | $(\mathrm{dB})$ | $(\mathrm{dB})$ | $(\mathrm{dB})$ | $(\%)$ |
| $\mathbf{3 0 0}$ | -68 | -44 | -78 | -70 | -44.9 | 0.57 |
| $\mathbf{6 0 0}$ | -62 | -44 | -63 | -70 | -44.6 | 0.59 |
| $\mathbf{9 0 0}$ | -65 | -57 | -60 | -62 | -60 | 0.10 |

Table 5.6: The differential far end cross-talk fraction measured at different frequencies.

At this point, it is important to estimate the effect of the multi cross-talk. The
worst case comes when the victim is surrounded by two aggressors, assuming that the others, not adjacent to the victim, have no influence. Therefore, the maximum multi cross-talk is around $1.2 \%$.
These measurements only ensue from the $P C B$, because the contribution from the connectors ${ }^{21}$ is not considered. However, only rarely there are traces that travel in parallel inside the $P C B$ and end up on neighbouring pins of the same connector.

The bandwidth, measured with a network analyzer $H P$ model $H P 4396 A$, is around 600 MHz (Fig. $5.38(\mathrm{a})$ ). This value is not perfectly in agreement with the simulation that returns $\sim 700 \mathrm{MHz}$. A weak point is the two hand-made connectors, necessary to match the network analyzer I/O format with the Sum-backplane ERNI contacts. Even part of the oscillations in the bandwidth curve can be pinpointed to these adapters. In fact, simply by improving the shielding in the conjunction point, the oscillations have been reduced by $\sim 50 \%$, recovering 2 dB . Another contribution to the mismatch can come from the huge tolerance $(15 \div 20 \%$ ) in the dielectric thickness, resulting in the $P C B$ build-up process.
An additional simulation, cutting into halves the trace length $(30 \mathrm{~cm}$ as foreseen in


Figure 5.38: Left: the Sum-backplane bandwidth measured with a network analyzer. Right: the differential signal at the input of the Sum-backplane (white line) and at the output (orange line).
the design phases), was carried out to check the bandwidth cut-off. The result was at the same time clashing and interesting: 2.7 GHz , indicating that the GHz domain is possible with the appropriate length. The next step will be to examine the feasibility to increase the number of layers, hence the routing space, while reducing the trace dimensions as much as possible. Obviously, this will considerably affect the $P C B$ cost, which does not increase linearly with the number of layers. For instance, the price for 28 layers is double that of twenty.
A very fast pulse generator has been used to test the signal integrity. In figure 5.38(b) the differential signals before and after the Sum-backplane are shown. The signal is quite good, and either reflections or ground bounce are visible. The limitation is again the bandwidth. The behaviour is typical of an RC low-pass filter, which modifies the input signal rise time ( $<200 \mathrm{ps}$ ) to around 1 ns . In fact, the Hyperlinx simulation of the produced $P C B$ estimates a capacitive load of 75 pF .

[^69]
### 5.2.2.5 Sum-board

The Sum-board is the main board for the final event selection (Fig. 5.39). It can handle up to three macrocells covering the whole mapping with only 19 units, still keeping the compactness of a small 3 U card. It is a high-speed mixed analogue and digital system, which can be controlled either automatically by the Astro-board and the software or manually providing the commands directly to the front panel input connectors.
The function diagram is shown in figure 5.40. The differential analogue signals are


Figure 5.39: A photo of the Sum-board. In the upper area there is the analogue electronics, while below the pale-green horizontal line (ground separation) there is the digital one. $D A C$ is the device between the two areas.
converted to single-ended format in preparation for the sum stage. The summation is executed in two successive steps to avoid the amplifier's saturation ( 4.2 V ), in case 19 signals clipped at $300 \div 400 \mathrm{mV}$ are piled up. In the first block, four groups of five ${ }^{22}$ channels are added up, attenuated and only in a second amplifier the four outputs are added. The consequent signal is compared with a programmable threshold and a trigger is generated when it is exceeded. The electrical schematics are given in appendix C.
The rest of the electronics is used for the threshold control, data transmission and monitoring. The main three devices are a single package multi- $D A C$, a voltage reference and a magnitude comparator for the board address verification. The $D A C$ ( $A D 5582$ ) is a 12-bit quad voltage output digital-to-analogue converter. A doubled-buffered parallel interface offers a fast settling time and a read-back mode of the internal input registers. Assuming that the electronic chain amplification returns $\sim 50 \mathrm{mV}$ every photoelectron, as in the prototype Sum-Trigger, and the Sum-board gain is fixed around 0.25 , the pulse will be $\sim 12.5 \mathrm{mV} /$ phe at the comparator level. The working voltage of $D A C$ is enabled between $0 \div 2 \mathrm{~V}$, so that the resolution obtained is 0.5 mV . This corresponds to 0.04 phe, well below the electronic noise level.

Standard signal integrity techniques have been used in the Sum-board, too. The stack-up counts 14 layers, divided into six for signals and eight for the ground and the power voltages. The $P C B$ structure has been plotted to get a differential pair impedance of $100 \Omega$ and the single-ended of $50 \Omega$. All of them are striplines ${ }^{23}$ disposed among ground layers, while the $\pm 5 \mathrm{~V}$ are isolated at the centre of the board.
The traces' length has been carefully calculated during the design phase. The channels' skew in the portion from the input connector and to the first sum stage is less than 11 ps (Fig. $5.42(\mathrm{a})$ ), while between the two sum amplifiers is null. The total propagation time up to the trigger output is 3.4 ns , always with the same extremely low skew (Fig. 5.42(b)). Even comparing channels belonging to different macrocells, the timing

[^70]

Figure 5.40: At the beginning, the differential analogue signals are converted in singleended (blue rectangle) lines, then they are added in two steps (violet triangles). At the end, the output is compared with a programmable threshold (red rectangle). On the bottom side, there are the digital commands for the threshold control and the data transmission. (C) F. Dazzi)


Figure 5.41: This is the Sum-board stack-up. It is composed of fourteen copper layers, six dedicated to the signals' routing. The support material is the standard $F R_{4}$ with a dielectric constant around 4.2. The high-speed signals travel only in striplines enclosed between two ground planes to avoid electromagnetic noise.
precision is not affected ( $<13 \mathrm{ps}$ ).
Another important topic is the bandwidth and the preservation of the signal properties. In fact, a long study has been carried out, and is still in progress, to find the best configurations for the receiving and the summing stages. As in the prototype SumTrigger, the current-feedback amplifier OPA695, from Analog Devices has been the initially preferred device. It is a wideband chip that combines exceptional $4300 \mathrm{~V} / \mu \mathrm{s}$ slew rate and low input voltage noise.
The receiving stage is a difference amplifier with some passive components to match the characteristic transmission line impedance (schematics sheet nr. 4 in appendix C). Preliminary tests demonstrate that this circuit introduces some asymmetries, slightly


Figure 5.42: On the top, the estimated propagation time up to the sum stage input for each channel. Channels in different macrocells are coloured differently. The maximum skew is less than 11 ps . On the bottom, the same evaluation, but considering the overall board. As before, the skew continues to be negligible, less than 13 ps .
deforming the signal shape. The positive and negative input bandwidths have been measured separately with a network analyzer (Fig. 5.43). The result reveals two dissimilar


Figure 5.43: Left: the positive input bandwidth of the difference amplifier. The cut-off point is above 1.1 GHz . Right: the same bandwidth of the negative input. Here, the -3 dB limit occurs around 845 MHz .
curves with distinct cut-off ${ }^{24}$. An additional test, duplicating the pulse generator signal with a power splitter (Microlab/FXR DA-3FN) and stimulating simultaneously both inputs with the same positive pulse, confirms the asymmetric behaviour (Fig. 5.44(a)). The output voltage should be constantly zero, but two bumps, corresponding to the signal edges, are visible. Probably the rise time of the inputs are differently affected by the two bandwidths, therefore the voltages do not increase with the same speed, resulting in a no zero function. In fact, the positive path returns a steeper edge ( $\mathrm{t}_{\text {rise }}$ (positive) $\mathrm{t}_{\text {rise }}($ negative $) \approx-200 \mathrm{ps}$ ) compared to the negative.
This effect seems to be irrelevant, when only one signal is injected and the receiving stage is observed (Fig. 5.45). However, we have to remember that the system can pile up to 19 pulses, involving other two amplifiers in series. An asymmetric shape is not

[^71]

Figure 5.44: Left: the difference amplifier output (curve 1), when stimulated with the same signal ( $\mathrm{A}=360 \mathrm{mV} ; F W H M=2.6 \mathrm{~ns} ; \mathrm{t}_{\text {rise }}=1.16 \mathrm{~ns}$ ) in both inputs (curve R1). The peak-to-peak output amplitude returns 35 mV ( $9.7 \%$ input amplitude). Right: the same verification, but introducing a low-pass filter before the positive input in order to equalize the bandwidth responses. There is an improvement, but it is not sufficient ( 16 mV , namely $4.4 \%$ ).
democratic in the summation phase, because its contribution depends on which signal portion is overlapped with the others.
Further studies have been elaborated to reduce this discrepancy. A low-pass filter ${ }^{25}$


Figure 5.45: Left: the pulse at the input of the difference amplifier. Right: the same pulse at the output level. The asymmetry is visible mainly on the peak. There is a bump corresponding to the positive edge end, which increases the amplitude of 30 mV with respect to the original pulse.
has been introduced just before the positive input in order to approach the negative input bandwidth. As shown in figure $5.44(\mathrm{~b})$, an improvement is achieved, but it does not completely solve the problem, suggesting that either there are some contributions of the second order that are not well understood or the filter adds new undesired complications.
The input impedance behaviour has been simulated in both amplifiers' inputs. The circuit has been designed to obtain a differential input impedance of $100 \Omega$, equally divided between the positive and the negative branch. Figure 5.46 (a) proves the accuracy up to 2 GHz . Introducing the filter, both impedances are stable around $50 \Omega$ up to

[^72]300 MHz , but the one that refers to the positive input starts to drop down (Fig. 5.46(b)). Around 800 MHz , the original value is lowered by $20 \%$, dominated by the impedance of the low-filter capacitor, as expected. The component of the positive pulse that enters in the amplifier is lowered in consequence, unbalancing yet again the response. On the one hand, the bandwidth has been equalized, on the other hand part of the positive signal is lost.


Figure 5.46: Left: the input impedance of the receiving stage calculated from both inputs of the difference amplifier without the low-pass filter. Right: the same simulation with the filter inserted. (C) F. Dazzi \& G. Galeazzi)

Finally, the different propagation time of both positive and negative components that compose the differential signal are simulated with the filter (Fig. 5.47(a)) and without (Fig. 5.47 (b)). The original skew is $\sim 40 \mathrm{ps}$ (positive output - negative output), which increases to around -100 ps . This delay, due to the low-pass filter, is another contribution that affects the output signal symmetry. In fact, inside the amplifier, the subtraction is performed by slightly shifted pulses. The earlier pulse dominates on the output rising edge, while the later one on the falling edge.
According to the results of the previous analysis, some modifications have been made


Figure 5.47: Left: the simulated propagation time of both branches (positive \& negative) of the same circuit without the low-pass filter. Right: the same simulation with the filter inserted. (C) F. Dazzi \& G. Galeazzi)
to the circuit. The capacitance of the low-pass filter has been lowered to 7.5 pF to reduce both the delay with respect to the negative input and the impedance drop at high frequencies. The resistive divider at the positive input has been changed to increase a
little bit the amplitude of the positive signal. The new resistance values are respectively $22 \Omega$ and $27 \Omega$. The bandwidth has been further enhanced, bringing down the feedback resistance to $301 \Omega$. Even the corresponding resistance at the negative input has been modified to $301 \Omega$ to match the expected gain. The resultant performance is quite good and the causes of the original problems seem to be well understood. Currently the bandwidths have been perfectly equalized at the frequency around 950 MHz (Fig. 5.48). To


Figure 5.48: Left: the positive input bandwidth of the difference amplifier at the receiving stage of the Sum-board. The cut-off point is around 970 MHz . Right: the same bandwidth $(950 \mathrm{MHz})$ of the negative input.
test the circuit behaviour in the whole bandwidth range, a Digital Signal Generator Tektronix DTG 5274 coupled with one differential output module DTGM30 has been borrowed from experimental nuclear physics group. Thanks to the internal clock of 2.7 GHz , it can generate very fast and symmetric pulses with a rise time of $\sim 200 \mathrm{ps}$ (Fig. 5.49(a)). Repeating the output signal measurement by injecting the same pulse into both inputs shows that even this problem has been shrunk to well under 10 mV (Fig. 5.49(b)).
Using the same equipment, even the two sum stages have been examined showing the


Figure 5.49: Left: the pulse generated by the high-speed Digital Signal Generator Tektronix DTG 5274. Right: the voltage output asymmetry injecting the same pulse in both inputs. The yellow signal is the amplifier output, while the red one is the math function subtracting the contribution from the pulse generator (white signal).
analogue signal evolution from the board input (Fig. 5.50(a)) to just before the digitalization (Fig. 5.50(b)). The signal becomes little by little smaller, because the entire
board's gain (x 0.25 ) has been fixed to reach the voltage limit of around 2 V , when all the 19 channels inside the same macrocell are firing. Considering that the pulses will be clipped at around $300 \div 400 \mathrm{mV}$, the output would exceed 6.5 V , without the gain normalization.
Further tests are foreseen in the immediate future in order to evaluate the behaviour


Figure 5.50: Left: the differential pulse from the generator (yellow \& blue) and the output of the receiver stage (violet). Right: the output of the first (blue) and the second (violet) sum stage.
of the board with several injected pulses, randomly delayed.
The bandwidth of the whole board, including the receiver, the first sum and the second sum stage, is shown in figure $5.51(\mathrm{a})$. The frequency spectrum is extremely flat up to 300 MHz , and the bump underlined in the receiver stage has been removed. The -3 dB limit is measured at $\sim 650 \mathrm{MHz}$.
The cross-talk has been measured in the long $(11 \div 12 \mathrm{~cm})$ stretch of trace between


Figure 5.51: Left: the bandwidth of the whole Sum-board. Right: The frequency spectrum from 1 MHz to 1.8 GHz of the single far-end cross-talk.
the receiver and the first sum stage. The peak, limited at a very small band around $\sim 900 \mathrm{MHz}$, returns $-47 \mathrm{~dB}(0.44 \%)$. The cross-talk curve decreases drastically at different frequencies. At 200 MHz , it is around $-60 \mathrm{~dB}(0.1 \%)$ and, at $100 \mathrm{MHz},-70 \mathrm{~dB}$. The contribution in the short differential lines at the receiver input, as well as in the spaced traces after the first sum stage, is negligible.

Currently, another amplifier fully compatible with the previous one, LMH6702 from

National Semiconductor, is under test. This is a wideband operational amplifier designed specifically for systems requiring exceptional signal fidelity. Benefiting from the current-feedback architecture, it offers a good stability at high frequencies. The signal shape with this new amplifier has been simulated with the complete circuit. The result is presented in figure 5.52. The receiving stage of the circuit shown in figure 5.52 has


Figure 5.52: On the top, the circuit used for the simulation. The summing stages are simplified with only one input. On the bottom, the performance of the circuit. Shown are the input pulse (black curve), the differential stage output (pink curve), the first sum output (green curve) and the second sum output (blue curve).
been mounted on the Sum-board and tested. This is the configuration suggested in the chip data sheet to obtain the best performance. Actually, the signal integrity is really impressive, but the bandwidth is limited at $\sim 500 \mathrm{MHz}$, which is too low for our purpose. As for the OPA695, the bandwidth response increases, lowering the resistor in the feedback. Finally, an acceptable bandwidth is obtained with a $100 \Omega$ resistor in feedback, another equal to the negative input and a small capacitive filter before the positive input to match the different behaviour of the inputs ( 3.3 pF ). The effect is completely analogous to the one discovered, testing the OPA695 amplifier (Fig. 5.53(a)). The comparison with the OPA695 amplifier reveals that the new chip behaves similarly, but with some limitations (Fig. 5.53(b)).
The bandwidth is lower than before, because the rise time of the chip passes from $\sim 307 \mathrm{ps}$ to $\sim 388 \mathrm{ps}$, injecting a very steep signal from the generator ( $\sim 200 \mathrm{ps}$ ). Nevertheless, the oscillations are more evident and the asymmetry is stronger. For these reasons, the OPA695 is preferred.

The last point deals with the quality control of the digital functions of the board. A


Figure 5.53: Left: the output signal of the final receiving stage, using the current-feedback amplifier OPA695. Right: the output signal of the receiving stage, this time with the voltage amplifier LMH6702.
specific board has been designed (schematics in appendix D) to plug a single Sum-board and connect it to the logic analyzer (Fig. 5.54(a)). We have used the logic analyzer Hewlett Packard $16500 B$, which can generate very fast and low differential signals that can be quite similar to the $P M T$ pulse. The set-up is shown in figure 5.54(b).


Figure 5.54: On the left, the Sum-test-board designed to perform a quality control of all the functionalities of the Sum-board. On the right, a photo taken during a test.

### 5.2.2.6 Astro-board and software interface

The Astro-board ${ }^{26}$ is the final stage of the Sum-Trigger-II electronic chain. It interfaces with the control software, processes the macrocell trigger rates and manages the trans-

[^73]mission of the parameters for the automatic adjustment of both the signal amplitude and delay.

Each macrocell can generate its own local trigger, so the Astro-board may potentially receive up to 55 triggers at the same time. It merges these local triggers through a global $\mathrm{OR}^{27}$, sending a single command to the prescaler, which activates the $D A Q$ for the recording phase.
The local information is also helpful to avoid high trigger rate alterations due to bright stars in the FoV, artificial light sources, moonlight or variation of the weather conditions. The Astro-board reads the trigger frequency of each macrocell, compares it with a predefined allowed range and automatically adjusts the discriminator thresholds of that Sum-board, until the rate does not stabilize inside the limits. The feedback approach makes the system very stable.

During the amplitude equalization, the Astro-board plays the role of an interface between the Sum-board and the Clip-board. The desired threshold is loaded to the Sum-board fast comparator, the channel under test is enabled (the rest, in the same macrocell, is disabled) and the first attenuation value is set in the Clip-board. The trigger rate is recorded and saved via software control. Then, the Astro-board changes the attenuation value and registers another rate. The process continues until there are enough points that well fit a cumulative function and the transition region from $100 \%$ to $0 \%$ of trigger counts is well covered. Finally, the software calculates the optimal value, which is at a count rate of $50 \%$, and orders the Astro-board to set the channel at this precise amplitude (Fig. 5.55(a)).


Figure 5.55: Left: the cumulative distribution function. Since the count rate distribution is Gaussian, the cumulative function can be described with an error function $\left(f(t)=\frac{2}{\sqrt{\pi}} \int_{0}^{t} e^{-x^{2}} d x\right)$. The $50 \%$ value coincides with the point where the second derivative is nullified, namely it is the peak of the Gaussian distribution. Right: the utilization of a fast flip-flop to synchronize a signal with the reference one. When the edge of the reference signal activates the clock, the input state is loaded in the output pin. Delaying the pulse, it is possible to assess the relative timing difference.

A very similar procedure is adopted for the delay synchronization, but it uses different devices of the Astro-board. The signal timing is determined counting the output rate either of an FPGA input register or of a fast flip-flop NB7V52M ${ }^{28}$, when the ref-

[^74]erence pulse ${ }^{29}$ is connected to the clock port (Fig. 5.55(b)). Then the signal is delayed relatively to the reference one, changing the bias voltage of the corresponding delay line in the Clip-board. Even in this case, the optimal point is selected as $50 \%$ of the cumulative distribution function.
The ON Semiconductor flip-flop offers an exceptional short set-up time (typically 15 ps ) and a maximum random jitter of $0.8 \mathrm{ps} R M S$. These features eliminate the possibility of having the flip-flop in a metastable state.

Both previous procedures will not be enabled for a pixel one step at a time, but the calibration is performed in parallel, activating many channels in distinct macrocells. In this way, the whole trigger area can be covered in 27 rate scans. The time required by a single run is tied to the required resolution, but in the worst case two minutes should be sufficient. In less than one hour, the complete equalization should be done.

The board, which is under the responsibility of the MPI team, is still in the design phase and there are no prototype PCBs to test. It will be a full digital 9 U board, located in the last position of the upper crate row. The core will be an FPGA Altera Cyclone IV, which will manage the 55 blocks for the amplitude and delay adjustment. The global OR trigger will be generated either in a dedicated $P L D$ or in a wired OR in order to increase the timing precision. The board will be equipped with many transceivers for the data transmission between the Sum-boards and the Clip-boards, by means of the Sum-backplane and the SPI-backplane respectively. The general block diagram is described in figure 5.56.


Figure 5.56: The main block diagram of the Astro-board. (Courtesy of D. Häfner)

### 5.2.2.7 SPI-backplane

The SPI-backplane is a 3U passive board with 18 DIN41612 96 contact connectors for the connection of the Clip-boards and another one for the Astro-board. The main functions are the power distribution and the availability of a serial bus for the data transmission to the Clip-boards (Fig. 5.57).

[^75]

Figure 5.57: The 3U SPI-backplane with 19 connectors.

The SPI serial bus is based on the master/slave mode, where the master device provides the clock and starts the data communication. This bus works with a single master and with one or more slave devices. In the Sum-Trigger-II case, the master is placed in the Astro-board, while each slave, the Clip-board, is not connected by a daisy chain ${ }^{30}$ configuration. From each slave, an independent bus is routed to the master, in order to minimize the jitter even in the data transmission.
This serial protocol consists of 4 lines:
SCLK: serial clock from the master. This is a control line.

MOSI - SIMO: master output and slave input. This is a data line (Tx).
MISO - SOMI: master input and slave output. This is a data line (Rx).
SS: slave select (active low). This is a control line, one for each slave.
They are administered by the central FPGA of the Astro-board and dedicated PLDs installed in each slave.
The transmission is activated when the $S S$ is "LOW". One bit per clock cycle is sent from MOSI to SIMO and from SOMI to MISO, and it is recorded in a shift register. To stop the communication, the $S S$ bit is set to "HIGH" again.

### 5.2.3 Prototype boards test

A small prototype of the new Sum-Trigger-II system, able to manage eight channels, has been designed and tested at the MAGIC site by the MPI team. The aim was to demonstrate the functionality and the reliability of the new design, especially the signal adjustment procedure.
This prototype was composed of four small boards (Fig. 5.58):
Clipping board prototype: It is a simplified version of the Clip-board. The input signals are amplified in two steps by a factor of 20 . Then, they are equalized in amplitude and time using a 12-bit resolution serial $D A C^{31}$. Finally, the clipping is applied with the amplifier LMH6553.

Old summing board: This is the Sum-board of the old system. Here, only the summation stage is performed.

[^76]Discriminator board prototype: This board provides the discrimination stage and the counting rate electronics, currently included respectively in the Sum-board and in the Astro-board. Very fast ECL comparators (MAX9600) are followed by one-shot chips to stretch the signals for the signal processing.

Computer control board: It manages all the functions for the data transmission control and the software interface. It houses an $U S B$ interface module (IOWarrior $56^{32}$ from Code Mercenaries), the SPI master CPLD and the $R S-485$ transceivers. A basic $C$ software, with the IO-Warrior 56 dynamic library installed, communicates to the computer control board.


Figure 5.58: The functional blocks of the prototype system. The green lines show the signal and the reference path, while the red ones indicate the controls.

For the test, nine unused channels were drawn from the analogue output of the receiver boards. One of them was used as a reference signal for the timing adjustment. The timing and the delay flat-fielding was performed analysing interleaved calibration pulses ( 25 Hz ), triggered applying an artificial gate centred on them. This prevented any corruption of the equalization, which might have introduced pulses from background or showers.
The recorded counting rates during the delay equalization are inserted in the plot presented in figure 5.59 (a). They optimally fit with an error function, proving the Gaussian nature of the jitter distribution. The crossing points between the horizontal and the vertical arrows indicate when the reference and the signal under test are synchronous. The resultant resolution is very good, around 100 ps as demonstrated in figure 5.59 (b). Moreover, long-term measurements revealed a high stability and the numbers were confirmed even after some days had passed.
The amplitude calibration was not as good as the timing one, but the cause can be pinpointed to the large fluctuations of the pulse. Its amplitude changes up to $10 \%$ in a time-scale of 20 minutes, sometimes manifesting large deviations, far from a Gaussian

[^77]

Figure 5.59: Left: the delay error function of three channels. The $50 \%$ rate value is marked with an horizontal arrow. Right: an image of the analogue pulses at the output of the summation stage (inverted polarity), after the delay adjustment. The blue signal is the gate for the selection of calibration pulses. (From [65])
distribution. However, looking again the pulses in figure 5.59 (b), one can see that the tolerance is less than $20 \%$.

This experience reinforces the original assumption that an accurate and recurrent calibration of both signal amplitudes and delays is fundamental. In fact, the measured amplitude variation in the whole trigger area is on average of the order of $30 \%$, while the time jitter distribution is spread over 1 ns [65]. These fluctuations are caused by intrinsic properties of the electronic chain, but also by external conditions such as temperature and humidity. They might be affected by strong changes, even in the short term, so it is mandatory to keep them well under control.

Finally, some rate scans were performed using a clipping level of 6 phe, during the normal MAGIC data-taking (Fig. 5.60). The cosmic rate is around 23 Hz , which is roughly in agreement with the classical single macrocell rate of the old system ( $\sim 50 \mathrm{~Hz}$ ). These measurements confirm the reliability of the new concept for a small group of


Figure 5.60: Three rate scans recorded during normal data-taking with the prototype of the new system. Below 15 phe the trigger rate is dominated by the $N S B$ while, above 15 phe, $\sim 23 \mathrm{~Hz}$ of cosmic events are registered. (From [65])
pixels. The following step will be to check the same specifications for the whole trigger area.

## The new stereoscopic trigger: MiniPulsar


#### Abstract

Ooking with two eyes is better than with one. This may be a strange state1 ment to summarize the essence of this chapter. By enabling the stereoscopic observation with more than one telescope, several improvements are achievable: lower energy threshold, better angular resolution, more precise impact parameter determination, improved energy reconstruction and higher sensitivity. In this chapter, the main features and some technological aspects of the stereoscopy are presented. Later, an upgrade of the MAGIC trigger system, based on the custom and multi-purpose MiniPulsar board, will be described in detail.


### 6.1 Stereoscopy

In the standard definition, stereoscopy refers to the optical technique to create a threedimensional (3-D) illusion, exhibiting two offset images independently to the left and right eye. More generally, it is the enhancement of the depth perception from a simple two-dimensional (2-D) plane.
The stereoscopy basis resides in the geometrical stereopsis principle. The human eyes, located in two distinct lateral positions some centimetres away, record slightly different images. This disparity of the eyes is exploited by the brain, which merges the images and derives supplementary information regarding the depth and the spatial position of the object in view. The images must be presented simultaneously and well aligned to the eyes.
The sensory human experience of Nature relies on a 3-D space, where width, height and depth are considered unitary elements of an orthonormal base. In contrast, most of the communication tools are based on 2-D supports, like photographs, book images, paintings and technical projection designs. It is spreading the demand to easily pass from one dimension to another. Stereoscopy reconstructs 3-D objects completely by matching some ( $\geq 2$ ) portable independent 2-D supports.
The same approach is used in many other environments such as television, cinema, aerial topography, civil and mechanical engineering and science. For instance, in biology and chemistry, complex molecular structures are often rendered in stereo-pairs. In most cases, it can be applied to any mathematical parameter, which is a function of two variables.
Another feature of stereoscopy, similar to the method used in astronomy, is expressed by
the calculation of the distance from the camera and an object in the picture $[125,101]$. The differences between the images, the cameras' separation, the focal length and some geometrical derivations are the main elements used to estimate it. The precision of the reconstructed position is subordinated by single image quality and the cameras' disposition in relation to the selected target. In this context, high resolution is not sufficient to obtain an elevated quality image. The background must be distinguished from the object, which is not possible if, for example, they have the same uniform colour. On the contrary, a variegated background in contrast with the area of interest, emphasizes the stereoscopic effect.
It will be made clear, in the next subsection, that the stereo $I A C T$ technique has many affinities with the optical stereoscopy described above. The final goal is different, but the way in which the single images are combined to get further discernments, is the same.

### 6.1.1 The stereoscopic technique in IACT telescopes

It has been demonstrated in chapter 2 , that the $I A C T$ technique is strongly based on the analysis of imaging parameters. One of the productive ways to improve the $V H E$ $\gamma$-rays detection quality is to make use of stereoscopy.


Figure 6.1: An example of an atmospheric shower image reconstruction with a stereo array of four telescopes. (From [1])

In VHE gamma astrophysics, stereoscopy records the image of an extended atmospheric shower, initiated by a $\gamma$-ray, with at least two neighbouring telescopes at the same time (Fig. 6.1). The achievable advantage is stringently related to a better image morphology reconstruction and an additional time constraint at the trigger level. Compared to the mono observation, stereoscopic data recording allows a precise three-dimensional determination of the shower core position, an effective Hillas parameter extrapolation, a good energy resolution and a more stringent rejection of muons, hadrons and $N S B$ flashes, which rarely hit two or more telescopes contemporaneously. This should open a new research window toward sources with weak flux or a still not well-defined spatial distribution of the $\gamma$-ray emission region. Moreover, the stereo approach should accurately resolve extended sources inside $1^{\circ}$ and, concerning the temporal profile, the strong variable VHE emitters.

Specific requirements drive the design of the $I A C T$ array. It is important to calculate which is the best distance between the telescopes $\left(D_{t e l}\right)$. Considering that the Cerenkov light pool, from an $E A S$, evolves in first approximation in a circle with a radius ( $R_{\text {eas }}$ ) of more or less 120 m (Fig. 6.2), the maximum acceptable $D_{t e l}$ is fixed by $R_{\text {eas }}$.

Then, the stereo effective area should be determined estimating the common geomet-


Figure 6.2: The average lateral density distribution for different primary energies and impact parameter 0 . On the left, due to primary $\gamma$-rays at 2.2 km a.s.l.. On the right, due to primary protons at 2.2 km a.s.l.. Dotted, dashed and solid lines present distinct Monte Carlo sets. Dotted lines do not consider atmospheric absorption, dashed lines take into account the light in the camera FOV $\left(5^{\circ}\right)$, while solid lines add the constraint of atmospheric absorption. (From [122])
rical light pool portion seen by the telescopes in trigger coincidence ${ }^{1}$ (Fig. 6.3(a)). We can say that the stereo collective area is proportional to the intersection between the collective areas of individual telescopes in stereo trigger (Fig. 6.3(b)). The single col-


Figure 6.3: On the left, a sketch of the common geometrical light pool portion in a stereocell of two telescopes (not to scale). The dimension of each cone is determined by the size of its camera trigger region. On the right, the effective area intersection at the ground level, for an IACT array. (Images credit: A. Bortoluzzi \& F. Dazzi)
lective area for a primary $\gamma$-ray from a point source, can be mathematically expressed as

$$
\begin{equation*}
A_{e f f}^{\gamma}=2 \pi \int_{0}^{\infty} P^{\gamma}(E, r) r d r \tag{6.1}
\end{equation*}
$$

[^78]where $P^{\gamma}(E, r)$ is the detection probability for a gamma with energy $E$ and impact parameter $r$. In case of $n$ telescopes in coincidence, the global detection probability becomes
\[

P_{a r r a y}^{\gamma}=\left\{$$
\begin{array}{c}
P_{\text {telescope }-1}^{\gamma}(E, r)  \tag{6.2}\\
\cdot \\
\cdot \\
\cdot \\
P_{\text {telescope }-n}^{\gamma}(E, r)
\end{array}
$$\right.
\]

Finally, the stereo effective area results

$$
\begin{equation*}
A_{e f f}^{\gamma}(n)=2 \pi \int_{0}^{\infty} P_{a r r a y}^{\gamma}(E, r) r d r \tag{6.3}
\end{equation*}
$$

Reducing the $D_{t e l}$ and the number of telescopes in coincidence, the common effective area increases and consequently the energy threshold is brought down.
Unfortunately, a third aspect prevents reducing the distance between telescopes too much. In fact, for very small $D_{t e l}$, the correlation between the image projections is tangible and every benefit from the stereoscopy is nullified. In addition, when the shower's core is close to the telescopes $(\lesssim 50 \mathrm{~m})$, the image starts to become circular rather than elliptical and the indetermination of the Čerenkov light intensity starts to be considerable (Fig. 6.4(a)). It is reasonable to find a likely compromise in the range $R_{\text {eas }} \div R_{\text {eas }} / 2$.
The previous assumption is always valid for a source at zenith angle zero. For different


Figure 6.4: Left: the fluctuations of the total number of photoelectrons produced in the telescope camera by $\gamma$-rays at different energies. (From [2])
Right: the telescopes' separation, met by the Čerenkov light from an EAS ( $D_{\text {shower }}$ ). (Image credit: A. Bortoluzzi \& F. Dazzi)
sky positions, the crucial parameter is not the distance between the telescopes on the ground, but on the plane perpendicular to the shower axis $\left(D_{\text {shower }}\right)$. This is the telescopes' distance, viewed by the Čerenkov photons (Fig. 6.4(b)). It is a function of both the zenith and azimuth angle, where the maximum discrepancy with $D_{\text {tel }}$ comes out when the shower axis ( $\sim$ pointing direction) is on the same plane of the joining telescope line. The effective distance becomes

$$
\begin{equation*}
D_{\text {shower }}=D_{\text {tel }} \cdot \cos (\theta) \tag{6.4}
\end{equation*}
$$

where $\theta$ is the zenith angle. Hence, the geometrical array configuration, as seen by photons, changes for different observing directions. Up to a zenith angle of $50^{\circ}$ the variation is less than $\sim 25 \%$.

The precision used to calculate the shower parameters, conversely to the energy threshold, increases when 3 or 4 telescopes are used in conjunction. The reason is that, with only two views, the events that fall close to the hypothetical line passing through the telescopes have the same projection angle and may not be reconstructed. As shown in figure 6.5, it is more often possible to find some two out of four quite different independent projections, which allow a very distinct gamma/hadron separation. The


Figure 6.5: Čerenkov light images of vertical $100 \mathrm{GeV} \gamma$-ray (right) and 300 GeV proton (left) detected by an array of four telescopes spaced 100 m apart from each other. Both showers cross the centre of the stereo-cell. While two proton's projections look like $\gamma$-ray (narrow and regular), the other two images indicate the hadronic nature. (From [1])
best array's layout is configured to have always a triangular or a quadrangular stereocell disposition with $\sim 60 \div 120 \mathrm{~m}$ side [1]. This is the right compromise which takes into account the collective area dimension, the background rejection power and the quality of the shower image that is built up. Even the symmetry and the orientation of the stereo-cell arrangement is important to optimize the effective area, because it is also a function of the azimuth angle $[95,44]$. The placement on the ground of the main current IACT telescopes is shown in figure 6.6.


Figure 6.6: The placement layout of the three main IACT telescopes. The dashed circle indicates the HESS-II telescope under construction. The drawing is scaled-down except for the telescope dishes, which are double the scale size. (Image credit: A. Bortoluzzi \& F. Dazzi)

The stereoscopic technique should be very powerful, even in the not sufficiently
explored energy domain between $10 \div 100 \mathrm{GeV}$ [1]. A Monte Carlo simulation of an $I A C T$ array, composed by a square of four medium size telescopes ( $\varnothing 10 \mathrm{~m}$ ), shows a gamma detection rate peak around 100 GeV (Fig. 6.7(a)). The telescope performance is quite conservative for a typical IACT: a) PMT quantum efficiency of $15 \%$; b) mirror reflectivity $85 \%$; c) reflective surface $\sim 80 \mathrm{~m}^{2}$. It is evident that the rejection power for a point source is very high, keeping alive only the noise contribution from electrons, which appear to be very similar to $\gamma$-rays (Fig. 6.7(b)).


Figure 6.7: Left: the differential detection rates of protons, electrons and a $\gamma$-ray point source (index -2.5) with an IACT array of four telescopes. Curves 2 and 4 are calculated with pixel size $0.15^{\circ}$, all others with size $0.25^{\circ}$. Right: the detection rates of $\gamma$-rays (solid lines), protons (dashed) and electrons (dot-dashed) after relaxed software imaging cuts have been applied. (From [1])

After the best single stereo-cell configuration is selected to achieve the requirements for a stringent background suppression, further progress is made by expanding the collective area, thus increasing the number of stereo cells mutually connected and partially overlapped.

### 6.1.2 The MAGIC stereoscopic system

The MAGIC stereoscopic system is composed of two IACT telescopes placed at a distance of 85 m and an angle of $\sim 38^{\circ}$ North-West. As explained in the previous subsection, this configuration, with only two telescopes, is not optimized for the cosmic ray background suppression and the image parameter reconstruction, but it is perfect to guarantee a wide stereo effective area and a low energy threshold. Figure 6.8 shows


Figure 6.8: The Monte Carlo simulation of the MAGIC stereo $\gamma$-rays collection area at the trigger level (dashed line) and after the standard analysis cuts. (From [40])
a flat collection area of $10^{5} \mathrm{~m}^{2}$ for energies higher than 1 TeV , while it is reduced to a factor 10 around 100 GeV .
The stereoscopic observation mode records only events that trigger both telescopes inside a temporal gate of 100 ns . The single telescope trigger imposes the condition that three close compact pixels are simultaneously ( $<6 \mathrm{~ns}$ ) above threshold. The NSB and muon rejection is severe, reducing the final rate to about 200 Hz , mainly due to protons. To compensate for the low number of telescopes in the array, a complex and advanced off-line stereo analysis has been developed. Innovative algorithms succeed in extracting accurately stereo parameters such as the impact point of the shower in the plane perpendicular to its axis (impact parameter) and the height of the shower maximum. The obtained geometrical parameters are then used to extract the energy of the primary particle, with a resolution as good as $15 \div 20 \%$ (Fig. 6.9(a)). The energy threshold, namely the peak of the energy distribution of $\gamma$-ray events after trigger, is approximately 50 GeV for a point source with a differential spectral index of -2.6 .
A relevant advancement in the stereo analysis is made by calculating the primary par-


Figure 6.9: Left: the stereo energy resolution (solid line) and the bias (dashed) obtained with the Monte Carlo simulations of $\gamma$-rays. The resolution corresponds to the $\sigma$ of the Gaussian distribution $\left(E_{\text {rec }}-E_{\text {true }}\right) / E_{\text {rec }}$, while its mean value is the bias. Mild cuts are applied: hadronness $<0.6, \theta^{2}<0.03$. Right: the stereo angular resolution as a function of the estimated energy obtained with the Crab nebula data sample (points) and compared with the Monte Carlo simulations (lines) for the 2-D Gaussian fit (solid line, full circles) and the $68 \%$ containment radius (dashed line, empty triangles). The resolution is defined as the standard deviation of the 2-D Gaussian distribution of the reconstructed events direction. For a point-like source, it coincides to a radius containing $39 \%$ of the $\gamma$-rays. (From [40])
ticle direction. The simple crossing point between the main axis of the event ellipses is not always satisfactory and an upgraded method, the so-called Stereo DISP-RF, has been introduced. For each telescope image, the DISP parameter (the angular distance between the centre of gravity of the image and the estimated source position) is estimated using multidimensional decision trees (Random Forest). Then, the crossing point of the main axes and the two DISP parameters are combined. The resulting angular resolution is considerably improved, as underlined by the plot 6.9(b). The Stereo DISP-RF method allows us to obtain a precision of $\sim 0.07^{\circ}$ at 300 GeV .

In the domain of few hundred GeV , the current MAGIC sensitivity ${ }^{2}$ is less than $0.8 \%$ of the Crab nebula flux, in agreement with the Monte Carlo predictions (Fig. 6.10(a)). In comparison with the single telescope performance, the improvement in significance

[^79]is compatible by a factor $2 \div 3$. An incontrovertible proof of the obtained progress is given by the stereo $C r a b$ nebula spectrum in the range 70 GeV to 11 TeV , which agrees with the results of the other $I A C T$ telescopes Fig. 6.10(b).


Figure 6.10: Left: the integral sensitivity of the MAGIC stereo system for data (black solid line) and Monte Carlo (black dashed line), compared with the MAGIC-I telescope (solid gray line) one. Right: the spectrum of the Crab nebula obtained with the MAGIC stereo system (black curve) compared with other experiments (gray curves). (From [40])

### 6.2 The MAGIC stereoscopic trigger

In 2009, the second telescope (MAGIC-II) started to operate with MAGIC-I. During the commissioning phase, they worked independently, tracking simultaneously the same sources. The off-line analysis compared the arrival time in both telescopes, flagging as originated by the same shower if inside a small temporal gate of some tens ns. This was a preliminary and simple way to detect stereo images, in order to extract the stereoscopic parameters. At the analysis level, the procedure worked very well and immediately the effectiveness was clear in the event reconstruction. Nevertheless, no hardware stereo trigger was applied to reduce the accidental and muon rate that could also improve the dead time and lower the pixel threshold without saturating the $D A Q$. In order to work in a muon-free background environment, a narrow time coincidence trigger between the two telescopes was implemented in a second stage. Obviously, this stereo trigger decision comes only after the local triggers have been selected. As shown in figure 6.11, the single telescope trigger pattern is formed by eight different local signals [55]. Some of them, such as the LT1 (standard digital trigger), SUMT (analogue Sum-Trigger) and the LT3 (stereo trigger), are source triggers, while others, such as CAL (calibration trigger), PED (pedestal trigger) and INJ (pulse injector trigger), are used for calibration and technical runs. The readout can be activated by one of these local triggers or by the stereoscopic trigger LT3.
The interface between the local triggers and the readout is made by the prescaler. This board, located in the LT2 system, uploads the trigger pattern and controls the rate to prevent the saturation of the acquisition system. All information is provided via a $L V D S$ bus in order to exclude faint triggers due to the noise.
Some examples could optimally clarify the concept of the system. Supposing that the SUMT is enabled in MAGIC-I, and LT1 in MAGIC-II, the saved events have respectively passed the Sum-Trigger and Level 1 trigger barrier. On the other hand, when the $L T 3$ bit is enabled, showers that exceed in both detectors the standard local


Figure 6.11: A simplified diagram of the trigger electronic chain. The 8 local triggers enter in the prescaler board to activate the final enable signal for the readout. The stereo trigger flag is defined inside the GTS logic. (© F. Dazzi)
trigger constraints inside a common timing window of 100 ns , are recorded (Fig. 6.12).


Figure 6.12: The camera image projections of a $\gamma$-ray event triggered by the stereoscopic system and recorded by telescopes.

There are a lot of possible trigger combinations, which are handled by a dedicated system, the so-called GTS (Global Trigger System) [109]. The GTS manages both mono and stereo trigger associations. The main functions of the $G T S$ can be understood looking at the simplified diagram of the trigger array system (Fig. 6.13(a)), while all the connections with the other subsystems are shown in figure 6.13(b). Its configuration sets the readout operational mode in order to sample events triggered by the local imposed trigger and/or by the stereo blend. In the last case, the number of telescopes


Figure 6.13: Left: an overview of the trigger system for the MAGIC telescopes array. Two telescopes are controlled by the GTS. Right: the detailed connections between the GTS and other subsystems such as the local triggers and the readout. (From [109])
involved in the final decision can be fixed up to four units ${ }^{3}$. This flexibility provides the possibility to change the dimension and the stereo-cell layout. The assignment of the telescopes in a specific stereo-cell is called "trigger partition" (Fig. 6.14). The current system can control up to four trigger partitions, namely four independent stereo-cells. The $D A Q$ is armed in any case by the local trigger, while the final decision to accept the event is taken only if one of the enabled trigger partitions returns a positive flag.


Figure 6.14: A sketch of the trigger partitions. The orange partition is a stereo-cell composed of the telescopes CT1 and CT2. The green one works in single mode with the $C T 3$, as well as the blue one with the CT4. The last yellow partition is not in use. (C) F. Dazzi)

### 6.2.1 Signal path length and timing

The MAGIC stereo trigger (LT3), a sub-function of the GTS, makes a tight time coincidence between both telescopes, taking into account possible sources of relative delay in the event arrival times. Basically there are two main sources, one fixed, due to the different electronic chain paths, and another variable coming from the telescopes' pointing direction.

[^80]The first component arises when the signal path length from the reflective surface to the LT3 is considered. There are several known contributions, some intrinsic to the array's geometry and subsystems' arrangement, and others from the different electronics used in the two telescopes. A simple list is presented, where $\Delta \mathrm{t}$ is defined as $\left(\mathrm{t}_{M 1}-\mathrm{t}_{M 2}\right)$ :

* The mirrors' shape and their supports are different. An uncertainty of some centimetres is present between the reflective dish and camera. ( $-0.5 \mathrm{~ns} \lesssim \Delta \mathrm{t} \lesssim$ 0.5 ns )
. The devices used in the camera electronics are completely dissimilar, such as PMTs, charge transimpedance preamplifiers and VCSEL, but the layout is very comparable. $(-8 \mathrm{~ns} \lesssim \Delta \mathrm{t} \lesssim 8 \mathrm{~ns})$
* The optical fibres' length is not exactly the same. In MAGIC-I the propagation time is 802 ns , while in MAGIC-II it is 810 ns . ( $\Delta \mathrm{t}=-8 \mathrm{~ns}$ )
* The logic of receiver boards is equal but the components are different. ( $-5 \mathrm{~ns} \lesssim$ $\Delta \mathrm{t} \lesssim 5 \mathrm{~ns})$
* Different cabling between the receiver boards and the LT1 crate. ( $\Delta \mathrm{t} \sim 15 \mathrm{~ns}$ )
* The LT1 systems have installed different backplanes, covering different trigger areas in the camera. ( $\Delta \mathrm{t} \sim 4 \mathrm{~ns}$ )
* Different cabling between the LT1 crate and the GTS. ( $\Delta \mathrm{t} \sim 15 \mathrm{~ns}$ )

After the measurement of the relative delay performed in La Palma, no delay has been applied at the input of the $L T 3$, because the various contributions annul each other. The second component, correlated to the different arrival times of the Čerenkov light front on the detectors, is corrected every 10 s introducing an additional delay, calculated from the telescopes' pointing coordinates. As shown in figure 6.4(b), the same shower arrives to the telescopes covering two different paths, hence resulting in distinct timing. The spatial difference corresponds to the variable $\Delta s$, function of the azimuth and zenith angles. $\Delta s(\theta, \varphi)$ can be expressed as the scalar product between the vector joining the two telescopes $(\overline{O P})$ and the pointing direction versor $\bar{u}$, when it has the same direction of the shower core axis. The vector $\overline{O P}$ has an azimuth angle of $38^{\circ}$, as reported in subsection 6.1.2. In figure 6.15, a simple sketch shows how they appear in a Cartesian base. The $\overline{O P}$ coordinates, expressed in metres, are

$$
\begin{aligned}
\overline{O P} & =\left(\begin{array}{lll}
D_{\text {tel }} \cdot \sin \left(38^{\circ}\right), & D_{\text {tel }} \cdot \cos \left(38^{\circ}\right), \quad H_{\text {tel }}
\end{array}\right) \\
& =\left(\begin{array}{lll}
85 \cdot \sin \left(38^{\circ}\right), & 85 \cdot \cos \left(38^{\circ}\right), & 0.14
\end{array}\right) \\
& =\left(\begin{array}{lll}
52.33, & 66.98, & 0.14
\end{array}\right)
\end{aligned}
$$

where $H_{\text {tel }}$ is the elevation difference of $14 \mathrm{~cm}^{4}$. The versor $\bar{u}$ coordinates are

$$
\bar{u}=(\sin \theta \cdot \sin \varphi, \quad \sin \theta \cdot \cos \varphi, \quad \cos \theta) ;
$$

the relative path obtained by the scalar product, ignoring $H_{t e l}$, is

$$
\begin{equation*}
\Delta s=\overline{O P} \cdot \bar{u}=\sin \theta \cdot(52.33 \cdot \sin \varphi+66.98 \cdot \cos \varphi) ; \tag{6.5}
\end{equation*}
$$

the corresponding plot is shown in figure 6.16.
Every time the central control updates the telescopes' position, the delay contribution

[^81]

Figure 6.15: Geometrical representation of the the Čerenkov light paths towards the two dishes as a function of the azimuth and zenith angles $(\theta, \varphi)$. The vector $\overline{O P}$ defines the position of MAGIC-I with respect to MAGIC-II, while the versor $\bar{u}$ indicates the telescopes' pointing direction. The scalar product between these two vectors determines the paths' spatial difference. For simplicity, the elevation between the two telescopes is not depicted. (Image credit: A. Bortoluzzi \& F. Dazzi)


Figure 6.16: The graphic representation of the function $\Delta s(\theta, \varphi)$ in the interval $0 \div \pi / 2$ for the zenith and $-\pi \div \pi$ for the azimuth. One maximum of the plot is visible at the coordinates: $\theta=90^{\circ}$ and $\varphi=38^{\circ}$. (C) F. Dazzi)
is calculated again and the signals' synchronization is applied at a level of the local telescope triggers. This operation is done with a very fast algorithm, because the available time range is limited by synchronization with the readout system. Even if the memory depth of DRS2 is restricted to only 512 ns , the main constraint is given by the acquisition trigger to $M U X-F A D C$. It occurs 320 ns after the local trigger is generated. The different arrival time on the telescopes, which is the largest source of delay, can be calculated from equation 6.5. The maximum is around $250 \mathrm{~ns}^{5}$, which should be added to the cabling contribution of $\sim 15 \mathrm{~ns}$ and the LT3 propagation time of $\sim 48 \mathrm{~ns}$.

[^82]Equation 6.5 is true for particles that have a trajectory along the telescope pointing direction. An uncertainty is introduced if we consider a generic shower falling inside the telescope's FoV. The new spatial variable is called $\Delta s^{\dagger}$ and is given by the scalar product between the vector $\overline{O P}$ and the shower axis ( $\bar{n}$ ), which can be far from $\bar{u}$ up to $3.5^{\circ} . \Delta \theta$ and $\Delta \varphi$ are the angular variations respect to the pointing direction.

$$
\begin{align*}
\Delta s^{\dagger} & =\overline{O P} \cdot \bar{n} \\
& =\sin (\theta \pm \Delta \theta) \cdot(52.33 \cdot \sin (\varphi \pm \Delta \varphi)+66.98 \cdot \cos (\varphi \pm \Delta \varphi)) \tag{6.6}
\end{align*}
$$

The maximum difference between $\Delta s$ and $\Delta s^{\dagger}$ tells which is the foreseen jitter of the arrival time of Čerenkov flashes. Considering that $\Delta \theta$ and $\Delta \varphi$ are close to zero, we may assume the following relation.

$$
\begin{align*}
\Delta s-\Delta s^{\dagger} & =d \Delta s=\frac{\partial \Delta s}{\partial \theta} d \theta+\frac{\partial \Delta s}{\partial \varphi} d \varphi  \tag{6.7}\\
& =\cos \theta(P \sin \varphi+Q \cos \varphi) d \theta+\sin \theta(P \cos \varphi-Q \sin \varphi) d \varphi
\end{align*}
$$

where $P=52.33 \mathrm{~m}$ and $Q=66.98 \mathrm{~m}$. Then the maximum is found imposing:

$$
\begin{align*}
\nabla(d \Delta s) & =\left(\frac{\partial(d \Delta s)}{\partial x} ; \quad \frac{\partial(d \Delta s)}{\partial y}\right)=0 \\
& =\left\{\begin{array}{l}
-\sin \theta(P \sin \varphi+Q \cos \varphi) d \theta+\cos \theta(P \cos \varphi-Q \sin \varphi) d \varphi=0 \\
\cos \theta(P \cos \varphi-Q \sin \varphi) d \theta-\sin \theta(P \sin \varphi+Q \cos \varphi) d \varphi=0
\end{array}\right. \\
& =\left\{\begin{array}{l}
(P \sin \varphi+Q \cos \varphi)=\frac{d \varphi \cos \theta}{d \theta \sin \theta} \cdot(P \cos \varphi-Q \sin \varphi) \\
\cos \theta(P \cos \varphi-Q \sin \varphi) d \theta-\sin \theta(P \sin \varphi+Q \cos \varphi) d \varphi=0
\end{array}\right.  \tag{6.8}\\
& =\left\{\begin{array}{l}
(P \sin \varphi+Q \cos \varphi)=\frac{d \varphi \cos \theta}{d \theta \sin \theta} \cdot(P \cos \varphi-Q \sin \varphi) \\
\cos \theta(P \cos \varphi-Q \sin \varphi) \cdot\left(d \theta^{2}-d \varphi^{2}\right)=0
\end{array}\right. \\
& =\left\{\begin{array}{l}
\theta=90^{\circ} \\
\varphi=128^{\circ}
\end{array}\right.
\end{align*}
$$

For symmetry, it is sufficient to consider this maximum, which returns a $d \Delta s$ of 5.19 m , that is 17.3 ns . The intrinsic fluctuation of $\Delta \mathrm{s}^{\dagger}$ generates a time jitter at the $L T 3$ input level, confirmed experimentally with the picture 6.17. The recorded jitter is a little bit higher than the prediction of equations 6.8 , but the contribution from the electronic chain has to be included.
The spread of the relative arrival time distribution can be used to discriminate particles that are not coming from the tracked source. For a point-like source, the minimum time gate is delimited by the angular resolution acceptance at very low energies and by the variation of the Čerenkov angle for huge events. Conversely, for extended sources that do not exceed the FoV, the limit is fixed by their extension. Obviously, these are ideal limits for electronic systems without jitter. In the first case, the maximum of equation 6.7 , with $\mathrm{d} \theta$ and $\mathrm{d} \varphi$ equal to $0.1^{\circ}$, is $14 \mathrm{~cm}(\sim 0.5 \mathrm{~ns})$. Lowering the LT3 gate in the range $0.5 \div 17.3$ ns would improve significantly the background exclusion capacity.
Even if the current rejection power of the trigger system is of the order of $\sim 10^{4}$, most of the recorded events are hadrons, while $\gamma$-rays of interest are still completely negligible. Assuming that the hadrons are isotropically distributed, the telescope trigger acceptance is determined by the solid angle of the FoV ( $\Omega_{\text {FoV }}$ ). Applying the stereo relative arrival time as discriminator, the trigger acceptance for a point-like source is


Figure 6.17: The picture of the $L T 3$ jitter measured at La Palma during normal datataking. The yellow signal is the local trigger from MAGIC-I at the LT3 input, the blue one the signal of MAGIC-II.
reduced proportionally to the solid angle seen by the angular resolution $\Omega_{\xi}$. Defining $R_{\text {FoV }}$ as the current stereo trigger rate and $R_{\xi}$ the new rate applying a more stringent gate, the ratio should be:

$$
\begin{align*}
\frac{R_{\xi}}{R_{F o V}} & \propto \frac{\Omega_{\xi}}{\Omega_{F o V}} \\
& \propto \frac{2 \pi(1-\cos (\Delta \xi / 2))}{2 \pi(1-\cos (\text { FoV/2))}}  \tag{6.9}\\
& \propto\left(\frac{1-\cos (\Delta \xi / 2)}{1-\cos (\text { FoV } / 2)}\right)
\end{align*}
$$

where the solid angle formula of cones with aperture $\alpha=\mathrm{FoV}$ and $\Delta \xi$ is used. For the MAGIC telescopes, we obtain:

$$
\begin{equation*}
R_{\xi} \propto R_{F o V} \cdot\left(\frac{1-\cos (\Delta \xi / 2)}{1-\cos (F o V / 2)}\right)=R_{F o V} \cdot 8.16 \cdot 10^{-4} \tag{6.10}
\end{equation*}
$$

where $\Delta \xi=0.1^{\circ}$ and $F o V=3.5^{\circ}$.
An additional rejection factor of three orders of magnitude can be introduced in the electronic chain. Actually, the local trigger arrival time is stored in on-line histograms with 25 ns resolution. Amending this information, even if it remains far from the ideal resolution of some ns, could be applied at the hardware level to reject some of the showers abundantly out of the pointing direction.

### 6.2.2 The Pulsar trigger board

The core of the GTS is a Pulsar (PULSer And Recorder) board (Fig. 6.18), a 9U VME motherboard developed by the University of Chicago for High Energy Physics applications [94]. In MAGIC-II, it is also used for the readout system and the management of the $D A Q$ control [15].
The Pulsar board houses three powerful FPGAs Altera APEX20K400 that make it very versatile for any purpose. This choice is largely driven by data transfer requirements, as this chip has a 652 pins $B G A$ package with about $500 \mathrm{I} / \mathrm{O}$ connections. Furthermore, it is supplied by an internal 26 KiB memory and two of them are connected to two fast SRAM memories, Cypress CY7C1350-F. This memory is a synchronous-pipelined burst $S R A M$ designed specifically to eliminate wait states during write/read transitions, dramatically improving the throughput. The storage capacity of 4 Mb is distributed to a common architecture $128 \mathrm{Kib} \times 36$. These two $F P G A s$ exercise an interface with


Figure 6.18: On the left, the top view of the Pulsar board. The three big gray squares are the Altera FPGAs. On the right, the bottom view of the board, with connected two mezzanines. (From [94])
the I/O modules, while the third one merges data from the previous two devices and prepares them for a potential transmission through the VME bus.
The board is predisposed to accommodate up to four mezzanines, which can be used to implement some additional functions or to extend the compatibility with other signal formats and any industrial standard link. Every mezzanine has 83 bidirectional connections visible to the motherboard $F P G A s$, fully compatible with the transmission system $S$-Link ${ }^{6}[60]$. The PCB dimensions meet the CMC standard (Common Mezzanine Card), so it is possible to implement different communication standards based on mezzanine cards and the same interface with the Pulsar board. The data flow power is enhanced by other four $L V D S$ connectors at the front of the board with more than 200 connections. In the case of the Pulsar trigger board, the I/O on the front side of the board handle the following signals:

A 64-bit bus for trigger input pattern.
A 64-bit bus for trigger output pattern.
The mezzanines manage these other signals:
The four local triggers from the telescopes. The LT1 signals are available on coaxial differential cables with $100 \Omega$ impedance, while the Sum-Trigger ones on a coaxial single-ended cable with $50 \Omega$.

The four output trigger partitions.
A 32-bit bus for the global trigger number.
The global veto signal and some auxiliary calibration triggers.
On the first two mezzanines, the local input and the output triggers are synchronized using the programmable delay chips Data Delay Devices 3D3428-5 with a maximum delay of $1.2 \mu \mathrm{~s}$, divided in 255 steps for a resolution of $5 \mathrm{~ns} /$ step (Fig. 6.19).

[^83]

Figure 6.19: The four mezzanines located on the back side of the Pulsar trigger board. The first two accept the local triggers from the single telescopes and they send around the global stereo triggers, while the last one distributes the global trigger number.

### 6.3 The future stereoscopic trigger

As described in section 4.9, an upgrade of the telescopes is under way. An important goal is to improve the stereoscopic trigger, on the one hand reducing the cabling delay contribution and on the other introducing a new powerful and compact board to replace the Pulsar trigger board. In fact, this board is no longer in production and the available units will be used for the MAGIC-I readout upgrade. The main idea is to exchange all the Pulsars with a service aim, saving some of them as spares. The replacement board is called MiniPulsar, a $6 \mathrm{U} V M E$ card that can be used in the trigger and $D A Q$ environments.

### 6.3.1 Electronic room upgrade

In subsection 6.2.1, the useful time windows for the stereo trigger has been calculated. The available gate is very tight and observations at very high zenith angles ( $\gtrsim 60^{\circ}$ ) are prevented by the hugely different arrival times on the two telescopes. This limit could become narrower for a telescope array extension, compromising the stereoscopic trigger efficiency. For the MAGIC upgrade, the rearrangement of the electronic room took into account the relative rack position in order to downsize the cable length between different source of physics triggers. In figure 6.20 , the layout before and after the upgrade is shown. The potential physics triggers come from the orange racks (LT1) and the green ones (Sum-Trigger). Currently, the configuration which returns the shortest connections between them has been chosen.

The variation of some important operative conditions affects the circuit performance, causing a degradation in the electrical signal quality. Temperature and humidity could change some parameters of the electronics, resulting in functionality and reliability problems. A huge temperature gradient varies the propagation time, introducing different relative delays. Moreover, a temperature enhancement increases the signals' jitter, lowering the timing resolution. To prevent this, in the new electronic room all racks are closed and the internal temperature and the air flow are monitored by an adequate cooling system.

### 6.3.2 MiniPulsar general description

The MiniPulsar (Fig. 6.21) takes inspiration from the Pulsar board. Its main goal is to substitute the Pulsars that have a service role in the MAGIC electronic chain.


Figure 6.20: On top, the photo of the new electronic room. (Image credit: J. L. Lemus) On bottom, the arrangement before (left) and after (right) the MAGIC upgrade. (C) F. Dazzi)

The production of Pulsar boards has stopped and some components are obsolete. The necessity to save as many spares as possible for the readout is vital for the experiment. Moreover, the Pulsar was created to satisfy several purposes in the data transmission environments, but it was not realized to manage isochronous signals with sub nanosecond precision. The design of new MiniPulsar tries to meet the current requirements.

The MiniPulsar is a 6 U VME motherboard, which houses a low-cost and versatile FPGA Cyclone-II (EP2C70F896) from Altera. It is a programmable device containing a 2-D row and column-based architecture to implement custom logic (Fig. 6.22(a)). Column and row wires provide signal interconnections among logic array blocks (LABs), embedded memory blocks, and embedded multipliers. Every LAB is constituted by 16 logic elements (LEs ${ }^{7}$ ) (Fig. 6.22(b)), for a total amount of 68416 LEs. It appears in a very compact $B G A$ package with 896 pins, of which 622 are usable I/O. It can provide up to 1.1 Mb of embedded memory, a global clock network of 16 lines distributed to

[^84]

Figure 6.21: Left: the top view of the first MiniPulsar prototype (version 1.8). Right: the bottom view.
all resources, four PLLs and 150 embedded multipliers. This chip can be configured to

(a) Cyclone-II architecture

(b) Cyclone-II logic element

Figure 6.22: Left: the architecture of a generic Cyclone-II device. Right: the schematics of the logic element. (From Cyclone-II handbook)
perform complex combinational functions between digital signals of different formats at a maximum data rate of 805 Mbps for inputs and 640 Mbps for outputs. In the current design, for single-ended lines the LVTTL is adopted, while for differential lines the LVDS. The I/O pins are grouped together into eight I/O banks, and each bank has a separate power bus. The preferred I/O standard can be selected for a given bank, increasing the interconnection flexibility. The maximum internal clock frequency, reachable for simple data process, is 405 MHz (speed grade -6), but it changes according to the implemented function. In addition, some analogue features, such as the slew rate and drive strength on each output pin, can be programmed.
Cyclone-II devices support a broad range of external memory interfaces. In the MiniPulsar project, a DDR2 SRAM memory (CY7C1380D) from Cypress is embedded with a high speed rate bus at 333 Mbps . The memory integrates $524288 \times 36$ cells with advanced synchronous peripheral circuitry and a two-bit counter for internal burst
operation. Most of the connections, such as addresses and data, are synchronous, gated by registers controlled by a positive edge-triggered clock input.

The main functions of MiniPulsar board are emphasized in figure 6.23. Most of the Pulsar features are perfectly reproduced in the new project. The innovation lies in the architecture, which is significantly simplified. One single FPGA manages all the stages and both the data-gathering and the data-processing, providing higher performance than before. The board dimension is reduced to $70 \%$ (from 9 U to 6 U ) with the single drawback that it can host three mezzanines out of four, but the great advantage that it can be moved to the standard LT2 VME crate, closer to the local trigger drivers. It is very portable and easy to adapt in every custom test set-up, ensuring a fast and effective integration.


Figure 6.23: The main functions diagram of the MiniPulsar top side (left) and bottom side (right). The front I/O connectors, $S V T$ and $L 1$ are exactly the same as the Pulsar board. Even the pin-out for the mezzanines is the same. (© F. Dazzi)


Figure 6.24: Left: the complete routing on the fourteenth layers of the MiniPulsar board. Most of the traces are connected to the central FPGA. Right: the complex stack-up of the board.

The optimization, for a generic high-speed timing purpose, is likely to be one of the most essential new features of this board (Fig. 6.24(a)). Every single trace has
been accurately studied in terms of skew, impedance and cross-talk. For this reason, a complex $P C B$ stack-up has been designed following the standard signal integrity rules (Fig. 6.24(b)). It is composed of fourteen layers, four of which are internal planes for high-speed signals, completely interposed between two internal ground planes in order to isolate them from the electromagnetic background noise. The other two external layers, on the top and bottom, are for slow control signals. The layers' thickness and the material dielectric constants have been carefully calculated to obtain a final transmission line impedance of $50 \Omega$ for single-ended traces and $100 \Omega$ for the differential one.
The I/O wire length is equalized to keep the skew down as much as possible. The lines to the front connectors are designed with a maximum timing difference of 50 ps , while the traces to the mezzanines present a more relaxed constraint at 250 ps . The meandering routing technique has been applied, as displayed in figure 6.25 . The maximum wave dimensions and the minimum distance between neighbour lines have been fixed to obtain a cross-talk lower than $10 \%$.


Figure 6.25: The complete view (left) and a zoom of a restricted zone (right) of the signal layer number one. The meandering traces for the length/timing adjustment are shown.

### 6.3.3 MiniPulsar prototype

The MiniPulsar prototype (version 1.8) can be divided in five important stages, as illustrated in figure 6.23. Every single part has been independently and deeply verified, spotting the design errors and wrong functionalities. A specific test bench firmware ${ }^{8}$ has been uploaded to check the board performance. Afterwards, a report of the stage list with the final test result is made. The symbol " $\sqrt{ }$ " indicates a completely successful upshot, while " $\boldsymbol{X}$ " means there is something wrong.
$\mathbf{X}$ Power distribution
$\mathbf{x} F P G A$
$\checkmark$ External $S R A M$
$\checkmark$ Front I/O connectors

[^85]$\mathbf{X}$ Mezzanines connections
The main power line is taken from the $5 \mathrm{~V} V M E$, then it is transformed in 3.3 V , 2.5 V and 1.2 V . The first two power lines feed the I/O drivers, the mezzanines and the $F P G A$, while 1.2 V supplies its core.
Switching voltage regulators have been selected, because they provide high current ( $\sim 10 \mathrm{~A}$ ) generating not much heat. This feature is ideal when the board has to feed power-consuming mezzanines in provisional test environments without cooling systems. The disadvantage is the high noise due to the regulators switching frequency that couples with some high speed wires.
In figures $6.26(\mathrm{a})$ and $6.26(\mathrm{~b})$, the 3.3 V power line is shown respectively in DC and AC oscilloscope mode. The voltage is not stable and the peak-to-peak variation is $\sim 500 \mathrm{mV}$. Searching the source of noise, using the oscilloscope probe as an antenna ${ }^{9}$, two components can be distinguished. The first noise arises when the probe-antenna is located close and parallel to the regulator transformer (Fig. 6.26(c)), while the second when close and parallel to the $P C B$ and the chips (Fig. 6.26(e)). By shielding the regulator with a small metal box, connected to ground, the first contribution with a square shape disappears (Fig. 6.26(d)), whereas the regular spikes still survive (Fig. 6.26(f)). The likely two independent sources of noise are the $P W M$ control ${ }^{10}$ in the voltage regulator ("square noise") and the high frequency switching in the $F P G A$ and I/O drivers (spikes). In fact, the spikes present a frequency equal to that applied in the $F P G A$.

Concerning the $F P G A$ and the surrounding circuitry, three design mistakes have been spotted during the tests. In the first case, a wrong package for the external flash memory (EPCS64) had been selected. This device is important because in the SRAMbased devices, such as the Cyclone-II, configuration data must be reloaded each time the chip powers up, the system initializes, or when new configuration data is needed. EPCS64 is a flash memory with a serial interface that can store configuration data and reload it to the $F P G A$ upon power-up or reconfiguration. For this prototype version, the problem has been fixed with a hand-made wiring between the chip and the $P C B$ pads (See in figure 6.21 the green wires on the bottom area of the top layer).
The second fault was the missing connection of two important configuration pins: $A S D O$ and $n C S O$. They send a control signal from the $F P G A$ to the serial configuration device in active serial mode. $A S D O$ is used to read out stored data, while $n C S O$ to enable the configuration device. As before, the solution has been further hand-made wirings (See in figure 6.21 the green wires on the central area of the top layer).
The third one was caused by the connection to 1.2 V instead to 3.3 V of one of the eight power banks in the $F P G A$. More than half the generating signals for the mezzanine nr. 1 have a wrong amplitude of 1.2 V , not compatible with $L V T T L$ standard. There are no possible solutions for the prototype version.

The $S R A M$ interface and the I/O connections present no problems and work properly. In figure $6.27(\mathrm{a})$, an example of a $L V D S$ signal output is shown. The yellow line is the positive signal, while the blue one the negative. Their difference is mathematically represented with the orange function. In figure 6.27 (b), the main controls for the $S R A M$ memory are recorded.

A major mistake was made in the connectors of mezzanines number 1 and 3 . Unfortunately they are wrongly orientated by $180^{\circ}$ around the axis perpendicular to the connectors themselves. A small $P C B$ adapter has been set up as a temporary solution.

[^86]
(a) The 3.3 V power line in DC mode

(c) Radiated noise without shield on the vertical plane

(e) Radiated noise without shield on the horizontal plane

(b) The 3.3 V power line in AC mode

(d) Radiated noise with shield on the vertical plane

(f) Radiated noise with shield on the horizontal plane

Figure 6.26: Measurements about the power system quality and study of the noise. On the top, the 3.3 V voltage recorded in DC (a) and AC mode ( b ). In the centre, the electromagnetic noise radiated around the regulator, without (c) and with (d) a metal box shield. On the bottom, the same estimation, without (e) and with (f) shield, parallel to the $P C B$ surface.

### 6.3.4 MiniPulsar final version

A new version ${ }^{11}$ of MiniPulsar board has been designed in order to fix the bugs of the first prototype. The main modification has been made in the power stage, where a big source of noise has been discovered. A triplet of different capacitor values on the supplies has been used in order to prevent resonances that could create unwanted

[^87]

Figure 6.27: Left: the $L V D S$ output measured on the connector L1 OUT pin 31. Right: the clock (yellow), the global write (blue) and the output enable (violet) signal controls for the external $S R A M$ memory.
spikes. This should minimize the local impedance to the ground plane and increase the immediate available charge during fast transients. Even under the FPGA package, the capacitance array has been improved.
The MiniPulsar is a multi-purpose board that can be employed in different systems. It should be very adaptable at any environment, serving always the requested efficiency. Hence, there is not an unique power solution which can provide high current and low noise, without dissipating a lot of heat. The implementation of a design, compatible with three distinctive power systems, has been the chosen strategy. The new $P C B$ can host three types of voltage regulators, one linear and two switching.
Following the main features of the three architectures:

* The switching regulator, selected for the prototype board, is still available in the new version. PTR08100W, from Texas Instruments, is a highly integrated, low-cost and variable module that delivers up to 10 A . The package layout is compatible with the standard TO-220 linear regulators, but it provides output current at a much higher efficiency and with much less power dissipation, thereby eliminating the need for a heat sink. Its characteristics make it attractive for applications that require high current without cooling control. The drawback is the elevated noise, unpleasant for analogue and high speed conditions (green and blue hands in figure 6.28).
* Using the same footprint with a slightly different passive circuitry, three linear regulators can be mounted. TPS75933 and TPS75925 supply the 3.3 V and the 2.5 V lines (blue hands in figure 6.28 ), while LP38843 the 1.2 V part (green hand in figure 6.28 ). The first two chips offer 7.5 A current output with a low dropout. The LP38843 is a 3 A output current regulator, typified by a fast response and an excellent stability. This configuration needs the heat sink and a good air flow control. It is recommended to use this as first choice, when fast and high quality signals are treated.
* Last option is a compromise solution based on a switching micro-module. The LTM4608, from Linear Technology, is a complex 8 A switch mode power supply (red hands in figure 6.28). It supports an output voltage range of 0.6 V to 5 V , set by a single external resistor. The current mode architecture enables a very


Figure 6.28: The new power stage of the MiniPulsar v.2.0. The small coloured hands indicated the new voltage regulators. The green hand is the 1.2 V footprint, while the blue hands are the 3.3 V and the 2.5 V . It possible to mount the switching or the linear regulators. The red hands show the switching module from Linear Technology.
fast transient response to line and load changes without sacrificing stability. The typical switching frequency is 1.5 MHz , but for noise sensitive applications, it can be externally synchronized from 0.75 MHz to 2.25 MHz . Even spread spectrum switching can be implemented in the design to reduce noise. Finally, the device supports an output voltage tracking for voltage margining.

## $\rightleftharpoons$

## Conclusions and outlook


#### Abstract

T HE CURRENT upgrade of the MAGIC telescopes moves in two ambitious and crucial directions. The first is the reduction of the energy threshold down to around 15 GeV , where interesting physics has still to be explored. The second is a significant improvement of the cosmic ray background rejection efficiency, both with advanced image analysis techniques and with innovative electronic systems and novel photodetectors. In this sense, the new Sum-Trigger-II plays an important role, especially for the first aim. In this last chapter the outcomes of this thesis work and the future perspectives are summarized.


### 7.1 Summary of the Sum-Trigger-II project

The stereo Sum-Trigger-II is an ambitious and complex project, which is realized to improve the detection power of low energy events, born from a collaboration between the MAGIC-Italia group, mainly Padova, Udine and Pisa, and the Max-Planck-Institut für Physik in Munich. All these teams have well-established knowledge and experience in the design of the trigger architectures for $I A C T$ experiments. In fact, the Italian groups have built the standard digital trigger and the current LT3, while the German group has developed the prototype of the first Sum-Trigger.

The compatibility with the already running layout ${ }^{1}$ and the mechanical constraints have been the starting points of the planning. Then, the attention has been focused on the challenging electronic properties, demanding selection algorithms adapted to the Čerenkov flash features. Since the Sum-Trigger-II principle is established on temporal and topological constraints, a full control of the signal elaboration is decisive. High bandwidth, good signal integrity and excellent timing synchronization are the key factors for a successful system, as demonstrated in the prototyping phase.
Most of the system, especially the selection event stage, is realized with analogue electronics, while the digital devices take care of the control and data processing.

The Sum-Trigger-II is currently under construction, and it is not yet operational, but it will be one of the most important elements of the MAGIC upgrade. Some subsystems have already demonstrated good behaviour, within design specifications. Others require additional studies and tests.
On the basis of Monte Carlo simulations, we expect that the new system will reach an

[^88]energy threshold of $\sim 20 \mathrm{GeV}$ and a collection area of $20000 \mathrm{~m}^{2}$ in mono mode datataking. Compared with the prototype Sum-Trigger, the improvement is significant, especially in the number of triggered events. In addition, the performance is even more interesting in stereo mode data-taking, where the analysis will also benefit in the event reconstruction. The energy threshold is lowered in the domain under 20 GeV with an impressive collection area of $\sim 40000 \mathrm{~m}^{2}$.

### 7.2 Main goals

This innovative project has three main goals. The first is a larger trigger area which increases the telescope sensitivity and allows wobble mode data-taking.
The second goal is the implementation of a complete automated tuning of the signal properties and the trigger processing parameters, to remove the constant and timeconsuming need of manual adjustments. Moreover, this should improve, at the same time, the system's reliability, the quality of the recorded data and the rejection of spurious events. In fact, most of the devices of the telescopes could change their properties or could gradually degrade. For instance, due to ageing, the photoelectron conversion efficiencies of the PMTs constantly decrease, each one with a different rate, thereby modifying the electronic chain gain. Periodically they need to be equalized, calculating new standard high voltage settings. A continuous control of the parameters of the telescopes allows one to record optimal data sets, always in very similar conditions, even over long time intervals.
Finally, the new system will be installed on both telescopes, enabling stereo observation in Sum-Trigger mode. This will allow the detection of faint events and to take advantage of the stereo image reconstruction. For instance, the fluctuation in the extrapolation of the height of the shower maximum affects heavily the energy resolution. The light yield varies significantly, especially when the shower axis is close to the telescope, as it often happened with the prototype Sum-Trigger. Figure 7.1 shows, for three different impact parameters, how the amount of light seen by telescopes varies with the height of shower maximum. The light yield is independent of the hight of shower maximum only for impact parameters greater than $\sim 100 \mathrm{~m}$. A precise calculation of the


Figure 7.1: Simulation of the light produced in a shower as a function of the height of maximum Čerenkov emission for different shower core distances: the full circles are for a distance of $40 \div 50 \mathrm{~m}$, the open circles for $90 \div 100 \mathrm{~m}$ and the full squares for $140 \div 150 \mathrm{~m}$. (From [73])
height of the shower maximum could become fundamental for the reconstruction and understanding of gammas at low energies, where the classical Hillas parameters loose their power.

The achievement of these three goals will significantly improve observations in the domain below 50 GeV , by gaining crucial information for the understanding of Pulsar, distant $A G N s$ and GRBs. The importance of this energy range is beyond dispute, as emerged in some recent hot cases. One has been clearly illustrated in the sub-section 5.1.3. The Crab Pulsar has been detected above $25 \mathrm{GeV}^{2}$, with a spectrum trend that follows a power low, confuting the Fermi-LAT assessments and excluding some models. Another important topic is the Crab nebula Inverse Compton peak estimation [136]. The cross-correlation between MAGIC and Fermi-LAT has allowed to perform an unprecedented measurement ${ }^{3}$ (Eq. 7.1), illustrated in figure (7.2).

$$
\begin{equation*}
I C_{\text {peak }}=59 \pm 6 \mathrm{GeV} \tag{7.1}
\end{equation*}
$$

Being the uncertainty dominated by systematic errors ( $\sim 15 \%$ ), more precise measurements will add information about the properties of a Supernova Remnant, such as the shock and the associated magnetic field.


Figure 7.2: The spectral energy distribution (SED) of the Crab Nebula obtained with the MAGIC telescopes, together with the results from previous $\gamma$-ray experiments. The black arrow indicates the systematic uncertainty (14\%) on the energy scale. (From [136])

Lowering the energy threshold is not only driven by the desire to explore a not well known energy domain, but it will provide better experimental overlapping with the $F E R M I / L A T$ satellite measurements. It must be stressed that this kind of overlap is presently unique in the world.
A deeper understanding of the properties of known $A G N s$ and of the $S S C$ model is foreseen. Finally, the low energy threshold will allow the detection of higher redshift sources allowing MAGIC to observe a more distant Universe.

### 7.3 Future perspectives

This new trigger system will not be of benefit only for MAGIC, since it is a topic under study also for the future large size telescopes of $C T A^{4}$ array. Several teams are performing complex simulations to understand which will be the best solution for the future IACT systems. These kinds of preparatory studies are not limited to very low energy capabilities, but they have to take into account other important parameters, such as cost, reliability and the possibility to be upgraded. MAGIC will be the only telescope in the world, which can directly compares such systems, providing precious

[^89]knowledge. In this sense, MAGIC should be considered as a real test-bench of $C T A$, in particular for the large size telescopes located at the centre of the array.

## Sum-mezzanine schematics

In this appendix, the schematics of the Sum-mezzanine are presented.

## A. 1 Sum-mezzanine schematics sheets

These schematics refer to the Sum-mezzanine version 1.1.




## B

## CTB-FCl schematics

In this appendix, the schematics of the $C T B-F C I$ are presented.

## B. 1 CTB-FCI schematics sheets

These schematics refer to the $C T B-F C I$ version 1.7. The transmitter stage has not

been modified during the test phase, whereas some passive components in the receiver amplifier have been changed. The two series inductances and the $R C$ filter have been
removed and the value of the input resistors have been reduce in order to increase the bandwidth.


## Sum-board schematics

In this appendix, the schematics of the Sum-board are presented.

## C. 1 Sum-board schematics sheets

These schematics refer to the Sum-board version 1.4.





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Sum-test-board schematics

In this appendix, the schematics of the Sum-test-board are presented.

## D. 1 Sum-test-board schematics sheets

These schematics refer to the Sum-test-board version 2.0.




## MiniPulsar test-bench firmware

In this appendix, the original $V H D L$ code of the MiniPulsar is reported.

## E. 1 The MiniPulsar test-bench code

This is the VHDL code uploaded in the MiniPulsar prototype board in order to check all the functionalities.

```
library ieee;
use ieee.std_logic_1164.all;
use ieee.std logic arith.all;
library altera;
use altera.altera_syn_attributes.all;
entity Testbench MiniPulsar is
generic(Frequenc}\mp@subsup{\overline{y}}{_}{\prime}\mathrm{ scale : integer := 40); -- 40 means 1MHz (1 microsecond)
port(
--INPUTS-
\begin{tabular}{lll} 
MAIN_CLK: & in std_logic; & -- Main clock \\
SDO FPGA: & in std_logic; & \\
SYSCLK: & in std_logic; & -- Clock from VME controller \\
ASN: & in std_logic; & -- VME address strobe
\end{tabular}
MSN: In sid_logic; 
WRN: in std_logic; 
AM: in std_logic_vector(5 downto 0); -- Address modifier
GA: in std_logic_vector(7 downto 0); -- Geographical address
A: in std_logic_vector(31 downto 1); -- VME address
L1IN: in std_logic_vector(33 downto 0); -- Inputs on connector HONDA RPS-8OLM
SVT_OUT_HOLD: in std_logic; -- Command stop read FiFo
DSN: - in std_logic_vector(1 downto 0); -- VME data strobe
SVT_IND: in std_logic_vector(22 downto 0); -- Input from FiFo (From connector KEL-8831)
SVT_STATUS: in std_logic_vector(4 downto 0); -- 0 = FiFo1 full;
                                    -- 1 => FiFo1 almost full;
                                    -- 1 =>FiFo1 almost
                                    -- 2 => FiFo1 empty;
                                    -- 4 => Status SVT_DS (WCLK)
RESET : in std_logic; -- Reset button
\begin{tabular}{|c|c|}
\hline --OUTPUTS-- & \\
\hline LCLK: & out std_logic; \\
\hline LCTRLN: & out std_logic; \\
\hline LDERRN: & out std \({ }^{-}\)logic; \\
\hline LDOWN_AN: & out std \({ }^{-}\)logic; \\
\hline LED_ERR: & out std \({ }_{-}^{-1 o g i c}\); \\
\hline LED_RUN: & out std_logic; \\
\hline LED_SEL: & out std_logic; \\
\hline LWENN: & out std_logic; \\
\hline SRAM_ADSCN: & out std_logic; \\
\hline SRAM-ADSPN: & out std_logic; \\
\hline SRAM-ADVN: & out std_logic; \\
\hline SRAM_CE1n: & out std _ logic; \\
\hline SRAM-CE2 : & out std _logic; \\
\hline SRAM_CE3n: & out std _logic; \\
\hline SRAM_CLK: & buffer std_logic; \\
\hline
\end{tabular}
```

-- Hola mezzanine clock
-- Move to input
-- Move to input
-- Bottom red led
-- Bottom green led
-- Bottom yellow led
-- SRAM address strobe from controller
-- SRAM addres strobe from processor
-- Increment address in SRAM burst cycle
-- SRAM chip enable 1
-- SRAM chip enable 1
-- SRAM chip enable 2
-- SRAM chip

begin
Led_scale $<=$ (Frequency_scale *2000000); -- 2000000 means 2 sec
Output_freq: process (MAIN_CLK)
begin
if MAIN_CLK' event and MAIN_CLK $=$ ' 1 ' then
if ( (Scale_counter < Frequency_scale) and (Scale_counter< (Frequency_scale/2))) then - First half duty cycle (50\%) Frequēncy $\quad$-- Increase counter
elsif ((Scale_counter $<$ Frequency_scale) and (Scale_counter $>=$ (Frequency_scale/2))) then Scale counter $<=$ Scale counter $+1 ; \quad$ - Increase counter $\begin{array}{ll}\text { Scale_counter }<=\text { Scale_counter }+1 ; & -- \text { Increase coun } \\ \text { Frequency_out }<=, 1, ; & -- \text { Output @ }, 1,\end{array}$
else - -- Scale counter@end of cycle Frequency_out $<={ }^{\prime} 0^{\prime} ; \quad--$ Output @ ${ }^{\prime} O^{\prime}$ Scale_counter $<=0 ; \quad--$ Reset counter
end if;
end if; $\quad$ process Output_freq;

Output_LEDs: process (MAIN_CLK)
begin
if MAIN CLK' event and MAIN CLK $={ }^{\prime} 1$, then
if $\left(\left(\overline{\text { Led }}\right.\right.$, time $<$ Led_scale $\left.^{\prime}\right)$ and (Led_time $<($ Led_scale/2))) then $-\quad$ First half duty cycle ( $50 \%$ )
if Led time $=$ (Led_scale/4) then -- Blink each 1 sec
LED_S̄L $<=$ ' 1 '; - -1 means ON

```
        --LED(2) <= '1';-- Uncomment if you want to check the upper LEDs &G comment in FiFo
                status
        else
        LED_SEL<= 'O';
        LED_SEL<= 'O';
            status
        end if;
        Led_time <= Led_time + 1; -- Increase LEDs counter
        Led_out <= , ,0';
        LED_ERR <= '0';
    --L\overline{E}D(3)<='O';-- Uncomment if you want to check the upper LEDs & comment in FiFo status
    elsif ((Led_time<< Led_scale) and (Led_time >= (Led_scale/2))) then-- Second half duty
        cycle
            if Led_time = 3*(Led_scale/4) then
        LED_\overline{SEL <= '1'; - -- LED_SEL ON}
        -L\overline{ED}D(2) <= '1';-- Uncomment if you want to check the upper LEDs &G comment in FiFo
    else
        Lse ( SEL <= '0'; -- LED SEL OFF
        - L\overline{ED}D(2)<='O';-- Uncomment if you want to check the upper LEDs-& comment in FiFo
            status
        end if;
    Led time <= Led time + 1
    Led_time <= Led
    LED_ERR <= '0';;
    -L\overline{ED(3)<='O';-- Uncomment if you want to check the upper LEDs &G comment in FiFo status}
    else
    Led_out <= ,0';
    Led_time <= 0;
```



```
        -sec)
    _-LED(3)<='1';-- Uncomment if you want to check the upper LEDs & comment in FiFo status
    end if;
end if;
end process Output_LEDs;
```

-- FiFos commands--
FiFo_status: process (SVT_STATUS)
begin
case SVT STATUS(0) is
case SVT STATUS(0) is
when $, \frac{1}{0}, \Rightarrow \operatorname{LED}(1)<={ }^{\prime}, ; \quad--$ FiFor full (Red led ON)
when ${ }^{\prime} \overline{0}, \Rightarrow \operatorname{LED}(1)<={ }^{\prime} 1^{\prime} ;{ }^{\prime},{ }^{\prime}$,
when others $\Rightarrow \operatorname{LED}(1)<={ }^{\prime}$,
when oth
end case;
case SVT_STATUS(1) is
when $, \overline{0}, \underset{\operatorname{LED}(2)}{\rightarrow}={ }^{\prime}$, ; $\quad-$ FiFo1 almost full (Yellow led)
when others $\Rightarrow \operatorname{LED}(2)<={ }^{\prime}{ }^{\prime} ;{ }^{\prime},{ }^{\prime}$;
end case;
if (SVT_STATUS(2) or SVT_STATUS(3)) $={ }^{\prime} 0$ ' then $\quad--$ FiFos empty (Green led ON)
LED (3) $<={ }^{\prime} 1^{\prime}$;
elsif (SVT_STATUS(2) xor SVT_STATUS(3)) $='^{\prime} 1$, then -- FiFo1 or FiFoz empty (Green led
blink)
LED (3) $<=$ Led_out;
else
$\operatorname{LED}(3)<={ }^{\prime}{ }^{\prime}$ ';
end if;
end process FiFo_status;
-- FiFos controls --
FiFo_controls: process (RESET, Frequency_out, SVT_STATUS(4), SVT_OUT_HOLD)
begin ${ }^{-}$
if RESET $={ }^{\prime}{ }_{0}$ ' then, $\quad-\quad$ Reset activated
$\begin{array}{ll}\text { f RESET }=\text { then } & \\ \text { SVT_CTRL }(0)<=, 1, ; & -- \text { Reset activated } \\ \text { SVT }\end{array}$
SVT_CTRL $(1)<=,{ }_{0}, ; \quad-\quad-\quad$ FiFo read deactivated
SVT_CTRL(2) <= , 0, '; $\quad--$ FiFo reset \& write deactivated
SVT ${ }^{-}$CTRL (3) $<={ }^{\prime} 0^{\prime} ; \quad-\quad$ FiFo write check deactivated
elsif SVT_OUT_HOLD $={ }_{1}{ }^{\prime}, 0$ then $\quad$-- FiFo read deactivated
SVT $\operatorname{CTRL}(1)<=, \stackrel{1}{0} ; \quad--$ FiFo read clock deactivated
$\begin{array}{ll}\text { SVT_CTRL } \\ \text { SVT } & \text { CTRL }\end{array}$ (2) $<=, 1, ; \quad--F i F o$ read clock deac
SVT_CTRL (3) <= SVT_STATUS(4); $\quad--$ FiFo write activated $\quad-\quad$ FiFo write check activated for desy chain
else $\quad{ }^{\text {SVT }} \operatorname{CTRL}(0)<={ }_{0}{ }^{\prime}$; $\quad$-- FiFo read activated
$\begin{array}{ll}\text { SVT_CTRL (0) } & <=\text { '0'; } \\ \text { SVT_CTRL (1) } & <=\text { Frequency_out; }\end{array} \quad--$ FiFo read activated ${ }^{\prime} \quad--$ FiFo read clock@ "Frequency out"
SVT CTRL (2) $<=$ ' 1 '; -
-- FiFo read clock @"F
SVT_CTRL ( 3 ) $<=$ SVT_STATUS ( 4 );
-- FiFo write activated
$\operatorname{SVT}^{-} \mathrm{CTRL}(3)<=$ SVT_STA
end $\mathbf{i} \overline{\mathbf{f}} ;$
end process FiFo_controls;
-- SRAM commands--
SRAM_CLK<= MAIN_CLK;
LD $<\equiv$ SRAM_DQ_in;
URL $<=$ SRAM_D $\bar{D}_{-}$in;

```
    if SRAM CLK' event and SRAM CLK = '0' then
    if RE\overline{SET = ,'0' then -}
        State_pres <= RESET_SRAM;
        SRAM counter <= 0;
        SRAM_\overline{WR_RD_count <= 0;}
    else
        State_pres <= State_fut;
    end if;
    if (SRAM_counter > SRAM_scale) then
        SRAM_counter <= 0;
            if (S\overline{RAM_WR_RD_count > SRAM_W_R_scale) then}
            SRAM_\overline{WR_RD}_count <= 0;
            else
                SRAM_WR_RD_count <= SRAM_WR_RD_count + 1; -- Increase SRAM data counter
            end if;
    else
        SRAM_counter <= SRAM_counter + 1; -- Increase SRAM cycle counter
    end if;
end if;
end process SRAM_FSM_clk;
SRAM_FSM: process (State_pres, SRAM_counter, SRAM_OEN) -- SRAM State machine function
begin
    case State pres is
        when RES\overline{ET}}\textrm{SRAM}=> -- State o => RESE
            State fu\overline{t}<= WAIT_SRAM;
            SRAM_\overline{DP}<=(\mathrm{ others }}=>\prime\prime,0')
        when WAIT_SRAM => -- State 1 => WAIT
            if (SRAM counter /= 1) and ((SRAM_counter /= 6)) then
                State fūt <= WAIT_SRAM;
            elsif (STRAM_counter = = 6) then
                State_fut<= PRE0_READ_SRAM;
            else
                State_fut<= PRE0_WRITE_SRAM;
            when PREO_WRITE_SRAM => -- Load address into registers for writing
            State \overline{fut <= \overline{PRE1_WRITE_SRAM ;}}\mathbf{}\mathrm{ - ST}
            when PR\overline{E}1_WRITE SRA\overline{M}}\underset{\mathrm{ State fut < = WRITE SRAM;}}{=>
                -- Load address into memory for writing
            State \overline{fut < = W}WRITE_SRAM;
            when WRITE_SRAM => _
            State fu\overline{t}<= WAIT_SRAM;
            when PRE\overline{0}RREAD_SRAM }=
            State \overline{fut < =- PRE1_READ_SRAM;}
    when PR\overline{E}1_READ_SRAM
            State fut <= READ_SRAM;
    when RE\overline{AD}_SRAM => - _
    when others =>
            State_fut<= RESET_SRAM;
end case;
    if Bidirectional function
    if SRAM OEN = ' }1\mathrm{ ,' then
        SRAM_\overline{DQ}(31 downto 0) <= SRAM_DQ_out(31 downto 0); -- SRAM data 0-31
        SRAM_DP <= conv_std_logic_vector(SRAM_WR_RD_count, 4); -- SRAM data 32-36
        SRAM_DQ_in <= (others => 'Z',);
        SRAM_DP-in <= (others => 'Z',);
    else
    SRAM_DQ_in (31 downto 0) <= SRAM_DQ (31 downto 0); -- Map SRAM_DQ into LD
            SRAM_DQ_in (31 downto 0) <= SRAM_DQ (31 downto 0); -- Map SRAM_DQ into LD 
            SRAM_DQ < = (others }\mp@subsup{}{}{-}=>,\mp@subsup{Z}{}{\prime},\mathrm{ ,);
    SRAM-DP <= (others = ' , Z,
end if;
end process SRAM_FSM;
with State_pres select
    SRAM_BW <= B" 1111" when RESET_SRAM,
    B"11\overline{111" when WAIT_SRAM,}
    B"1111" when PREO_WRITE_SRAM,
    B" 1111" when PRE1_WRITE_SRAM,
    B"0000" when WRITE_SRAM,
    B"1111" when PRE0__READ_SRAM,
    B"1111" when PRE1_READ_SRAM,
    B"1111" when READ_SRAM,
    B"1111" when others;
with State pres select
    SRAM_BWEN}<=,1, when RESET_SRAM
    ',1, wwen WAIT_SRAM,
    '1', when PREO_WRITE_SRAM,
    , 1, when PRE1_WRITE_SRAM,
    , 0, when WRITE__SRAM,
        , when PRE0_\overline{READ_SRAM,}
        when PRE0_\overline{READ SRAM,}
        when PRE1- READ-
        when READ_SRAM\overline{M}
    '1' when others;
with State_pres select
    SRAM_GWN <= '1, when RESET_SRAM,
    ',1, wwen WAIT_SRAM,
    , 1, when PREO_WRITE_SRAM,
    '1
        , when WRITE _SRAM,
            when PREO_\overline{READ_SRAM,}
            when PRE1__READ_SRAM,
            when READ_SRAM}\overline{M}
    '1' when othe\overline{r}
with State_pres select
```

```
    SRAM CE1n <= '1, when RESET SRAM,
    '1', when WAIT SRAM,
    '0' when PRE0_WRITE SRAM,
    when PRE0_WRITE_SRAM,
    when PRE1_WRITE SR
    when WRITE_/_SRAM,
    when PRE0_READ_SRAM,
    when READ__SRAM}\overline{\mathrm{ ,}
    '1', when otherrs;
SRAM_CE2 <= '1';
SRAM -CE3n <= ,0',
with State_pres select
    SRAM_OEN <= '1' when RESET_SRAM,
        1, wwhen WAIT_SRAM,
        , when PRE0_WRITE_SRAM,
        when PREIT\overline{L SRINE,}
        , when PRE0_\overline{READ_SRAM,}
    , 1', when PRE1-READ-SRAM,
    ,0', when READ_S_SRAM,
    MAM when othe\overline{r}s;
with_State pres select
    SRAM_ADSPNN <= '1, when RESET_SRAM,
        '1', w
        when PREO_-WRITE_SRAM,
        when PRE1-}\mp@subsup{}{}{-}\mathrm{ WRITE-
            when WRITE
            when PRE0_\overline{READ_SRAM,}
            when PRE1-READ_SRAM,
            '1', when READ_SRAM-
            '1', when others;
with State pres select
    SRAM_ADSCN <= '1', when RESET_SRAM,
        '1', when WAIT_SRAM,
            when PREO_WRITE_SRAM,
            when PRE1_-WRITE_SRAM,
            when WRITE SRAM,
            when PREO \overline{READ SRAM,}
            , when PRE1__READ_SRAM,
            '1', when READ_SRAM,
            , 1, when READ_SR
with State pres select
    With State_pres select 
    SRAM_ADD\overline{R}<== (年hers => '0') wh
    (others => '0') when WAIT_SRAM,
    conv_std_logic_vector(SRAM_WR_RD_count,SRAM_ADDR'length) when PRE0_WRITE_SRAM,
    (others => '0') when WRITE_SRAM,
    conv_std_logic_vector(SRAM_WR_RD_count,SRAM_ADDR'length) when PREO_READ_SRAM,
    conv_std_logic_vector(SRAM_WR_RD_count,SRAM__ADDR'length) when PRE1_READ_SRAM,
    (others => ,0') when READ_\overline{SRAM,}
    (others => '0') when others;
with State_pres select
    SRAM_DQ_out(18 downto 0) <= (others => '0') when RESET_SRAM,
    (others }\overline{=>},0') when WAIT_SRAM
    (others => '0') when PREO_WRITE SRAM,
    (others => '0') when PRE1- WRITE ' SRAM,
    conv_std_logic_vector(SRAM__WR__RD_count, 19) when WRITE_SRAM,
    (others => ,0,) when PRE0_READ_SRAMM,
    (others => ,0,) when PREO_READ_SRAM,
    (others => '0') when PRE1_READ_SR
    (others => '0') when READ_SRA
with State pres select
    SRAM_DQ_out(31 downto 19)<= (others => '0') when RESET_SRAM,
    (others #}\Longrightarrow,0,) when WAIT_SRAM,
    (others => '0,') when PREO-WRITE SRAM,
    (others }=>,0,') when PRE1_WRITE-SRAM,
    conv std_logic vector(SRAMM WR _RD_count, 13) when WRITE_SRAM,
    (others => ,0,) when PREO_READ -SRAMM,
    (others => ,0') when PRE1__READ_SRAM,
    (others => ,0,') when READ__SRAM,
    (others => '0') when others;
-- General I/O--
LED_RUN <= Led_out;
LCL\overline{K}<= Frequency_out; -- Map GA(O) into LCTRLN
LCTRLN <= GA(0); 
```



```
LDOWN_AN <= GA(2); 
LWENN <= GA(3); ;
UDW0_A <= GA(4); 
UDW1_A <= GA(5); 
```



```
UXOFFN <= ASN; 
DTACKn <= Frequency_out;
DATA_EN <= '1,',when RESET = '0' else '0'; -- Enable the VME tranceivers (Active low)
DIR_\overline{DATA <= '0', when DATA_EN = '0' else ', Z'; -- Enable VME tranceiver direction ('O' from}
    FPGA to VME)
```

```
SVT_OUT <= SVT_IND; 
L1O\overline{UT}(3\overline{3}\mathrm{ downto 0) <= L1IN(33 downto 32) & -- Map Frequency out in -- Map the L1IN into LIOUT}
    Frequency_out & - -- Map L1IN31 for WCLK of FiF
```



```
F1CTRL(5 downto 0)<= AM(5 downto 0); ; -- Map F1CTRL[32..28] into AM[5..0]
F1CTRL(32 downto 6) <= (others }=>>\mathrm{ Frequency_out);
CARD1_ID <= (others }=>>\mathrm{ Frequency_out);
F2IO <= (others }=>>\mathrm{ Frequency_out);
F2CTRL <= (others => Frequency_out);
CARD2 ID <= (others => Frequency out)
D(31 downto 0)<= A(31 downto 1) & SYSCLK; -- Map VME address into VME data + Sysclk
end Bhv;
```


## F

## MiniPulsar schematics

In this appendix, the schematics of the MiniPulsar are presented.

## F. 1 MiniPulsar schematics sheets

These schematics refer to the MiniPulsar version 2.1.










Tesi di dottorato di Francesco Dazzi, discussa presso l'Università degli Studi di Udine

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## Useful units

The basic units used in this thesis are listed and briefly explained in this section.
A : ampere, unit of current. By definition, $1 \mathrm{~mA}=10^{-3} \mathrm{~A}$.
a.u. : arbitrary units.
b : bit.
B : byte. By definition, 1 byte $=8$ bit.
Crab nebula unit is an integral flux unit. It is the fraction of Crab nebula flux above a certain energy threshold, which corresponds to the measured or reported flux.
dB : decibel.
erg unit of energy, used in astronomy. $1 \mathrm{erg}=10^{-7} \mathrm{~J}$.
$\mathbf{e V}$ means electronvolt. It is a unit of energy often used in particle and astroparticle physics. It is equal to approximately $1.602 \times 10^{19} \mathrm{~J}$. By definition, $1 \mathrm{keV}=10^{3} \mathrm{eV}$, $1 \mathrm{MeV}=10^{6} \mathrm{eV}, 1 \mathrm{GeV}=10^{9} \mathrm{eV}, 1 \mathrm{TeV}=10^{12} \mathrm{eV}$, and $1 \mathrm{PeV}=10^{15} \mathrm{eV}$.

Gbps giga bits per second.
gr : gram, unit of weight. By definition, $1 \mathrm{~kg}=1000 \mathrm{gr}$.
Gsample/s : giga sample per second.
h : hour.
$\mathbf{H z}$ : hertz, unit of frequency. By definition, $1 \mathrm{kHz}=10^{3} \mathrm{~Hz}, 1 \mathrm{MHz}=10^{6} \mathrm{~Hz}$ and $1 \mathrm{GHz}=10^{9} \mathrm{~Hz}$.

KiB : kibibyte. By definition, $1 \mathrm{KiB}=2^{10}$ byte $=1024$ byte .
Kib : kibibit. By definition, $1 \mathrm{Kib}=2^{10}$ bit $=1024$ bit.
light year is a unit of length. Corresponds to $9,461 \times 10^{15} \mathrm{~m}$.
$\mathbf{m}$ : metre, unit of space. By definition, $1 \mathrm{~km}=1000 \mathrm{~m}, 1 \mathrm{~cm}=10^{-2} \mathrm{~m}, 1 \mathrm{~mm}=$ $10^{-3} \mathrm{~m}, 1 \mu \mathrm{~m}=10^{-6} \mathrm{~m}$ and $1 \mathrm{~nm}=10^{-9} \mathrm{~m}$.
$\mathbf{M}_{\odot}$ is the mass of the Sun.
Mbps mega bits per second.
MJD stands for Modified Julian Date. Is a time unit corresponding to the number of days elapsed since midnight of November 17, 1858.
parsec is a length unit, corresponding to $30.857 \times 10^{15} \mathrm{~m}$.
pc : parsec.
pF : picoFarad.
phe stands for number of photo-electrons and is a unit that characterizes the images size collected by a $I A C T$. It represents the sum of the calibrated charge of a triggered event collected by each $P M T$ of the telescope camera.
redshift $(z)$ is the ratio decreased by a unit between the radiation wavelength emitted by an object in Doppler motion with respect to an observer, $\lambda_{\text {em }}$, and that observed, $\lambda_{o b}: 1+z=\frac{\lambda_{o b}}{\lambda_{e m}}$. In astronomy it is used as a distance or time unit.
$\mathrm{s}:$ second, unit of time. By definition, $1 \mathrm{~ms}=10^{-3} \mathrm{~s}, 1 \mu \mathrm{~s}=10^{-6} \mathrm{~s}, 1 \mathrm{~ns}=10^{-9} \mathrm{~s}$ and $1 \mathrm{ps}=10^{-12} \mathrm{~s}$.
sr : steradian.
$\mathbf{U}$ In electronics, U means dimensional unit. When the subject is the $P C B$ height, the minimum dimension is 3 U , which corresponds to 100 mm . Then each increment is made by 44.45 mm steps. A 6 U board is height 233.35 mm , while 9 U are 366.79 mm . When the subject is a mechanical rack, the single unit is always $44,45 \mathrm{~mm}$, so 3 U are 133.35 mm . The starting different is introduced to allows the insertion of the boards.
$\mathbf{V}$ : volt, unit of voltage. By definition, $1 \mathrm{mV}=10^{-3} \mathrm{~V}$ and $1 \mu \mathrm{~V}=10^{-6} \mathrm{~V}$.
$\mathbf{W}$ : watt, unit of power. By definition, $1 \mathrm{~kW}=10^{3} \mathrm{~W}$.
yr : year.
$\Omega$ : ohm, unit of resistance.

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[^0]:    ${ }^{1}$ Max Planck Institute for Physics in Munich, Germany.

[^1]:    ${ }^{1}$ Astronomy is a natural science that deals with the study of celestial objects. It is divided into two main branches, distinguished as astrometry and astrophysics.

[^2]:    ${ }^{2}$ A circumpolar star is a star that, as viewed from a given latitude on Earth, never sets (that is, never disappears below the horizon), due to its proximity to one of the celestial poles. Circumpolar stars are therefore visible for the entire night on every night of the year.
    ${ }^{3}$ The Big Dipper is an asterism of seven stars, which are the seven brightest of the formal constellation Ursa Major.

[^3]:    ${ }^{4}$ It is the apparent path of the Sun, or the real path of the Earth as seen from the Sun.
    ${ }^{5}$ Astrolatry is the worship of stars and other heavenly bodies as deities, or the association of deities with heavenly bodies.

[^4]:    ${ }^{6}$ Circle in which a planet moves and which has a centre that is itself carried around at the same time on the circumference of a larger circle.

[^5]:    ${ }^{7}$ Copernicus' major theory was published in De revolutionibus orbium coelestium, in the year of his death, though he had formulated the theory several decades earlier.
    ${ }^{8}$ This principle asserts that the natural motion of a celestial body is around a circle, and the motion must be uniform when viewed from the centre of that same circle.
    ${ }^{9}$ The plane of the Moon's orbit is inclined with respect to the ecliptic. This angle varies due to the complexity of the Moon's orbit, but the average inclination is $5^{\circ}$. The intersection of these two orbital planes form an axis, or line, and the points of intersection are called the Moon's nodes.
    ${ }^{10}$ Galileo Galilei did not invent the telescope, but was the first to use it systematically to observe celestial objects and record his discoveries. The first telescope was created by Hans Lippershey in 1608, one year before.

[^6]:    ${ }^{11}$ It consists to estimate the apparent changes of position between stars, when seen from different points of view.
    ${ }^{12}$ A spectrograph is an instrument which separates an incoming wave into a frequency spectrum.
    ${ }^{13}$ The Draper's work was followed through by Annie Jump Cannon. A new catalogue containing 225300 stars was published between 1918 and 1924.

[^7]:    ${ }^{14}$ Nuclear fusion can be either exothermic or endothermic, but here we're simply talking about exothermic kind, when stars release immense quantities of energy. The endothermic nuclear fusion is the mechanism by which all the elements heavier than iron are created in a supernova.

[^8]:    ${ }^{15}$ Schwarzschild radius is defined as: $R_{s}=2 G M / c^{2}$, where $G$ is the gravitational constant, $M$ is the mass of the central body, and $c$ is the speed of light in a vacuum.
    ${ }^{16}$ The Hubble's law is defined as: $z=H_{0} D / c$, where $z$ is the redshift of the galaxy, $D$ the distance, $c$ the light speed and $H_{0}$ the Hubble's constant, whose value is $74 \mathrm{~km} / \mathrm{s}$ per mega parsec.

[^9]:    ${ }^{17}$ The name Big Bang was invented by Hoyle in 1950.

[^10]:    ${ }^{18}$ Magnetohydrodynamics is the discipline which studies the dynamics of electrically conducting fluids.
    ${ }^{19}$ Cosmic rays are energetic particles, originating from outer space.
    ${ }^{20}$ Physical cosmology is the study of the largest-scale structures and dynamics of the Universe.
    ${ }^{21}$ Cosmic microwave background is thermal radiation filling the observable Universe almost isotropically. It is the remnant heat left over from the Big Bang.

[^11]:    ${ }^{22}$ A sounding rocket is an instrument-carrying rocket designed to take measurements and perform scientific experiments during its sub-orbital flight.

[^12]:    ${ }^{23}$ The Standard Model is the name given to the current theory of fundamental particles and how they interact. It is a theory concerning the electromagnetic, weak, and strong nuclear interactions, which mediate the dynamics of the known subatomic particles.

[^13]:    ${ }^{24} \mathrm{An}$ electroscope consists of two leaves of gold foil suspended from an insulated electrode in a metal box with glass window. When the electrode collects an electric charge, the leaves spring apart due to the electric repulsion.

[^14]:    ${ }^{25}$ The ionization chamber is a gas-filled radiation detectors, and is used for the measurement of ionizing radiation.

[^15]:    ${ }^{26}$ The Dirac equation is a relativistic quantum mechanical wave equation that provides a description of elementary spin- $1 / 2$ particles, such as electrons.
    ${ }^{27}$ A Geiger counter is a particle detector that measures ionizing radiation produced in a low-pressure gas tube. Each particle revealed produces a pulse of current, where the energy is not distinguished.
    ${ }^{28}$ The photographic emulsion is based on silver-gelatin process, consisted of silver halide crystals suspended in gelatin, and the substrate of glass, plastic film or paper.

[^16]:    ${ }^{29}$ The longitude dependence is a consequence of the misalignment between the geomagnetic dipole axis and the Earth's rotation axis.
    ${ }^{30}$ The GZK (from inventors Greisen - Zatsepin - Kuzmin) is a theoretical upper limit on the energy of cosmic rays from distant sources.

[^17]:    ${ }^{31}$ Charged particles gain energy travelling through the shock wave front, produced by a star explosion. The particles undergo multiple reflections, due to moving variable magnetic field, between the upstream and the downstream zone. In every reflection they increase the velocity.

[^18]:    ${ }^{32}$ The Pierre AUGER Observatory is an international cosmic ray observatory designed to detect ultra-high-energy cosmic rays.

[^19]:    ${ }^{33} \mathrm{An} A G N$ (Active Galactic Nucleus) is a compact region at the centre of a galaxy.
    ${ }^{34}$ The program was run by the Department of Defence to keep watching clandestine nuclear tests. During a scan, Vela satellites detected for the first time a $\gamma$-ray burst

[^20]:    ${ }^{35}$ Blazar is a member of the wide group of $A G N s$

[^21]:    ${ }^{36}$ Before Whipple, there were some precursors, which followed the Stuart Blackett's intuition about the Čerenkov light production in air [16]. The first discovery was made in 1953 by J. V. Jelley and W. Galbraith [79]. Then, some rudimentary prototype detectors were build in Crimea (1959-65), in Ireland (1962-66) and Massachusetts (1965-66) [134].
    ${ }^{37}$ Imaging Atmospheric Čerenkov Technique is a technique utilized by the telescopes that collect and analyse the Cerenkov light produced by extended air shower initiated by a cosmic ray. Usually they are sensitive to the blue light $(300 \div 400 \mathrm{~nm})$ and apply imaging algorithms.

[^22]:    ${ }^{38}$ The primary interaction of photons in the LAT energy range with matter is pair conversion.
    ${ }^{39}$ The total satellite mass is equal to 350 kg . For comparison the $L A T$ 's weight is 2789 kg .

[^23]:    ${ }^{40}$ Bremsstrahlung radiation becomes noticeable when the energy of the particle is very high compared to its self-energy. This constraint favours mainly electrons.

[^24]:    ${ }^{41}$ The $A R G O-Y B J$ experiment has reported an enhanced TeV emission in September 2010, but this claim was not supported by the simultaneous observations of MAGIC and VERITAS.

[^25]:    ${ }^{42}$ The synchro-curvature mechanism unifies the ordinary synchrotron and curvature radiation. In fact, synchrotron radiation is independent of the curvature radius of magnetic field, while curvature one is caused by particles moving along the curved field lines.

[^26]:    ${ }^{43}$ The Roche lobe is the spatial region around a star, within which orbiting material is gravitationally bound to that star.

[^27]:    ${ }^{1}$ The electromagnetic showers can be also originated by $\mathrm{e}^{ \pm}$.
    ${ }^{2}$ The photon $\mathrm{E}_{c}$ is $\approx 5 \mathrm{MeV}$, when the Compton radiation dominates over pair creation.
    ${ }^{3}$ It can be defined as the material thickness, which reduces the mean energy of a radiation by a factor e.
    ${ }^{4}$ It is measured in terms of atmospheric depth, that is how much atmosphere the shower can pass through.

[^28]:    ${ }^{5}$ The name is due to the Russian discoverer P. A. Čerenkov, who recorded the radiation for the first time in the 1934.
    ${ }^{6}$ At the altitude of 10 km , close to the shower maximum development, this limit is double because n diminishes.

[^29]:    ${ }^{7} 10 \mathrm{~ns}$ is a conservative value. The contribution after 6 ns could be considered negligible.

[^30]:    ${ }^{8}$ The oxygen and the nitrogen constitute the $99 \%$ of the atmosphere.

[^31]:    ${ }^{9}$ Space-time is usually interpreted with space as being three-dimensional and time playing the role of a fourth dimension.

[^32]:    ${ }^{10}$ It is the method utilized to distinguish gamma from hadronic events, analysing the shower images.
    ${ }^{11} n$ is the number of pixels that must be considered. For instance conc3 checks the 3 brightest channels.

[^33]:    ${ }^{12}$ It is a multi-dimensional classification system structured on decisional trees. It runs in a dedicated program.

[^34]:    ${ }^{13}$ The pedestal is an estimation of electronic noise in the electronic chain.
    ${ }^{14}$ The time slice is related to the readout sampling speed. Here it corresponds to 0.5 ns .
    ${ }^{15}$ The interleaved calibration events have not not to be confused with calibration runs. During data runs, in which the telescope is triggered by cosmic events, some calibration pulses are included to update the calibration factors.

[^35]:    ${ }^{16}$ Afterpulses are spurious signals that appear after the main pulse of a $P M T$.

[^36]:    ${ }^{17}$ This method has been introduced with the stereo analysis. Before the energy was measured using the random forest algorithm, trained with events of known energy.
    ${ }^{18}$ The electrons contribution is not treated in this simplified description.

[^37]:    ${ }^{19}$ It is a data sample recorded tracking a dark region of the sky close to the source.

[^38]:    ${ }^{20} \mathrm{~A}$ darkpatch is a region of the sky where there are not bright sources.
    ${ }^{21}$ The sand from the Sahara desert.

[^39]:    ${ }^{1}$ It is an extension of the Standard Model, in which a special symmetry puts in correspondence fermions and bosons.
    ${ }^{2}$ Stable means even with a lifetime greater than the age of the Universe.

[^40]:    ${ }^{3}$ Relatively to the development of a more energetic shower.
    ${ }^{4}$ For technical detail on these configurations read section 4.6.

[^41]:    ${ }^{5}$ The combination of atmosphere and telescope forms a sort of calorimeter.

[^42]:    ${ }^{6}$ This is also the number of stages in the Heitler model, namely the number of interaction along each path starting from the primary interaction.
    ${ }^{7}$ Above $\sim 150 \mathrm{MeV}$ the Čerenkov emission due to an electron is in saturation.

[^43]:    ${ }^{1}$ When not specified, the description of the subsystems deals with both telescopes.

[^44]:    ${ }^{2}$ In front of the telescope, there is a tower in the North direction to avoid focusing the sun light. When the telescope is in parking position, it is possible to access the camera.

[^45]:    ${ }^{3}$ The honeycomb is a light yet structurally rigid product, which has a geometry that follows the hexagonal cells.

[^46]:    ${ }^{4}$ The $R S-485$ is transmission used mainly in digital communications networks. It is a standard defining the electrical characteristics of drivers and receivers for use in balanced digital multi-point systems.

[^47]:    ${ }^{5}$ They are hemispherical borosilicate window and rubidiumbialkali photocathode PMTs.
    ${ }^{6}$ It is dichloromethane $\left(\mathrm{CH}_{2} \mathrm{Cl}_{2}\right)$ mixed with Paraloid B72 and 1.4 P-Terphenyl.

[^48]:    ${ }^{7}$ A Cockcroft-Walton generator is an electric circuit which generates a high DC voltage from a low voltage AC or pulsing DC input.

[^49]:    ${ }^{8}$ For $\mathrm{N}=2$, as for the 2 NN , only two pixels are adjacent.

[^50]:    ${ }^{9}$ The receiver board of $M A G I C-I$ has been designed by the MPI group.
    ${ }^{10}$ The ECL (Emitter-Coupled Logic) is a logic family that achieves high speed by using an overdriven $B J T$ differential amplifier with single-ended input.
    ${ }^{11}$ The capacitor is variable and its capacitance can be changed using a screw driver.
    ${ }^{12}$ Falling on the boundary of two non-overlapping macrocells, a compact group of activated pixels might not pass the trigger.
    ${ }^{13}$ PLD (Programmable Logic Device) is an electronic device useful to prepare reconfigurable digital circuits.

[^51]:    ${ }^{14}$ The MOSFET (Metal Oxide Semiconductor Field Effect Transistor) is a transistor used for amplifying or switching electronic signals.
    ${ }^{15}$ In the outer ring there are 12 blind pixels, so the effective number is 447 .
    ${ }^{16}$ The Individual Pixel Rate is a system of scalers that count the frequency in each pixel after the threshold of the LTO.

[^52]:    ${ }^{17}$ More details about this board will be presented in chapter 6 .

[^53]:    ${ }^{18}$ It is a laser that uses the quantum well technology, so the efficiency is greater than that of standard laser, because the electrons that contribute to laser action are quantized.
    ${ }^{19}$ The LED models are NISHIA NSPB300 and NSHU590.
    ${ }^{20} C A N$ is a message-based protocol widely used in automotive applications and in industrial automation.

[^54]:    ${ }^{21}$ LabVIEW is a graphical programming environment.

[^55]:    ${ }^{22}$ At the time of writing.
    ${ }^{23}$ Each DRS4 handles up to 8 channels.

[^56]:    ${ }^{1}$ This means that the linear sum of correlated signals is always higher than the sum of uncorrelated Gaussian noise sources, if the $R M S$ noise value does not exceed the signal amplitude.

[^57]:    ${ }^{2}$ In this data-taking mode, the signal and the background are recorded at the same time, moving the pointing direction at two sky positions $0.4^{\circ}$ far from the source, every 20 minutes.

[^58]:    ${ }^{3}$ In the Sum-Trigger software control, dubbed Sumo, the signal calibration was missing.

[^59]:    ${ }^{4}$ The software has been mainly developed by M. Lopez.

[^60]:    ${ }^{5} A D C$ (Analogue to Digital Converter) is a device that converts a continuous voltage to a discrete time digital representation.
    ${ }^{6}$ TDC (Time to Digital Converter) is a device which calculates the arrival time of an incoming pulse, returning its value in a digital form.
    ${ }^{7}$ The reference signal is simply a channel in the trigger area.
    ${ }^{8}$ The SPI (Serial Peripheral Interface) bus is a synchronous serial data link standard named by Motorola that operates in full duplex mode.

[^61]:    ${ }^{9}$ The model is $10054999-$ N0500AULF.
    ${ }^{10}$ The model is $10076181-101 L F$.

[^62]:    ${ }^{11}$ The signal is first amplified by a factor A and then adjusted in amplitude with an attenuator, in the range $[(1 / A)-k] \div[(1 / A)+k]$, where $2 k$ is the maximum attenuation.

[^63]:    ${ }^{12}$ The selected number of sections are determined by the compromise between the space limitation and performance, which are not so different for higher values.
    ${ }^{13} \mathrm{~A}$ varactor diode is a type of diode, which has a variable capacitance that is a function of the voltage impressed on its terminals. It operates in reverse-biased mode, so the capacitance is modulated, changing the thickness of the depletion zone, in function of the applied bias voltage ( $0 \div 30 \mathrm{~V}$ ).

[^64]:    ${ }^{14}$ The -3 dB limit is the value which defines the cut-off frequency. Beyond this point, the transferred power is less than half.
    ${ }^{15}$ From the Monte Carlo simulation, the best value is around $6 \div 7$ phe. To translate it in terms of volts, an absolute calibration is essential to extrapolate the conversion factor.

[^65]:    ${ }^{16}$ Every chip $A D A 4927-2$ contains two transmitter amplifiers ADA4927.
    ${ }^{17}$ In the final project, the Sum-backplane is inserted at this level, in place of the cable. The capacitive load will certainly be different, however, it would be even more problematic to drive a 5 m cable.

[^66]:    ${ }^{18}$ The net is not routed in a straightforward manner searching the minimal path, but a zigzagging method is used to match the longest net.

[^67]:    ${ }^{19}$ There are 60 signal pins and other 30 for ground.

[^68]:    ${ }^{20}$ In electronics, this is defined as the far-end cross-talk.

[^69]:    ${ }^{21}$ The multiline cross-talk is less than $3 \%$ at 100 ps and the insertion loss is less than 1 dB up to 3 GHz

[^70]:    ${ }^{22}$ This number is necessary because of the worsening of the bandwidth for signals greater than 2 V .
    ${ }^{23}$ A stripline is a trace of metal sandwiched between two parallel ground planes. The surrounding insulating material of the substrate forms a dielectric.

[^71]:    ${ }^{24}$ For both inputs of the Sum-board, there is a resistive termination of $50 \Omega$, which lowers the signal by -6 dB . The relative -3 dB cut-off occurs at -9 dB .

[^72]:    ${ }^{25} \mathrm{~A}$ capacitor of 10 pF has been connected between the positive amplifier input and ground.

[^73]:    ${ }^{26}$ It means Analog Sum-Trigger-II prOcessing board.

[^74]:    ${ }^{27}$ The OR operator performs logical disjunction on two boolean expressions. If either expression evaluates to the logic state "HIGH", OR returns "HIGH". If neither expression evaluates to "HIGH", OR returns "LOW".
    ${ }^{28}$ The NB7V52M is a 10 GHz differential D flip-flop. The differential input and the clock incorporate

[^75]:    dual internal $50 \Omega$ termination resistors, accepting $L V D S$ logic levels. The chip is offered in a low profile $3 \times 3 \mathrm{~mm}, 16$ pins $Q F N$ package.
    ${ }^{29}$ It is the generic signal transmitted in a channel belonging to the Sum-Trigger-II.

[^76]:    ${ }^{30} \mathrm{~A}$ daisy chain is a wiring scheme, in which multiple devices are wired together in sequence or in a ring.
    ${ }^{31}$ The $D A C 7568-A$, from Texas Instruments, for the attenuation, while the version $-C$, with a wider range, for the delay lines.

[^77]:    ${ }^{32}$ It is an universal $U S B$ controller with $50 \mathrm{I} / \mathrm{O}$ pins, which contains a high-speed $U S B$ to $S P I$ converter.

[^78]:    ${ }^{1}$ Hereafter, the sub-array, in which the telescopes are configured to be in trigger coincidence, is called stereo-cell.

[^79]:    ${ }^{2}$ The minimum flux that assures a $5 \sigma$ detection $\left(N_{\text {excess }} / \sqrt{N_{b g d}}\right)$ in 50 h of observation.

[^80]:    ${ }^{3} \mathrm{Up}$ to now, the stereoscopic system was composed of two telescopes, and the two additional units had never been considered.

[^81]:    ${ }^{4}$ The position of MAGIC-I is 2186.98 m a.s.l., while for MAGIC-II is 2187.14 m a.s.l.

[^82]:    ${ }^{5}$ The maximum of the equation 6.5 is 85 m , when $\theta=90^{\circ}$ and $\varphi=38^{\circ}$. It corresponds to a delay of 283 ns . The deemed maximum is fixed to 250 ns , because there are no observations for zenith angles higher than $60^{\circ}$ so far.

[^83]:    ${ }^{6} S$-LINK is a data link, designed at $C E R N$.

[^84]:    ${ }^{7}$ The logic element is the smaller programmable entity of $F P G A$. In this device, it is composed of 4 look-up table inputs, a programmable register and a carry chain connection.

[^85]:    ${ }^{8}$ The $V H D L$ code is copied in appendix E .

[^86]:    ${ }^{9}$ Connecting the ground peg with the probe terminal, a coil, which acts as an antenna, is created.
    ${ }^{10}$ A PWM (Pulse Width Modulation) control is a device commonly used to manage the power in the modern electronic power switches.

[^87]:    ${ }^{11}$ This is the version 2.1. The schematics are available in appendix F.

[^88]:    ${ }^{1}$ The final layout is based on the $D R S_{4}$ readout.

[^89]:    ${ }^{2}$ Recently it has been detected up to 400 GeV by VERITAS and MAGIC.
    ${ }^{3}$ The peak is estimated by fitting the data set with a power law function.
    ${ }^{4} C T A$ (Čerenkov Telescopes Array) is an array of IACT telescopes with three different mirror sizes.

