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(Article begins on next page)

Between quantum and classical gravity: Is there a mesoscopic spacetime?

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Abstract

Between the microscopic domain ruled by quantum gravity, and the macroscopic scales described by general relativity, there might be an intermediate, "mesoscopic" regime, where spacetime can still be approximately treated as a differentiable pseudo-Riemannian manifold, with small corrections of quantum gravitational origin. We argue that, unless one accepts to give up the relativity principle, either such a regime does not exist at all — hence the quantum-to-classical transition is sharp —, or the only mesoscopic, tiny corrections conceivable are on the behaviour of physical fields, rather than on the geometric structures.

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"Spacetime" is a powerful word in physics. It refers simultaneously to some "grand stage", where all phenomena can unfold, but also to a dynamical entity itself, governed by Einstein's equations. Mathematically, it is an umbrella term encompassing both "pre-physical" structures (dimension, topology, differentiable structure etc., usually absorbed into the notion of an appropriate smooth manifold), and objects with a physical interpretation (the metric, the curvature, a temporal orientation, etc.) [1].

Yet, the same word also evokes a theoretical landscape far from being settled. Our present model of spacetime as a pseudo-Riemannian differentiable manifold can be considered satisfactory and efficient from cosmological scales down to particle physics scales (energies of at least 10²⁰ eV, from ultra-high

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energy cosmic rays). However, quantum fluctuations emerging at microscopic level are expected to shatter the classical structure of space and time at small scales (frequently, one refers to the Planck length $\ell_{\rm P} \sim 10^{-33}$ cm). This might imply changes in the physical fields and/or in the "pre-physical" structures, with a strong dependence on the model adopted [2].

In principle, any such microscopic variation of the classical scheme might propagate upwards to a "transition" scale ℓ much larger than the Planck one. It could thus entail mesoscopic modifications of spacetime [3], already within our present experimental window, where much effort is focussed to provide tight constraints [4]. The picture is then the following: below ℓ_P , spacetime (or whatever replaces it) can no longer be modelled after a pseudo-Riemannian differentiable manifold, which provides instead an accurate description at scales larger than ℓ . In the mesoscopic region between ℓ_P and ℓ , such model may still be viable, provided that appropriate (small) corrections be applied to the laws of physics and/or to the geometrical objects. Just to give one example, in the context of Causal Sets theory [3], ℓ is a non-locality scale bridging the gap between the microscopic causal network at the Planck scale, and the macroscopic, smooth spacetime manifold.

It is fair to ask, then, what could be the common features of the corrections expected to emerge in this mesoscopic regime. To begin with, we notice that the scale ℓ is certainly much smaller than any curvature radius associated with macroscopic gravitational fields. At the same time, it is much larger than the Planck length, where quantum gravitational effects become relevant. These are exactly the conditions under which we would expect special relativity to hold. Therefore, any mesoscopic-regime deviation from standard physics induced by the sub-Planckian behaviour of spacetime, either can show up as corrections to the physical laws in ordinary Minkowski spacetime, or, more radically, can be ascribed to changes of the Minkowskian structure itself. In order to understand which possibilities are there for the latter deviations, we shall tinker with the founding pillars of special relativity.

To begin with, it is worth stressing that the features of relativistic kinematics admit two possible interpretations. One can believe that they reveal some underlying "spacetime structure", which surfaces through the dynamics of observers and measuring devices, but exists independently of these systems. However, this conclusion is not mandatory, and one can also take a less elaborate view, in which "spacetime structure" is just a convenient notion to express structural properties of measurements. Thus, space and time are just bookkeeping devices useful to organise such measurements, rather than physical entities on their own. In this sense, whether there is or not a regime in which it makes sense to speak of a spacetime, depends on the feasibility (in principle) of these operations. This is the view that lies, often implicitly, behind most derivations of the Lorentz transformation, and is the one we shall adopt in the following.

A postulate lying at the very foundations of classical, non-gravitational physics is that, in any given region of spacetime, one can find at least one system of observers, define procedures for synchronising clocks, and choose units for length, such that the distance between any two observers does not depend on time, and that such distances satisfy the Euclidean axioms. Moreover, clocks are chosen to measure time in such a way that the most elementary laws of physics take their simplest form [5].

These assumptions are seldom made explicitly, but are fundamental in the development of both Newton's and Einstein's mechanics. We shall refer to them collectively as postulate (A). Among many other things, they allow us to describe events using the Lorentzian frames germane to all treatments of relativistic kinematics, i.e. an ordered set of coordinates x^a (a=1,2,3,4, with $x^4=t$), with the following operational meaning: the differences $\Delta x^a=x_Q^a-x_P^a$ for some ordered pair of events (P,Q) are values of distances and durations measured by the observers.

Lorentzian frames differing from each other by spatial rotations and translations, and by time translations, are physically equivalent — they correspond to the same system of observers, for which (A) is supposed to hold. Experience, however, suggests that such a system of observers is not unique: if (A) holds for a system of observers, then it holds also for any other system whose observers have all the same constant velocity with respect to the first system. We shall call this postulate (B).

We can then consider the maps $x'^a = f^a(x^1, x^2, x^3, x^4; v)$, relating the Lorentzian coordinates of an event in two frames adapted to the two systems of observers (v is the velocity of the second frame with respect to the first one). It has been known for more than a century, starting from the pioneering work by von Ignatowsky, that the form of the maps f^a can be derived assuming only four hypotheses [4, 6, 7]:

- (i) Spatial and temporal homogeneity (equivalence of all locations in space, and instants of time);
- (ii) Spatial isotropy (equivalence of all directions in space);
- (iii) Principle of relativity (absence of a preferred frame mathematically, this property bestows a group structure on the functions f^a);
- (iv) Pre-causality (the temporal ordering of events occurring at the same spatial location in one frame cannot be reversed in another frame).

The result is the Lorentz transformation, containing an undetermined constant with the meaning of an invariant speed. The latter might in principle be infinite (yielding the Galilei transformation), but experiments show that it coincides with the speed of light in vacuum.

Summarising, the Minkowskian structure is a consequence of postulates (A) and (B), and of assumptions (i)–(iv). Therefore, a mesoscopic regime

exists where spacetime structure deviates from the special relativistic one, only if at least one of these postulates/assumptions does not hold. This point is worth stressing, for Lorentz invariance is often identified with the relativity principle. Actually, a violation of *any* of the assumptions above would result in a departure from Lorentz invariance. Let us then explore the various possibilities.

The most robust assumption in the list above is probably pre-causality (iv). Dropping it is almost tantamount to giving up the possibility of doing physics, so we shall keep it. Note that this claim does not express any belief about possible fundamental properties of time, but is only a requirement about clock measurements, and their use in coordinating physical phenomena.

One obvious option is to relinquish the principle of relativity (iii), which results in a vast catalogue of proposals [8]. However, many eminent models of quantum/emergent gravity enforce this principle at the very fundamental level [2, 9], and quite tight experimental constraints have been cast [4].

A breakdown of isotropy at a kinematical level — assumption (ii) — is fully compatible with the relativity principle and theoretically viable, provided that one trades the pseudo-Riemannian metric for a pseudo-Finslerian one, the manifold structure of spacetime remaining intact [7, 10]. Yet, the onset of a privileged direction in space is not the kind of effect one would expect to emerge from an underlying quantum regime.

We are thus left, among assumptions (i)–(iv), only with spatial and temporal homogeneity (i). The technical role of this hypothesis is to make the functions f^a linear in the x^a . Indeed, this is a very powerful implication: once linearity is established, no room is left for any constant with dimensions other than a speed. It seems, then, that (i) is the ingredient to give up if one wants to recover some kind of scale dependence, with some fundamental length like ℓ_P appearing in the f^a . Relaxing homogeneity/linearity, however, amounts to abandoning the operational interpretation of the coordinates x'^a , for the differences $\Delta x'^a$ no more account for any duration and/or length in a given reference frame. If the relativity principle (iii) is still supposed to hold, this is true also for the coordinates x^a — for those in any frame, actually. But the possibility to set up coordinates with a straightforward operational interpretation is a very basic assumption, guaranteed by postulate (A). It results that any attempt to weaken homogeneity demands a radical redefinition of ground-level concepts.

We have shown that, if one assumes that spacetime in the mesoscopic regime still obeys postulates (A), (B), plus hypotheses (i)–(iv), then it has a full Minkowskian structure, and it makes no sense at all to call it "mesoscopic". In this case, if anything unforeseen crops up at a microscopic level, it does so abruptly, as in a second-order phase transition.

On the other hand, if one wants to keep the relativity principle (iii), but is nevertheless open to abandoning one of the other hypotheses, then the only convincing possibility is to relax the very postulate (A). The spacetime structure at scales smaller than ℓ would thus be significantly different from that in the macroscopic domain — "mild" deformations (such as, e.g., those accounting for spatial anisotropy [7]) are not enough. This might lead, among other effects, to radically new phenomenology, such as that accounted for by (possibly curved) non-commutative phase space, and/or non-associative velocity space [11]. But this regime would not be "mesoscopic" in any meaningful way, as strong effects on large scale physics would be generically expected [12]. Similarly, a scenario containing nonlocal defects [13] would not allow for an operational construction of spacetime, if one assumes that such defects could also alter the worldlines of observers.

The above argument can be rephrased in terms of symmetries of the physical laws. If (A), (B), and (i)–(iv) all apply, we must expect strictly Poincaré-invariant laws, at any scale down to ℓ_P . If, on the other hand, at least one of our postulates/assumptions breaks down around ℓ , the laws of physics will no longer be Poincaré-invariant at smaller scales. If isotropy and the relativity principle are not affected, such symmetry breaking can only be severe — not necessarily unviable, but potentially tightly constrained.

Remarkably, exact Poincaré invariance does not prevent a priori the onset of new physics in the mesoscopic regime. It is still possible that the very mechanisms leading to the sudden emergence of a classical spacetime end up introducing new Lorentz- and translation-invariant terms in the standard physical laws, suppressed by coefficients depending on powers of some ℓ —hence, negligible at macroscopic scales (see, e.g., [3]).

"Spacetime" is a powerful word indeed. When seen as a "grand stage" for physical phenomena, we ought to either take it as is, or rebuild it from scratch — it seems to offer no place for intermediate regimes. As a synonym for physical laws and their symmetries, however, it can provide room for a potentially rich, unforeseen phenomenology.

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